

# E- and F-region Electric Fields, Conductivities, and Currents from PFISR

AMISR Summer School: Group 4

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# Outline

- 1 Experiment Goals and Design
- 2 Estimating the Electron Densities
- 3 Estimating the Pedersen Conductivity
- 4 Estimating Electric Fields
- 5 Estimating Currents and Joule Heating

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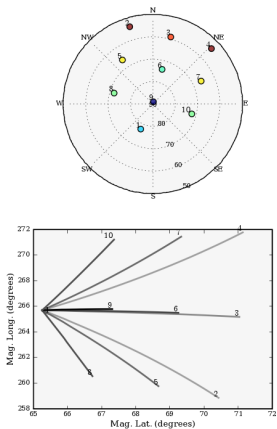
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# Experiment Goals

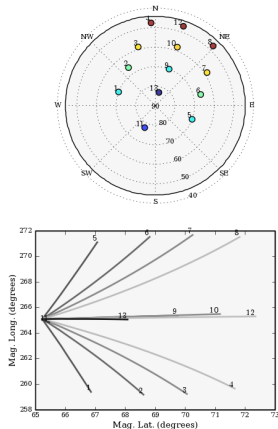
- 1 Measure the latitude and longitude variation of the F-region electric field and the E-region ion velocity.
- 2 Pulses: Combination of Long pulses and AC pulses, with a grid of 3 x 3 beams. One of the beams was pointed along B in order to get neutral winds.
- 3 Time of Experiment: This might be particularly interesting during auroral activity, so we requested 00 - 02 LDT or 8 - 10 UT.
- 4 Number of beams: 10

# Beam Positions

Our Experiment:

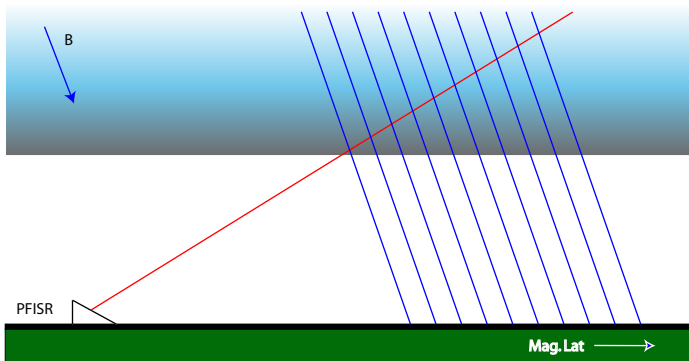


Lyons02 Experiment:



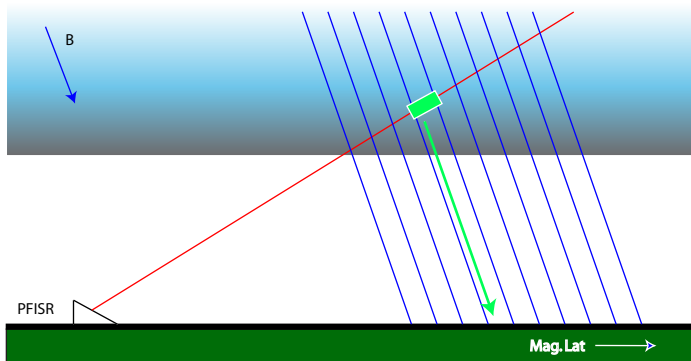
# Velocities as a function of Latitude

Viewing from the East:



