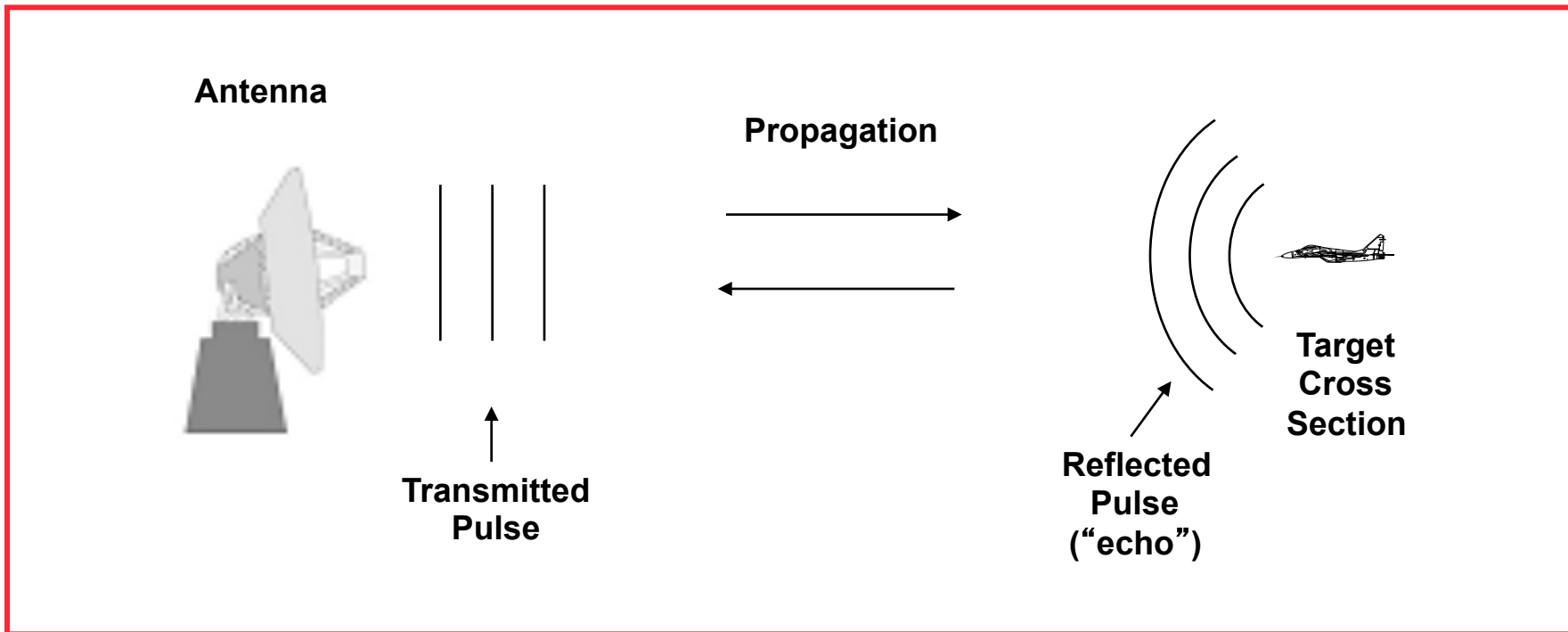




# RADAR

## RAdio Detection And Ranging

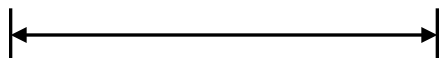
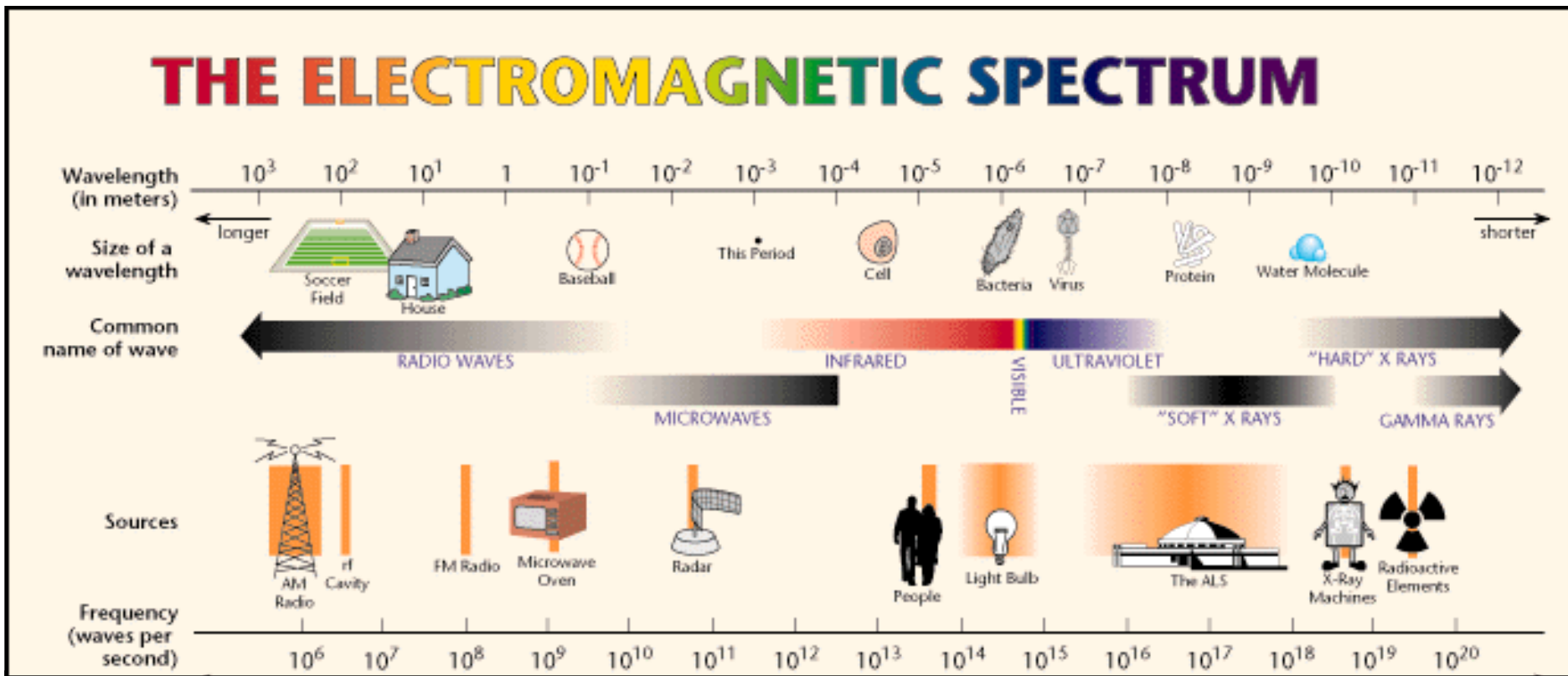


### Radar observables:

- Target range
- Target angles (azimuth & elevation)
- Target size (radar cross section)
- Target speed (Doppler)
- Target features (imaging)