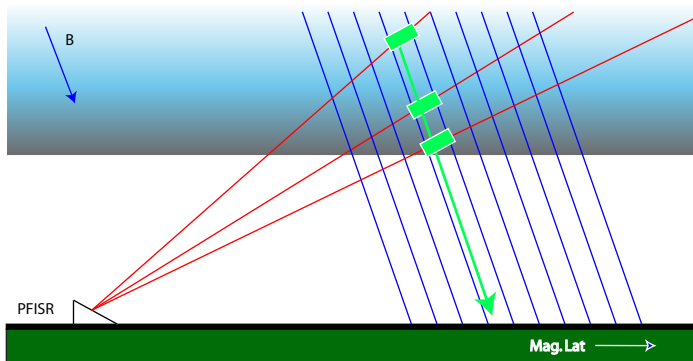
# Velocities as a function of Latitude

Range bin corresponds to a latitude bin



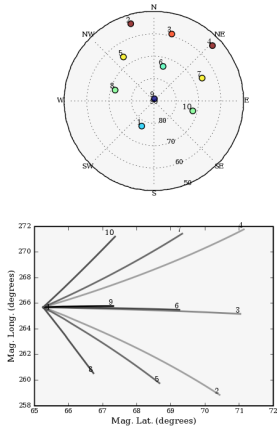
# Velocities as a function of Latitude

Multiple beams give redundant measurements





# Beam Positions Revisited



# Extracting the Vector Velocities

$$v_{los}^i = k_x^i v_x + k_y^i v_y + k_z^i v_z = \mathbf{k}^i \cdot \mathbf{v}$$

$$\mathbf{k} = \hat{e} \cos \theta \sin \phi + \hat{n} \cos \theta \cos \phi + \hat{z} \sin \theta$$

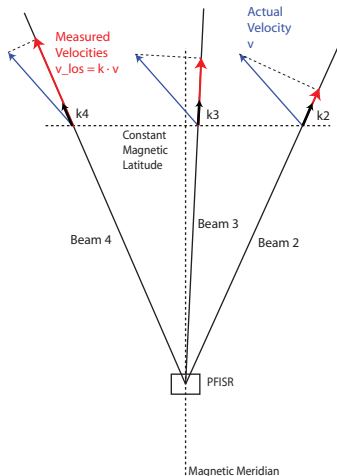
with two or more measurements:

$$v_{los}^i = \mathbf{k}^i \cdot \mathbf{v} + e_{los}^i$$

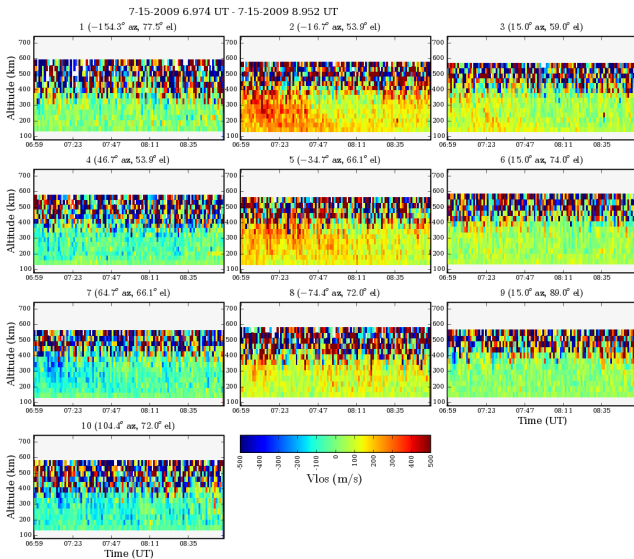
$$\begin{bmatrix} v_{los}^1 \\ v_{los}^2 \\ \vdots \\ v_{los}^n \end{bmatrix} = \begin{bmatrix} k_{pe}^1 & k_{pn}^1 & k_{ap}^1 \\ k_{pe}^2 & k_{pn}^2 & k_{ap}^2 \\ \vdots & \vdots & \vdots \\ k_{pe}^n & k_{pn}^n & k_{ap}^n \end{bmatrix} \begin{bmatrix} v_{pe} \\ v_{pn} \\ v_{ap} \end{bmatrix} + \begin{bmatrix} e_{los}^1 \\ e_{los}^2 \\ \vdots \\ e_{los}^n \end{bmatrix}$$

then,  $\mathbf{v}$  is estimated as:

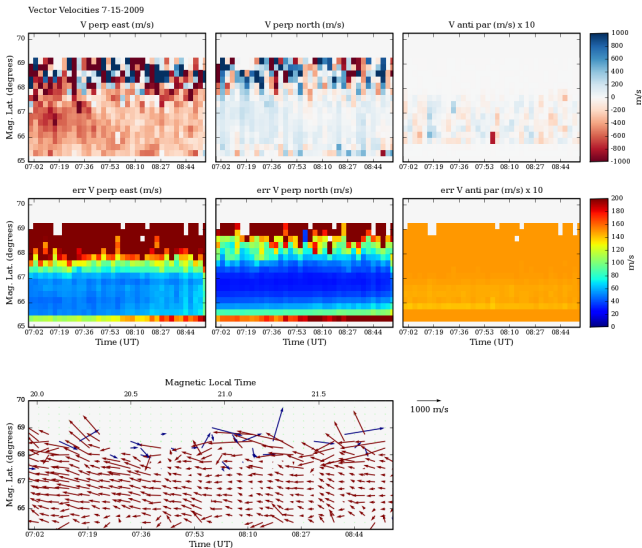
$$\hat{\mathbf{v}} = \Sigma_v \mathbf{A}^T (\mathbf{A} \Sigma_v \mathbf{A}^T + \Sigma_e)^{-1} \mathbf{v}_{los}$$



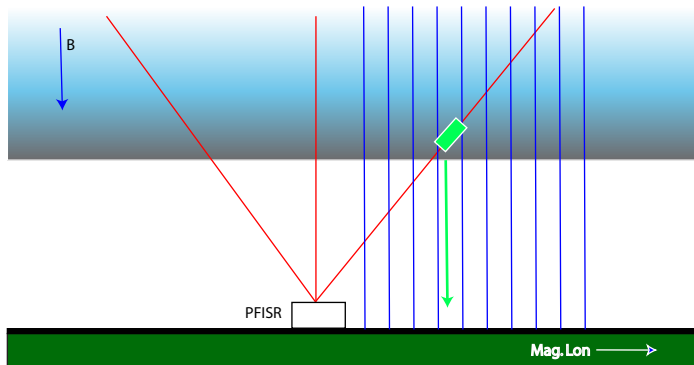
# Derived Velocities c/o Mike Nicolls



# Derived Velocities c/o Mike Nicolls



# Velocity as a function of Longitude?



# Simple 2-beam calculation

From *Heiselman and Nicolls*, RS, 2008; neglecting Earth curvature,

$$\mathbf{k}' = \begin{bmatrix} k_{pe} \\ k_{pn} \\ k_{ap} \end{bmatrix} = R_{geo \rightarrow gmag} \cdot \mathbf{k} = \begin{bmatrix} \cos \delta & -\sin \delta & 0 \\ \sin / \sin \delta & \cos \delta \sin / & \cos / \\ -\cos / \sin \delta & -\cos / \cos \delta & \sin / \end{bmatrix} \begin{bmatrix} \cos \theta \sin \phi \\ \cos \theta \cos \phi \\ \sin \theta \end{bmatrix}$$

given a  $k$  for each beam, and assuming the velocity along B is negligible,

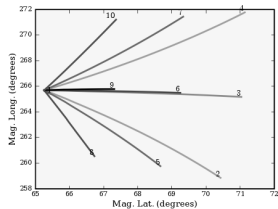
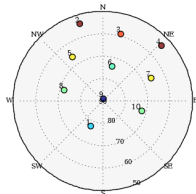
$$v_{pn}^{2,8} = \frac{v_{los}^2 - \frac{k_{pe}^2}{k_{pe}^8} v_{los}^8}{k_{pn}^2 \left( 1 - \frac{k_{pn}^8 k_{pe}^2}{k_{pn}^2 k_{pe}^8} \right)}$$

$$v_{pn}^{4,10} = \frac{v_{los}^4 - \frac{k_{pe}^4}{k_{pe}^{10}} v_{los}^{10}}{k_{pn}^4 \left( 1 - \frac{k_{pn}^{10} k_{pe}^4}{k_{pn}^4 k_{pe}^{10}} \right)}$$

$$v_{pe}^{2,8} = \frac{v_{los}^8 - \frac{k_{pn}^8}{k_{pn}^2} v_{los}^2}{k_{pe}^8 \left( 1 - \frac{k_{pn}^8 k_{pe}^2}{k_{pn}^2 k_{pe}^8} \right)}$$

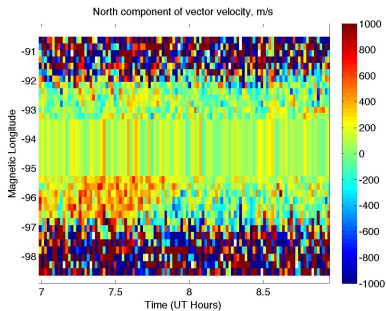
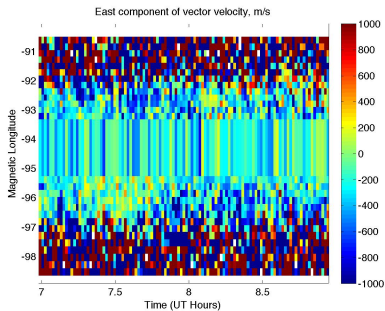
$$v_{pe}^{4,10} = \frac{v_{los}^{10} - \frac{k_{pn}^{10}}{k_{pn}^4} v_{los}^4}{k_{pe}^{10} \left( 1 - \frac{k_{pn}^{10} k_{pe}^4}{k_{pn}^4 k_{pe}^{10}} \right)}$$

# Beam Positions Revisited



# Results

Mean velocities: -246.8 m/s East, 66.3 m/s North,  
or 255 m/s at  $-75^\circ$  azimuth

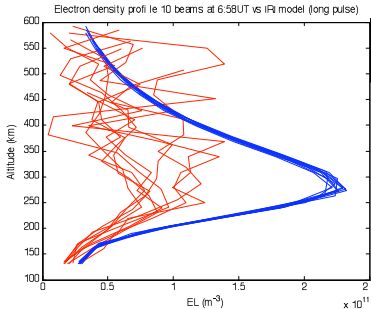


NOTE: We haven't done any calculations of errors!

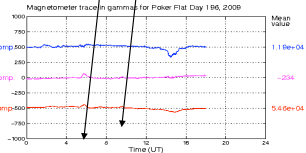


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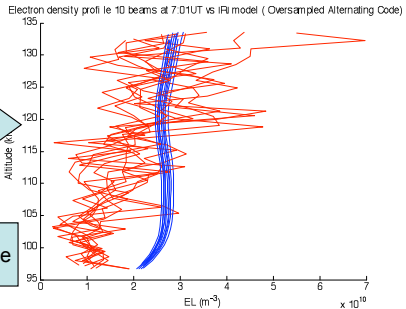


Long Pulse



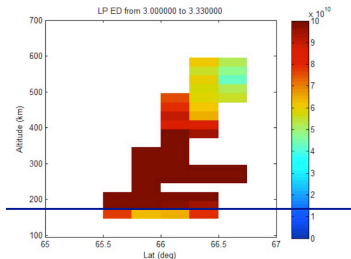
Quiet time  
Still big differences compared with IRI