# Electromagnetic Waves

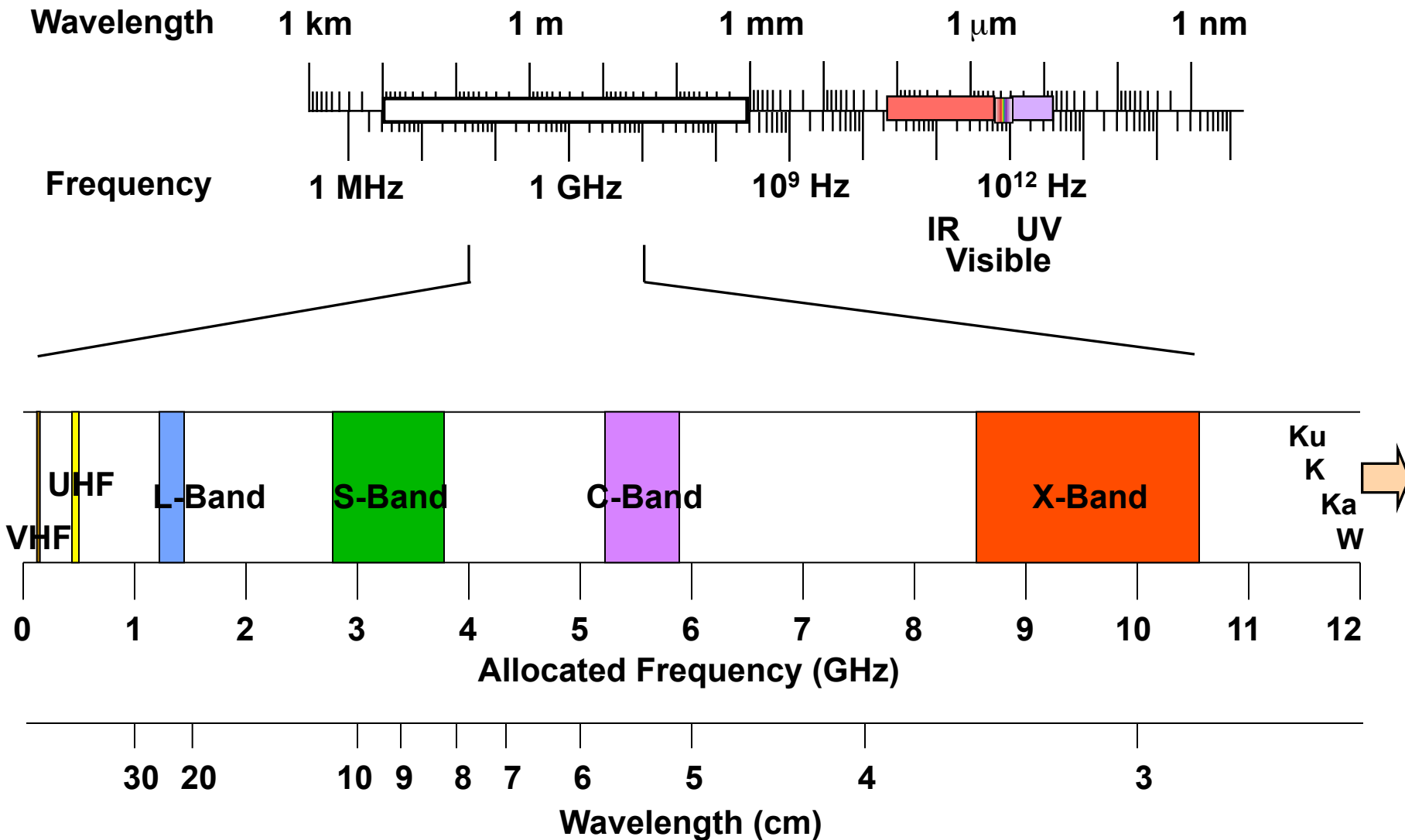


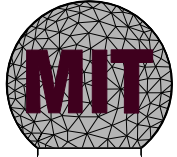
Radar Frequencies



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# Radar Frequency Bands





HAYSTACK OBSERVATORY

# Lincoln Laboratory Satellite Tracking Radars

## Frequency Bands

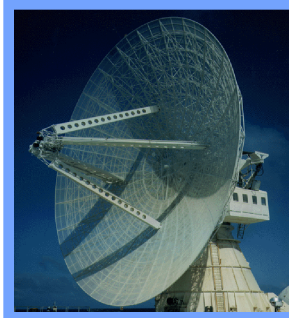
ALTAIR



MILLSTONE



TRADEX



ALCOR



HAY/HAX



MMW



VHF

UHF

UHF

L

L

S

C

X

K<sub>u</sub>

K<sub>a</sub>

W

Freq. Band

0.1

1

FREQUENCY (GHz)

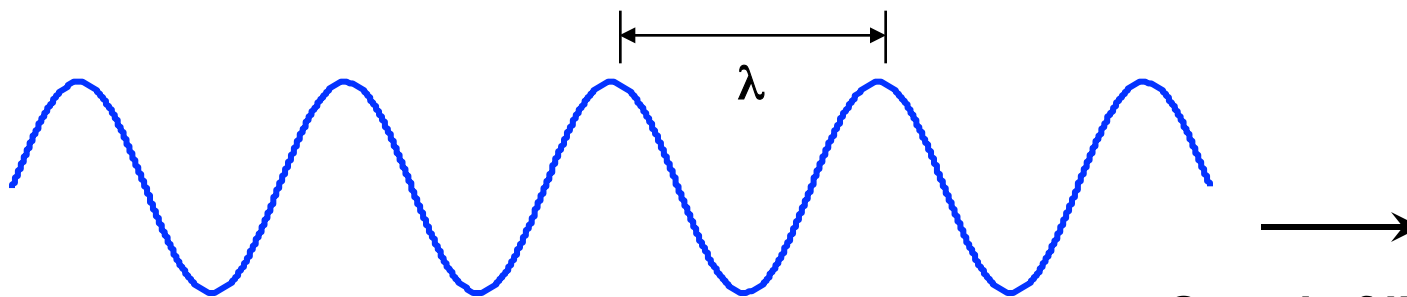
10

100



# Properties of Waves

## Relationship Between Frequency and Wavelength



Speed of light,  $c$   
 $c = 3 \times 10^8$  m/sec  
 $= 300,000,000$  m/sec

$$\text{Frequency (1/s)} = \frac{\text{Speed of light (m/s)}}{\text{Wavelength } \lambda \text{ (m)}}$$

Examples:

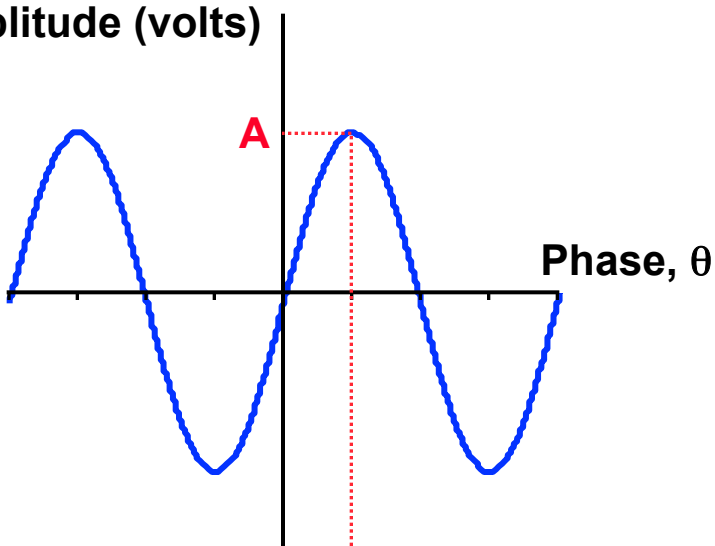
<u>Frequency</u>	<u>Wavelength</u>
100 MHz	3 m
1 GHz	30 cm
3 GHz	10 cm
10 GHz	3 cm