Alternating Code

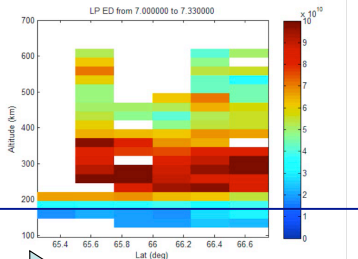


# Long Pulse (E F)

Group 2



Group 4

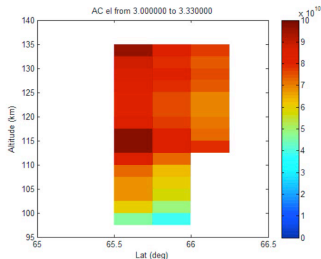


At low altitude, EL enhancement appears  
during disturbed period

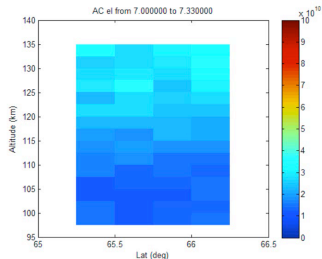


# Alternating code (E)

Group 2



Group 4





## Summary of this part

- IRI model has great differences compared with the real measurement by ISR
- F region peak can be observed by both groups data
- ED is higher at “slightly” disturbed period for E region
- Validation needed to use the “seriously” disturbed period comes after G4 period
- ISR is capable of observing a certain area ionosphere continuously



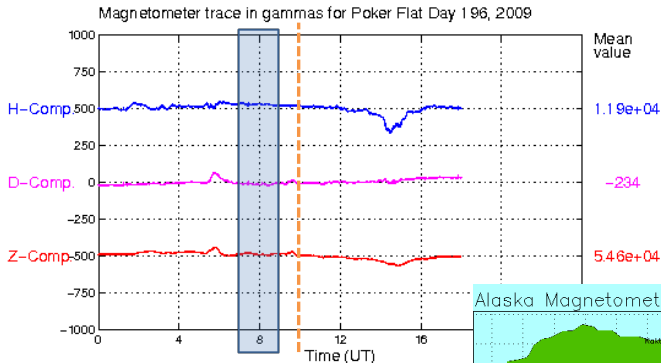


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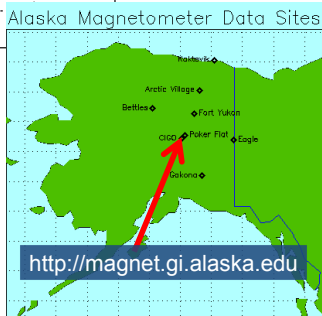


# Magnetometer Data



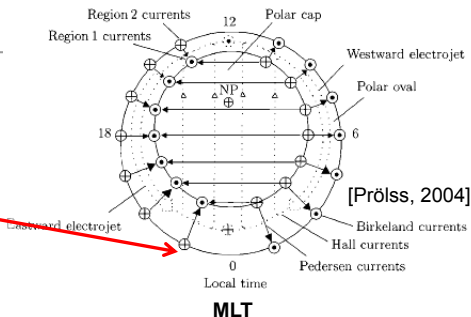
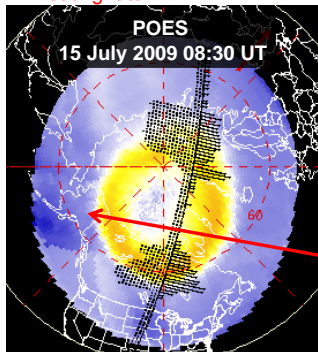
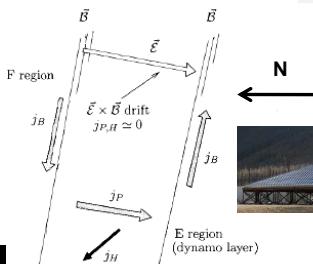
15 July 2009 experiment:  
 07:00 – 09:00 UT  
 (23:00 – 01:00 LDT)