# Properties of Waves

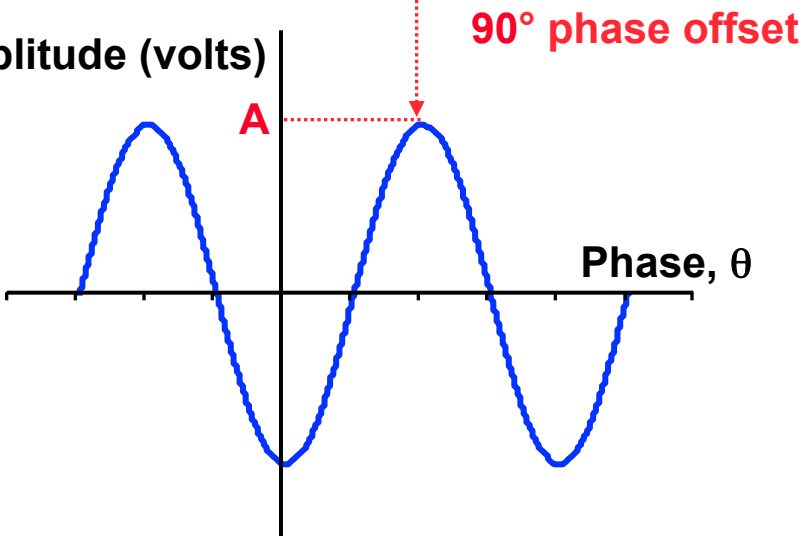
## Phase and Amplitude

Amplitude (volts)



$$A \sin(\theta)$$

Amplitude (volts)

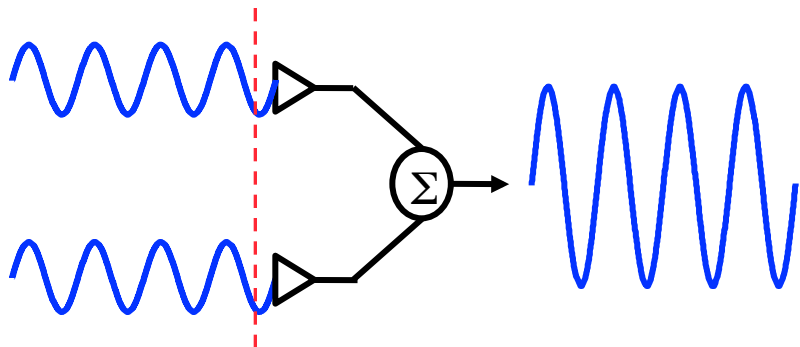


$$A \sin(\theta - 90^\circ)$$

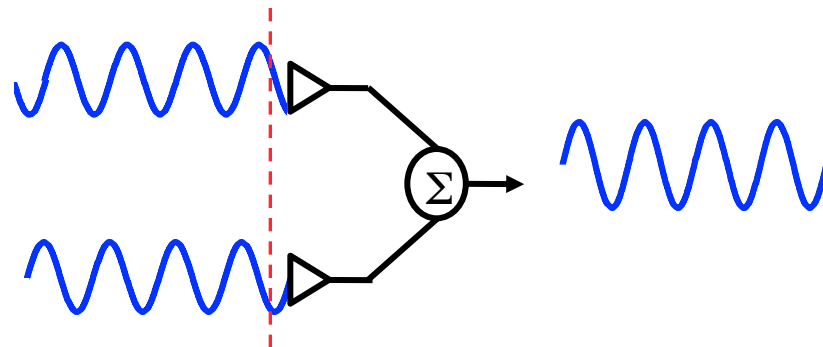


# Properties of Waves

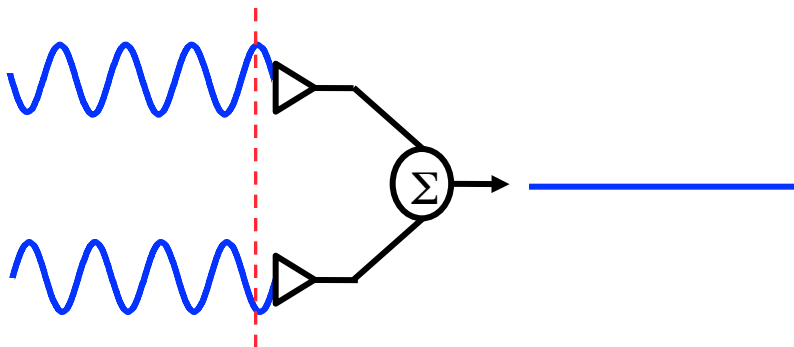
## Constructive vs. Destructive Addition



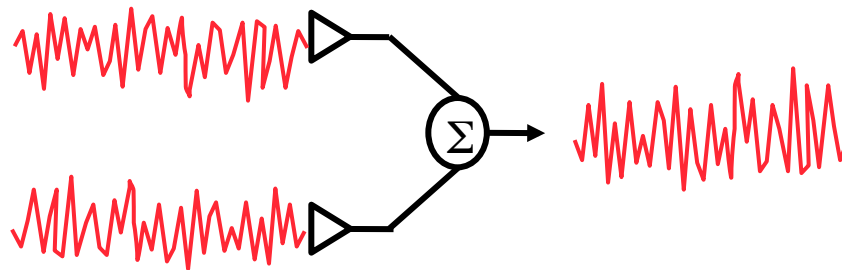
**Constructive**  
(in phase)



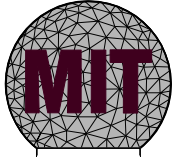
**Partially Constructive**  
(somewhat out of phase)



**Destructive**  
(180° out of phase)

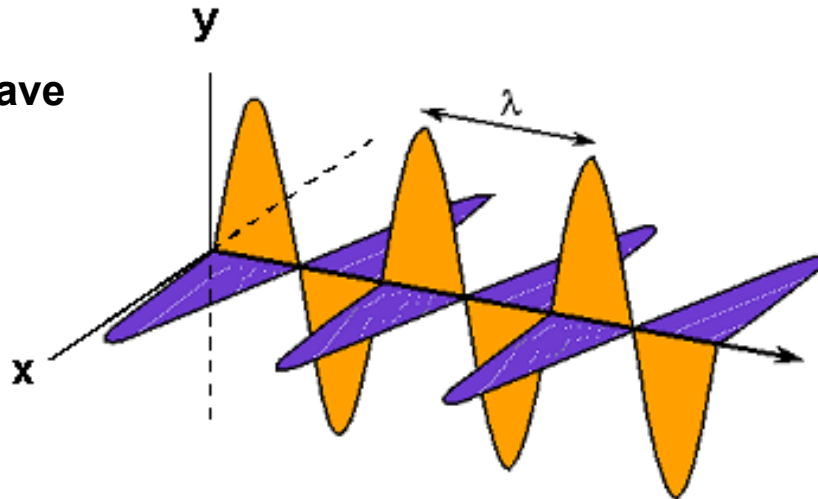


**Non-coherent signals**  
(noise)



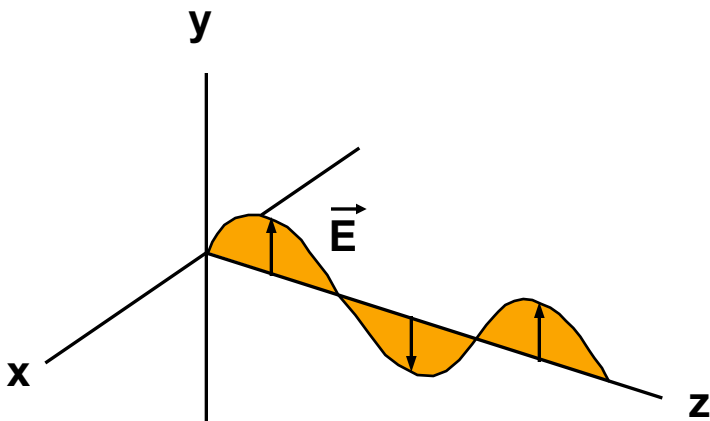
# Polarization

Electromagnetic Wave

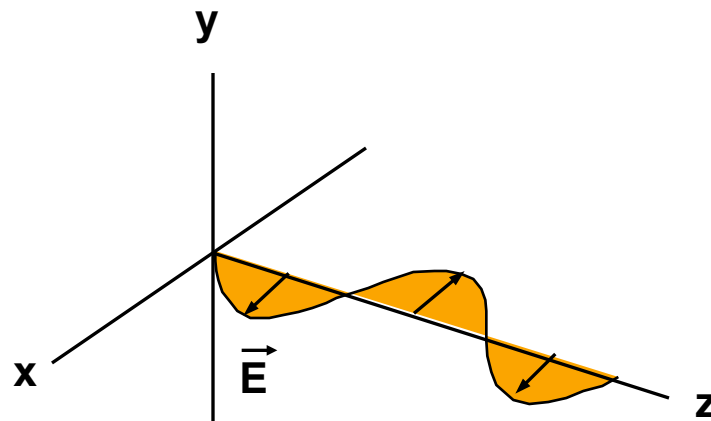


- Electric Field
- Magnetic Field

Vertical Polarization



Horizontal Polarization

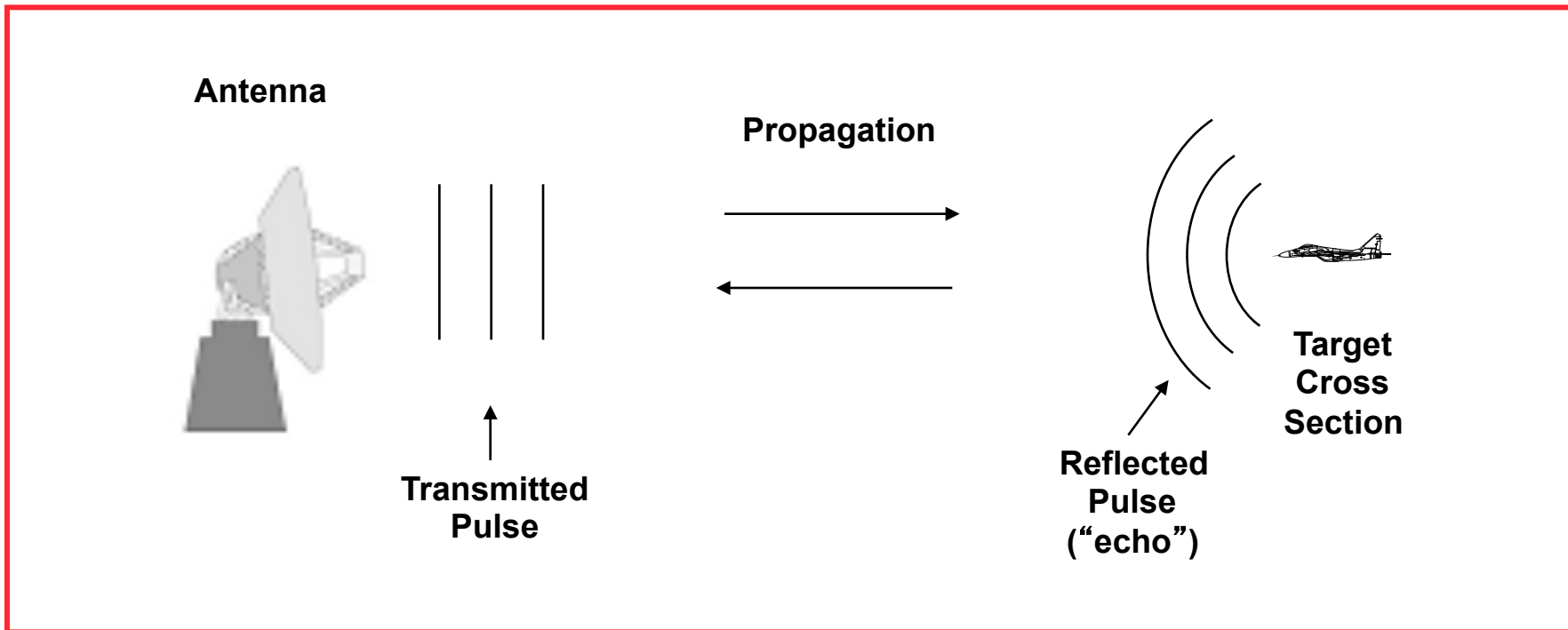






# RADAR

## Radio Detection And Ranging

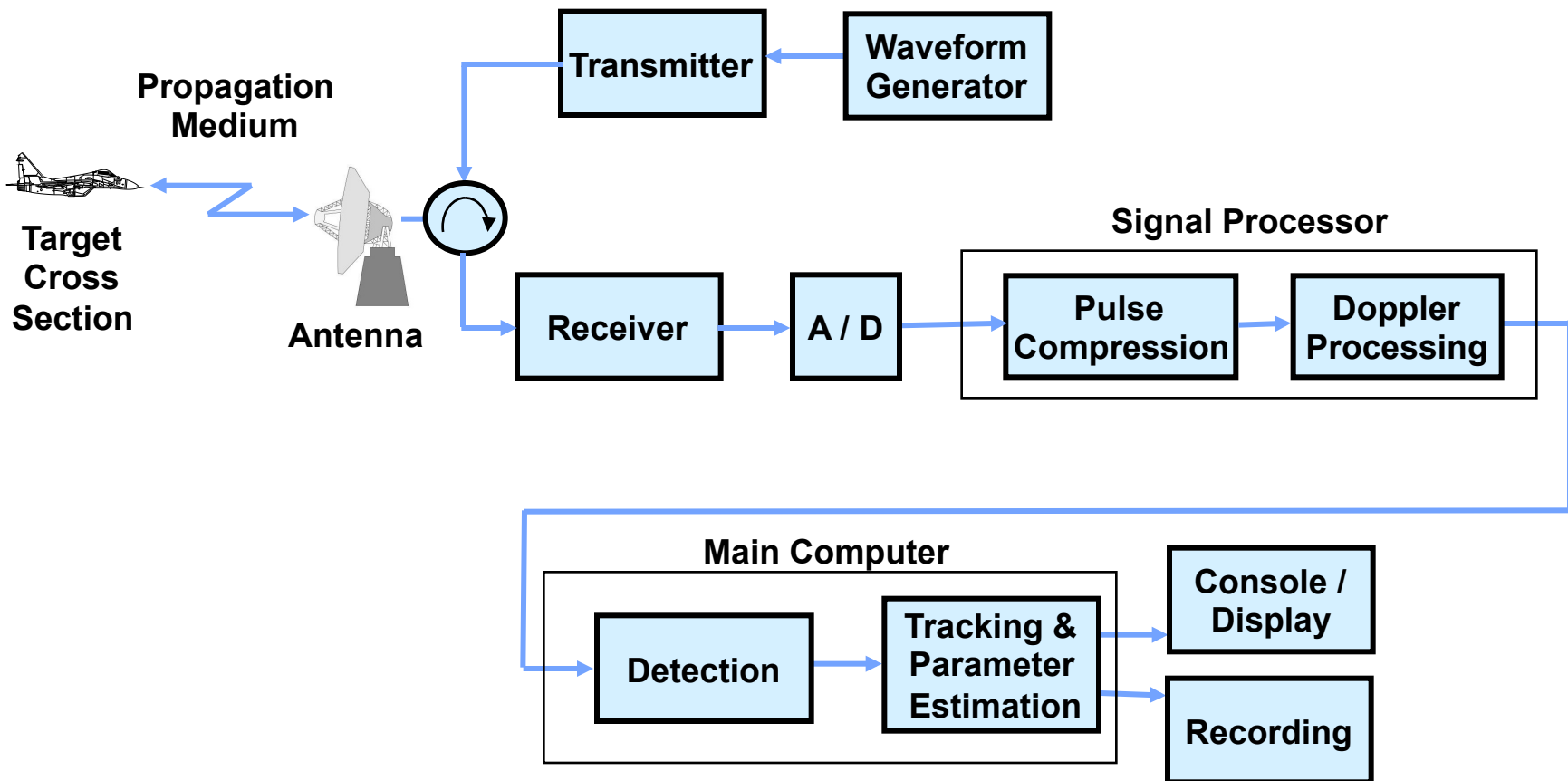


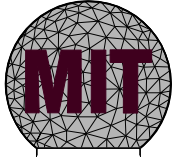
### Radar observables:

- Target range
- Target angles (azimuth & elevation)
- Target size (radar cross section)
- Target speed (Doppler)
- Target features (imaging)

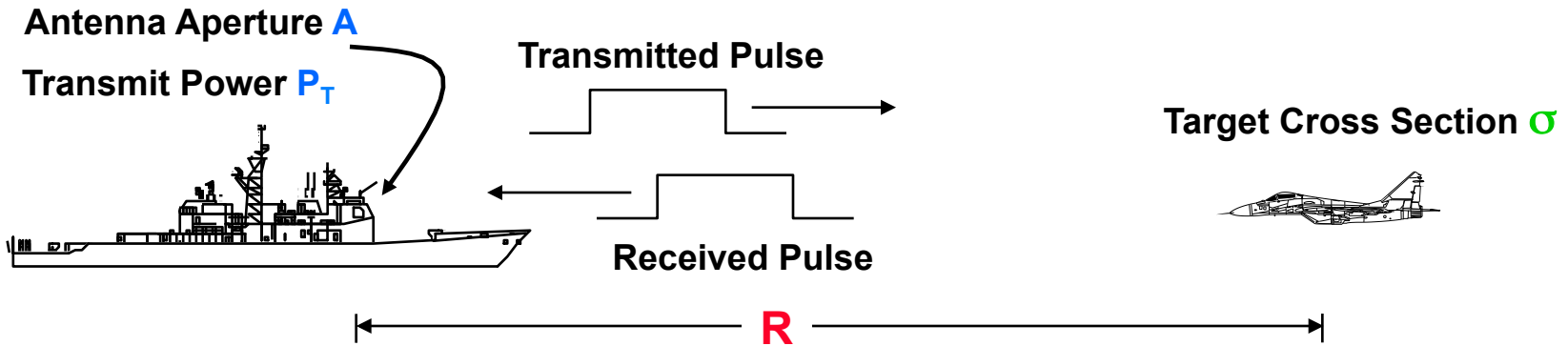


# Radar Block Diagram

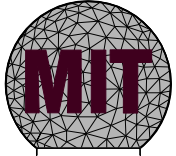




# Radar Range Equation



Received Signal Energy	=	Transmit Power	Transmit Gain	Spread Factor	Losses	Target RCS	Spread Factor	Receive Aperture	Dwell Time
		$[ P_T ]$	$\left[ \frac{4\pi A}{\lambda^2} \right]$	$\left[ \frac{1}{4\pi R^2} \right]$	$\left[ \frac{1}{L} \right]$	$[ \sigma ]$	$\left[ \frac{1}{4\pi R^2} \right]$	$[ A ]$	$[ \tau ]$



# Definition of a dB

The relative value of two things, measured on a logarithmic scale, is often expressed in deciBell's (dB)

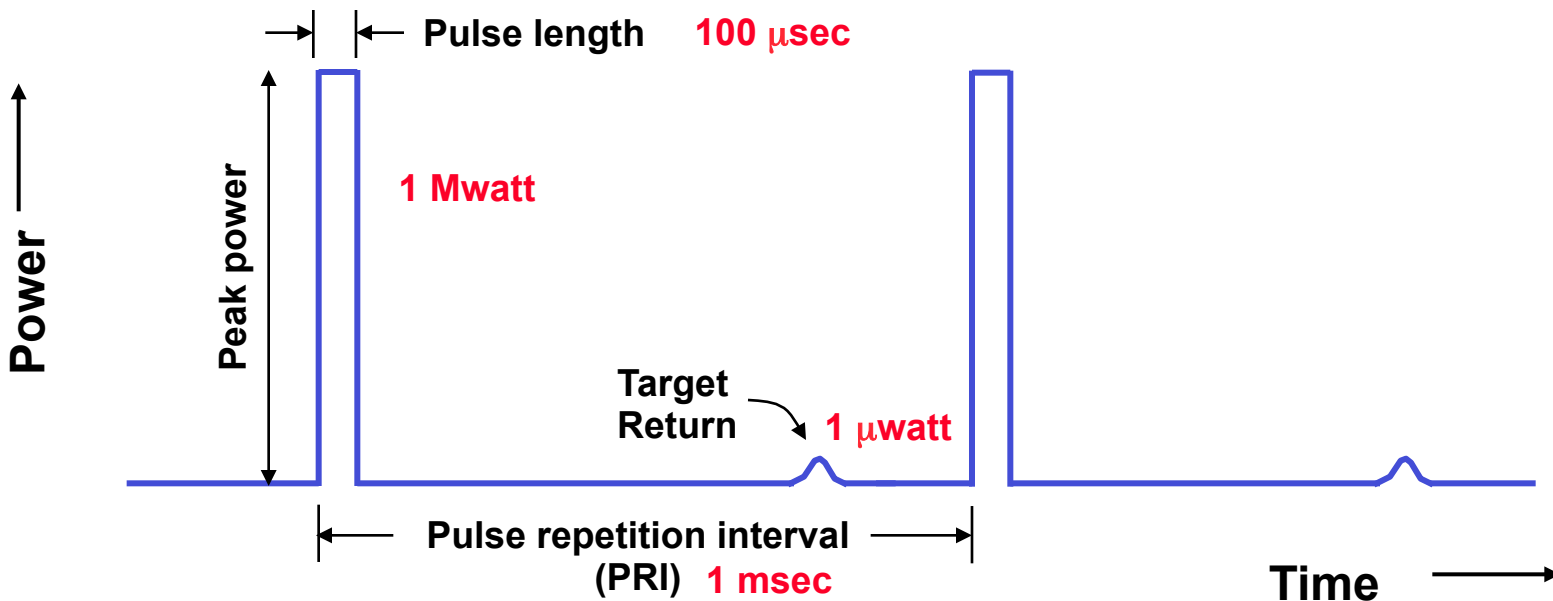
Example:

$$\text{Signal-to-noise ratio (dB)} = 10 \log_{10} \left[ \frac{\text{Signal Power}}{\text{Noise Power}} \right]$$

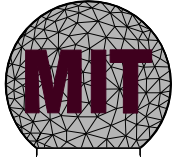
<u>Factor of:</u>	<u>Scientific Notation</u>	<u>dB</u>	
10	10 <sup>1</sup>	10	0 dB = factor of 1
100	10 <sup>2</sup>	20	-10 dB =
1000	10 <sup>3</sup>	30	factor of 1/10
⋮			-20 dB = factor of 1/100
⋮			
1,000,000	10 <sup>6</sup>	60	3 dB = factor of 2
			-3 dB = factor of 1/2



# Pulsed Radar Terminology and Concepts

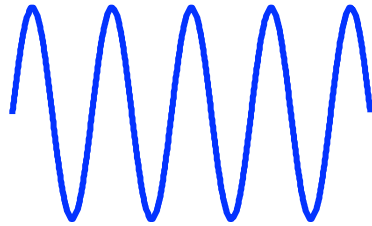


- Duty cycle =  $\frac{\text{Pulse length}}{\text{Pulse repetition interval}}$  **10%**
- Average power = Peak power \* Duty cycle **100 kWatt**
- Pulse repetition frequency (PRF) =  $1/(\text{PRI})$  **1 kHz**
- Continuous wave (CW) radar: Duty cycle = 100% (always on)



# Radar Waveforms

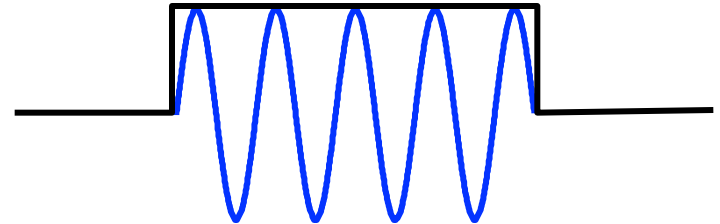
What do radars transmit?