Fairbanks magnetic midnight is ~10:00 UT

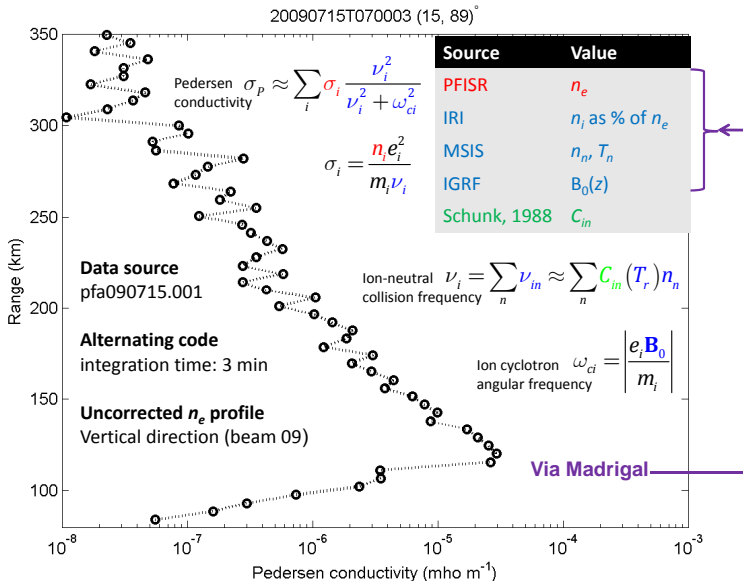


# Methodology

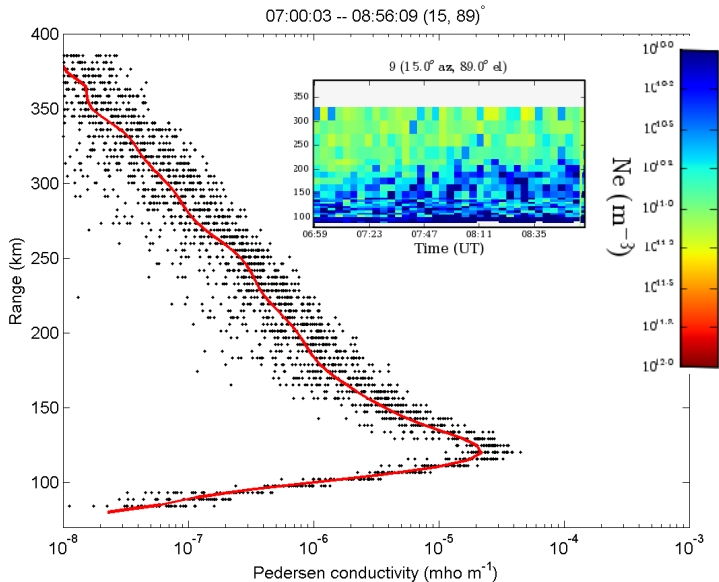
1. Measure F-region  $V_{i\perp}$  with PFISR long pulse
2. Assume  $\mathbf{E} \times \mathbf{B}$  drift to infer  $\mathbf{E}$
3. Estimate  $\sigma_p$  from PFISR  $n_e$  and MSIS model  $n_n$
4. Calculate  $j_p$  and Joule heating rate