Waves?



or Pulses?

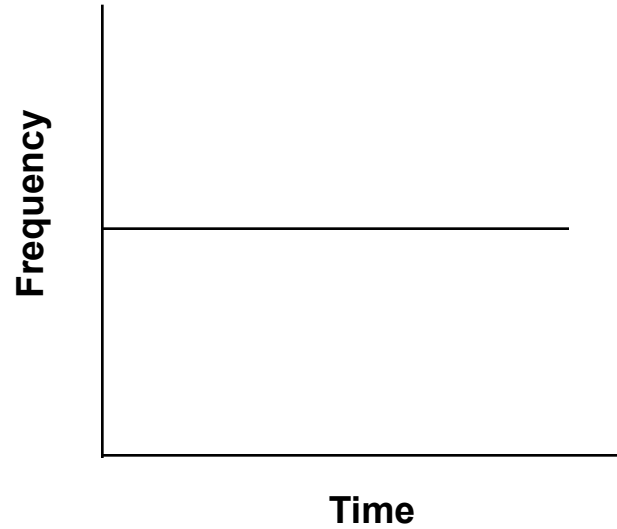
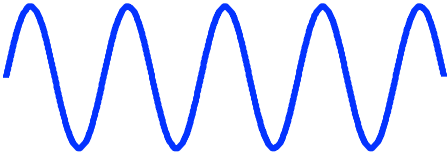


Waves, modulated  
by “on-off” action of  
pulse envelope

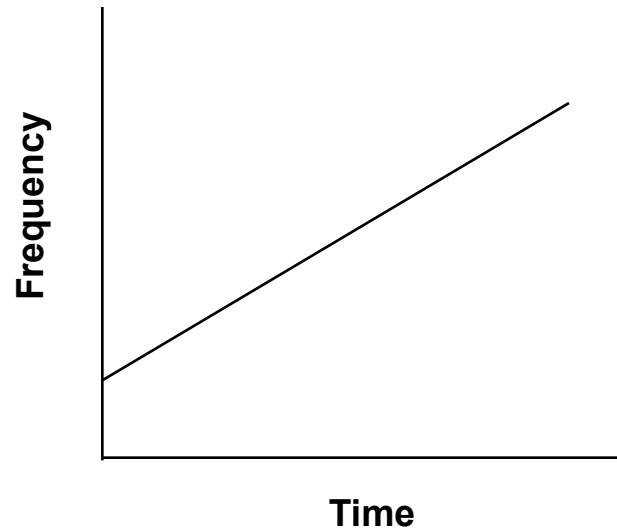
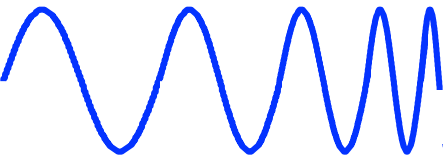