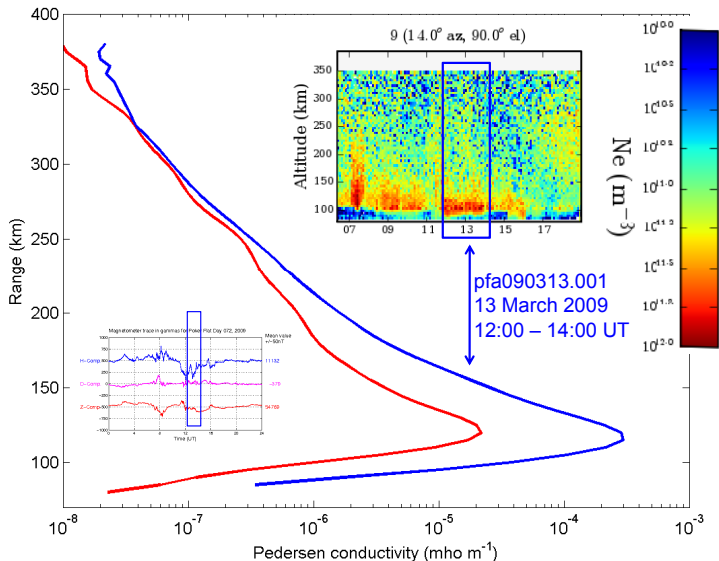
# Extracting the Conductivity



# Conductivity Profiles



# Comparison with Storm-time Data

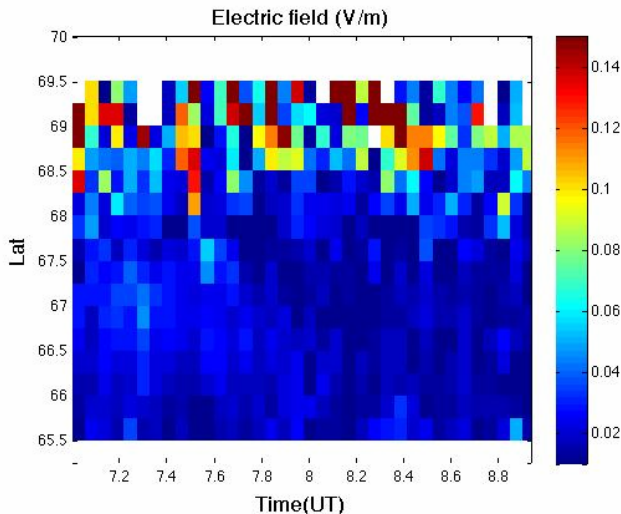


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## Electric Fields

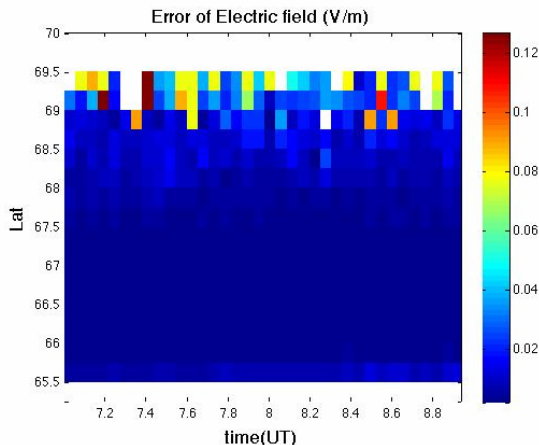
Calculated electric field:  $|E| = |V_i| |B|$



# Errors in Electric Field

Propagated errors of electric field:

$$\sigma_E^2 = \left(\frac{\partial E}{\partial V_{\perp N}}\right)^2 \sigma_{V_{\perp N}}^2 + \left(\frac{\partial E}{\partial V_{\perp E}}\right)^2 \sigma_{V_{\perp E}}^2$$





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# Calculating Current Density

## Method to calculate current density

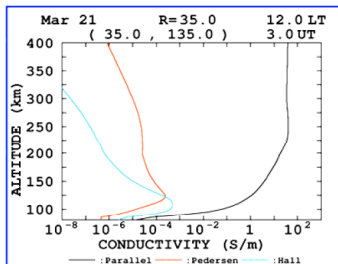
### Method 1:

$$\mathbf{j}' = n \cdot e \cdot (v_i' - v_e') = n \cdot e \cdot (v_i - v_n - (v_e - v_n)) = n \cdot e \cdot (v_i - v_e)$$