# Radar Waveforms (cont' d.)

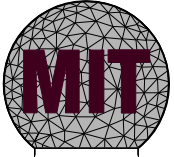
Pulse at single frequency



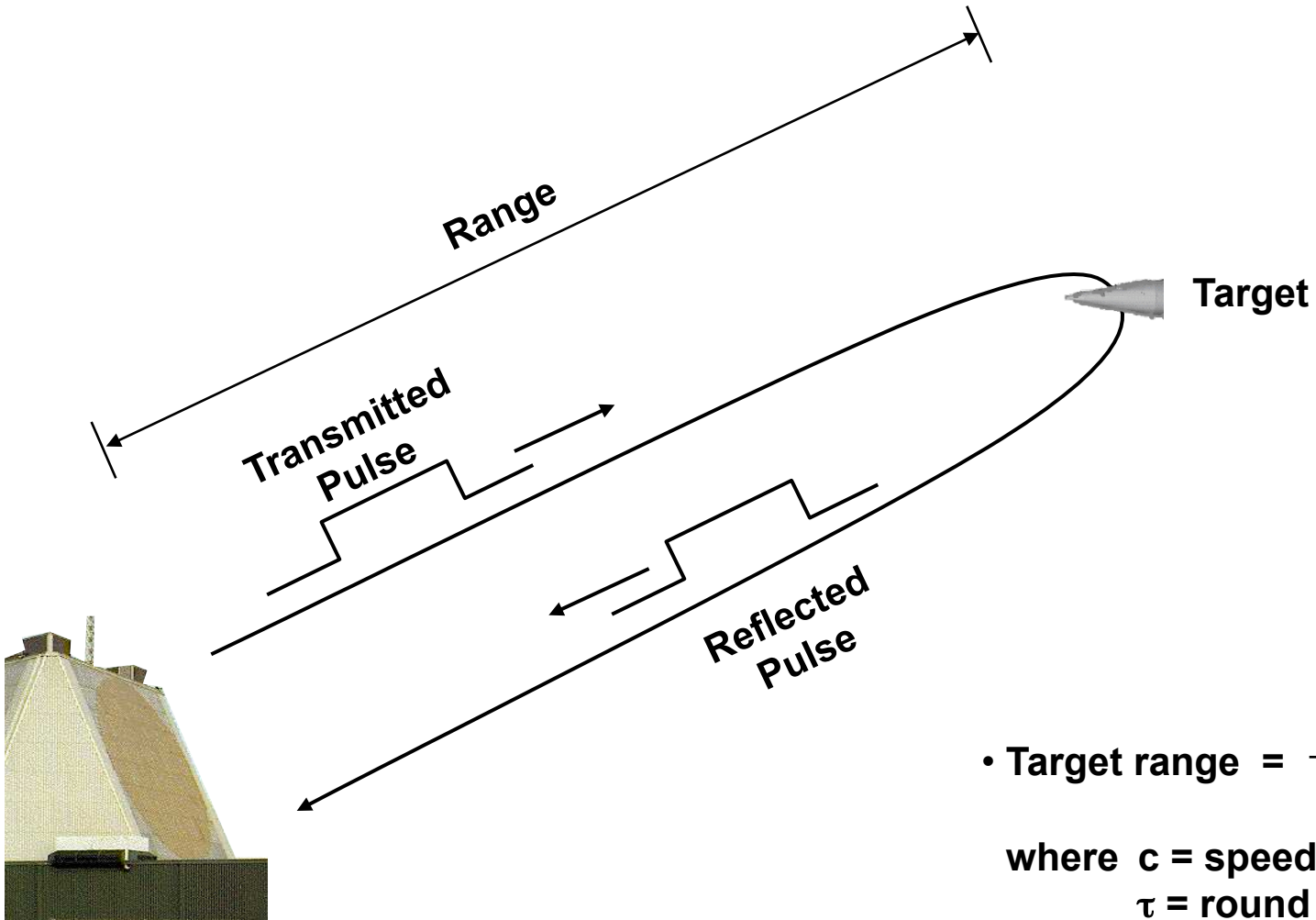
Pulse with changing frequency



**Linear  
Frequency-  
Modulated  
(LFM)  
Waveform**



# Radar Range Measurement



- Target range =  $\frac{c\tau}{2}$

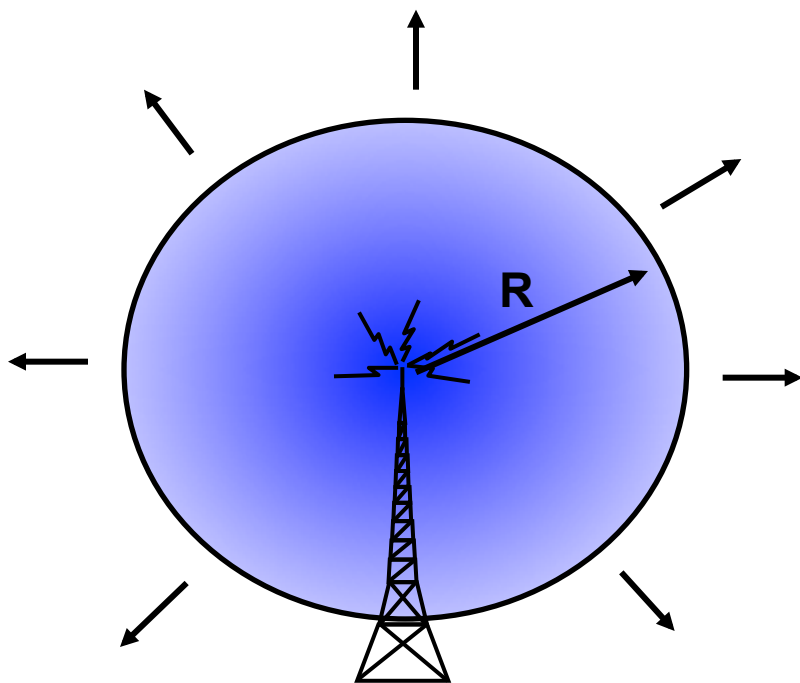
where  $c$  = speed of light  
 $\tau$  = round trip time



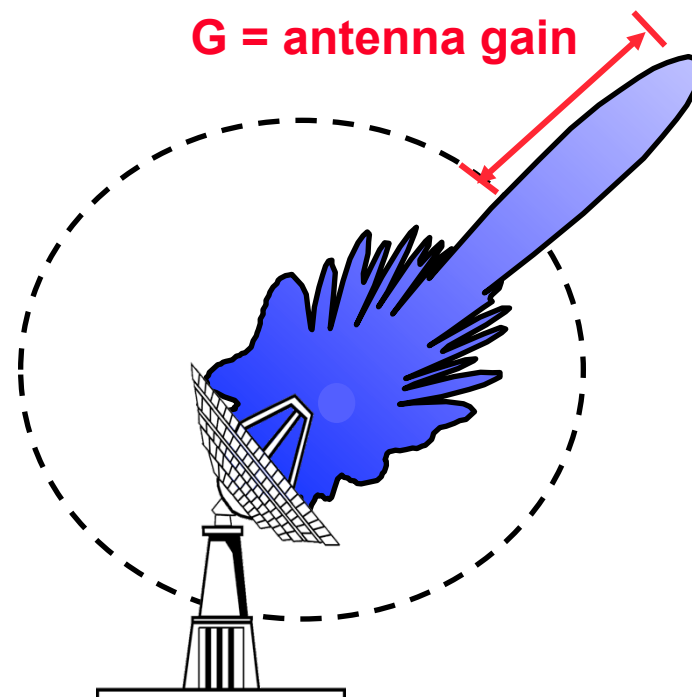


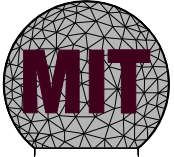
# Antenna Gain

Isotropic antenna



Directional antenna

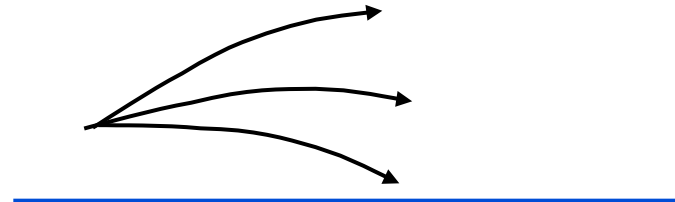
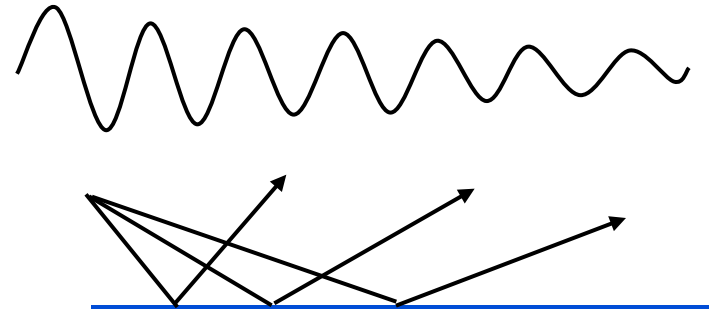




# Propagation Effects on Radar Performance

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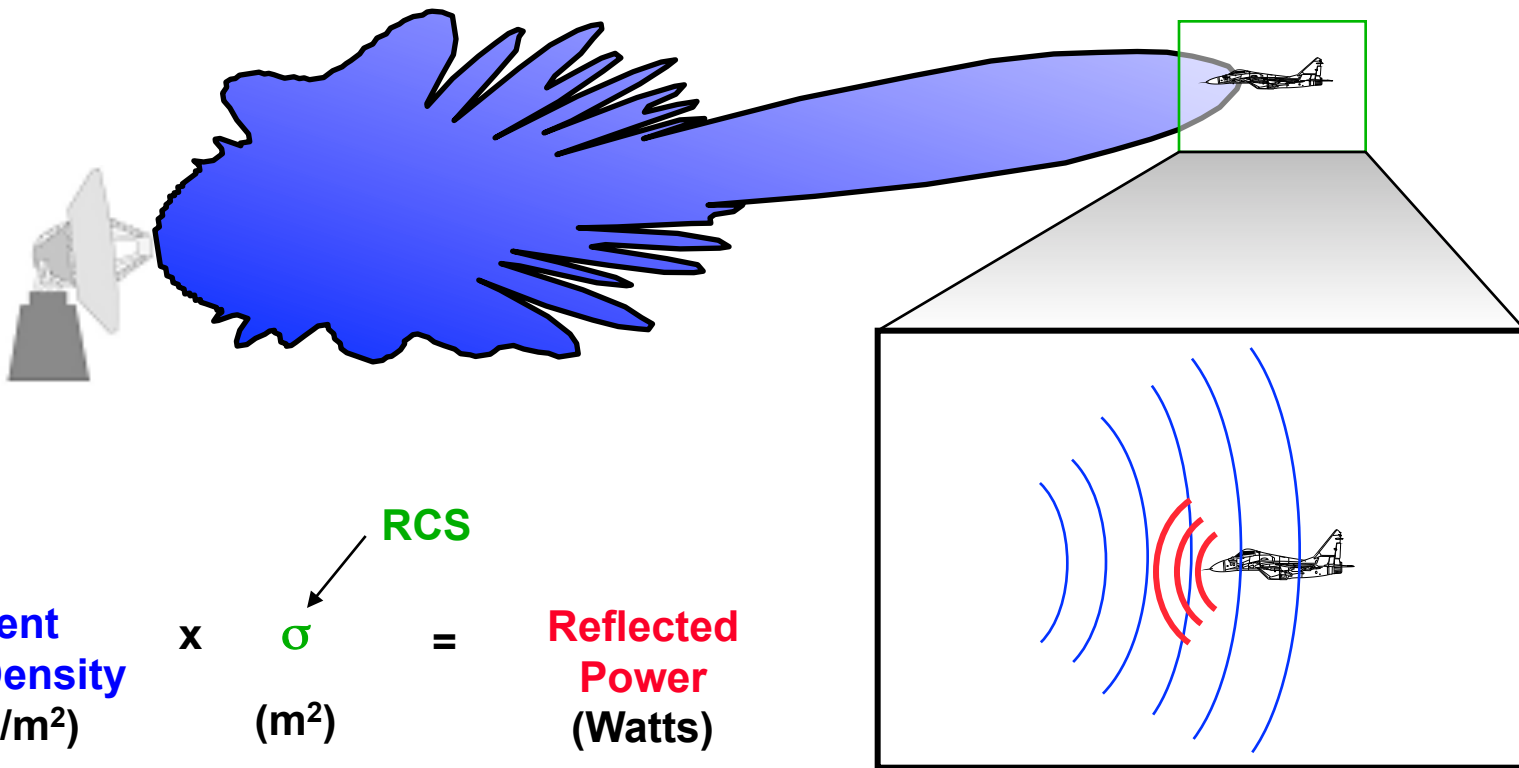
- Atmospheric attenuation
- Reflection off of earth's surface
- Over-the-horizon diffraction
- Atmospheric refraction