### Method 2:

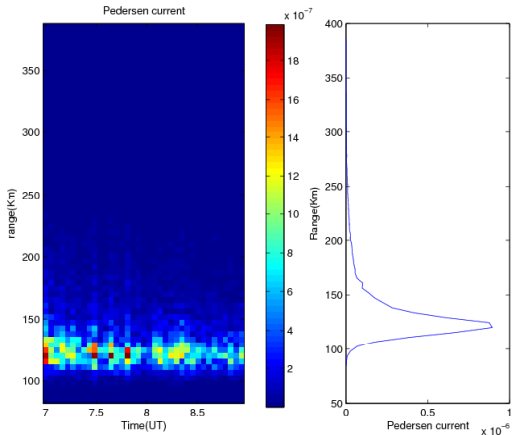
$$\mathbf{j}' = n \cdot e \left\{ \left( \frac{k_e}{1+k_e^2} + \frac{k_i}{1+k_i^2} \right) \frac{\mathbf{E}'}{B} - \left( \frac{k_e^2}{1+k_e^2} - \frac{k_i^2}{1+k_i^2} \right) \frac{\mathbf{E}' \times \mathbf{B}}{B^2} + \left( \frac{k_e^3}{1+k_e^2} - \frac{k_i^3}{1+k_i^2} \right) \frac{(\mathbf{E}' \cdot \mathbf{B}) \mathbf{B}}{B^3} \right\}$$

$$= \sigma_p \mathbf{E}'_{\perp} - \sigma_H \frac{\mathbf{E}' \times \mathbf{B}}{B} + \sigma_{\parallel} \mathbf{E}'_{\parallel}$$



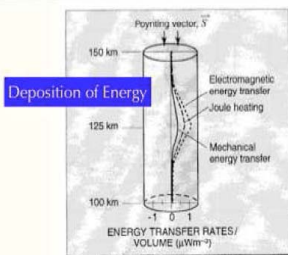
# Pedersen Currents vs. Altitude and Time

## Pedersen current



# Method for Calculating Joule Heating

## Joule heating

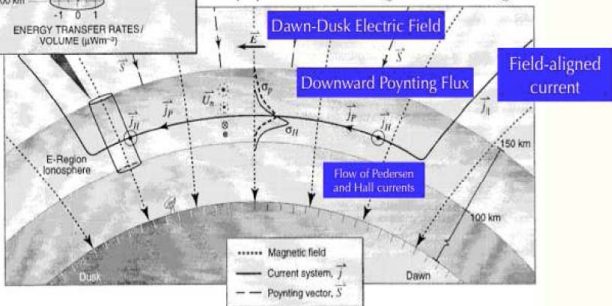


- Supplied electromagnetic energy is converted to heat (Joule heating) or momentum (Lorentz forcing)

$$q_j = \mathbf{j} \cdot \mathbf{E}' = \mathbf{j} \cdot (\mathbf{E} + \mathbf{U} \times \mathbf{B}) = \sigma_P |\mathbf{E} + \mathbf{U} \times \mathbf{B}|^2$$

$$q_m = \mathbf{U} \cdot (\mathbf{j} \times \mathbf{B})$$

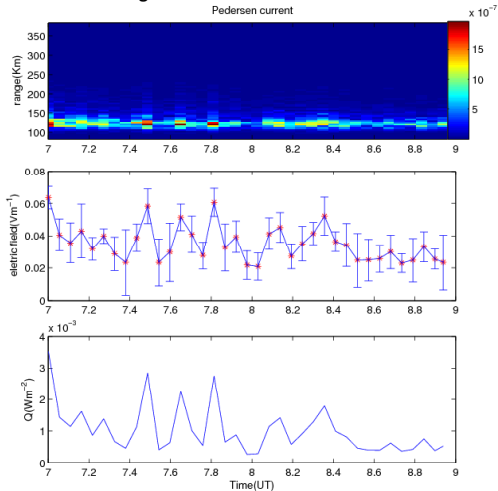
- $q_m$  negative - neutral gas is a sink (load)
- $q_m$  positive - neutral gas is a source (generator)



Thayer [2000]

# Joule Heating vs. Time

## Height Integrated Joule heating rate



# Thanks!

Mike, Craig, Asti,  
Anthea, Anja, Phil,  
Bill, Josh, Sixto,  
Shelley, Mary, John K.