**Radar beams can be attenuated, reflected and bent by the environment**



# Radar Cross Section (RCS)



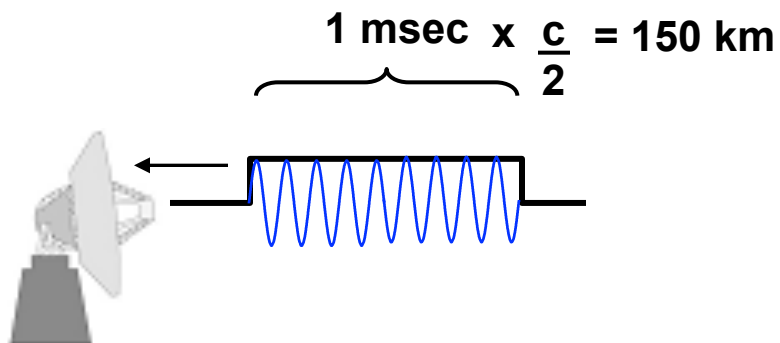
Radar Cross Section (RCS, or  $\sigma$ ) is the *effective* cross-sectional area of the target as seen by the radar

measured in m<sup>2</sup>, or dBm<sup>2</sup>

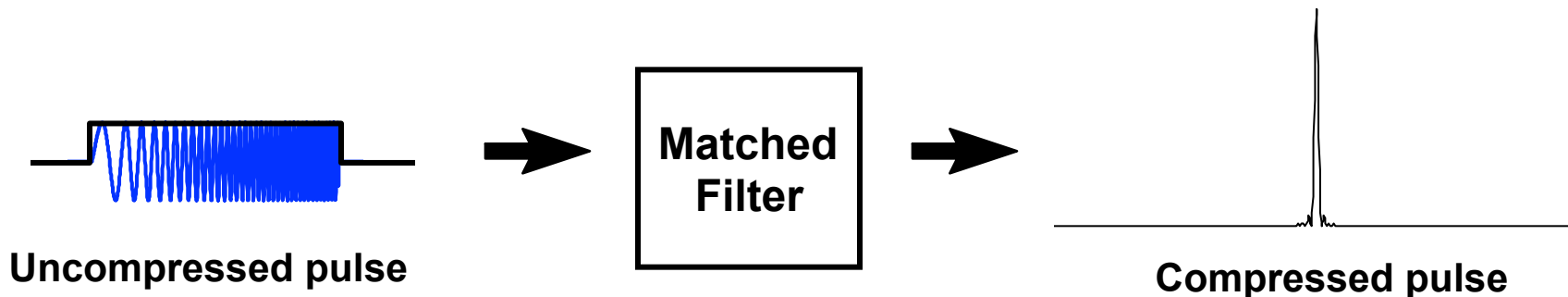


# Signal Processing Pulse Compression

**Problem:** Pulse can be very long; does not allow accurate range measurement

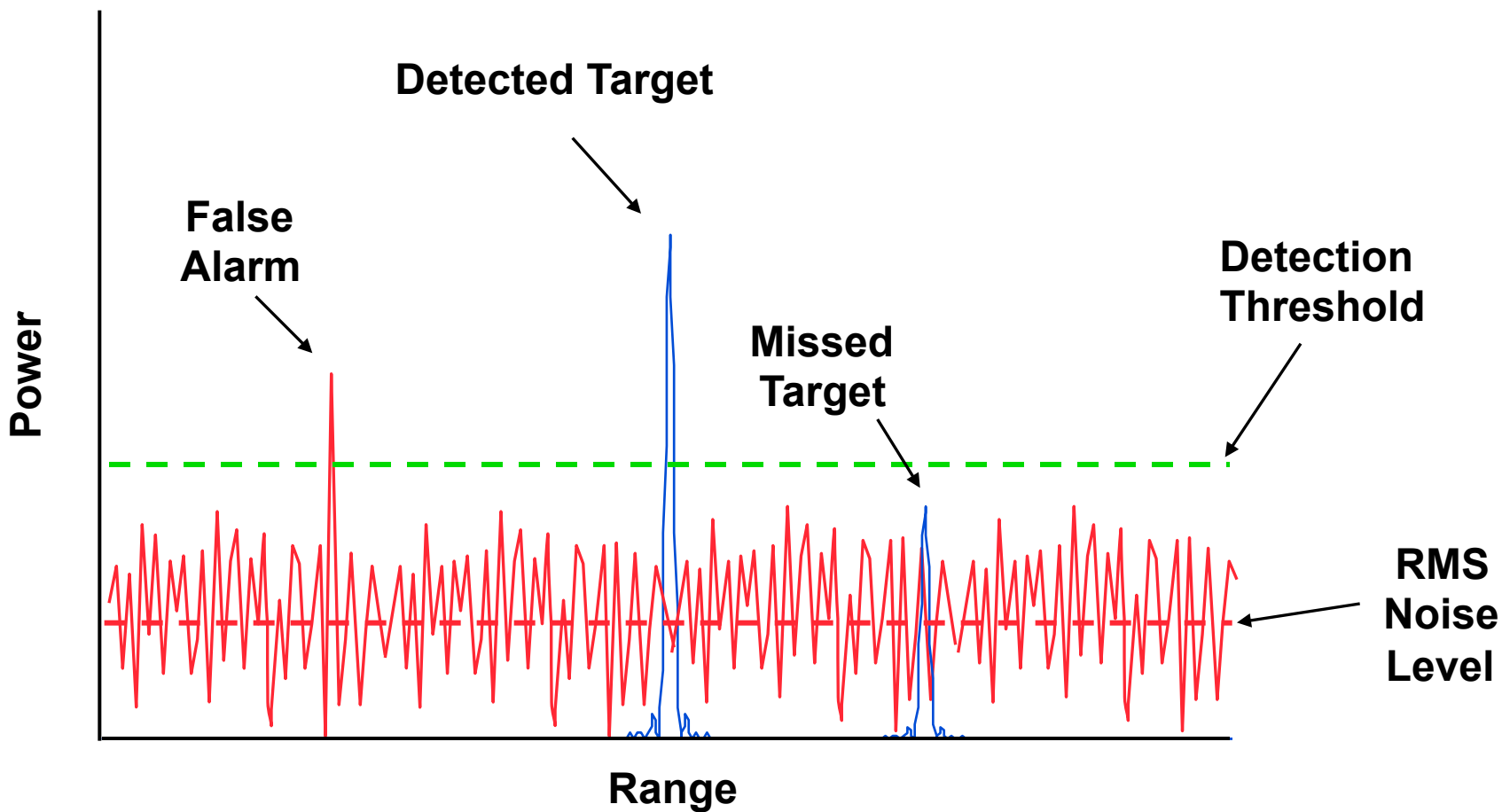


**Solution:** Use pulse with changing frequency and signal process using “matched filter”



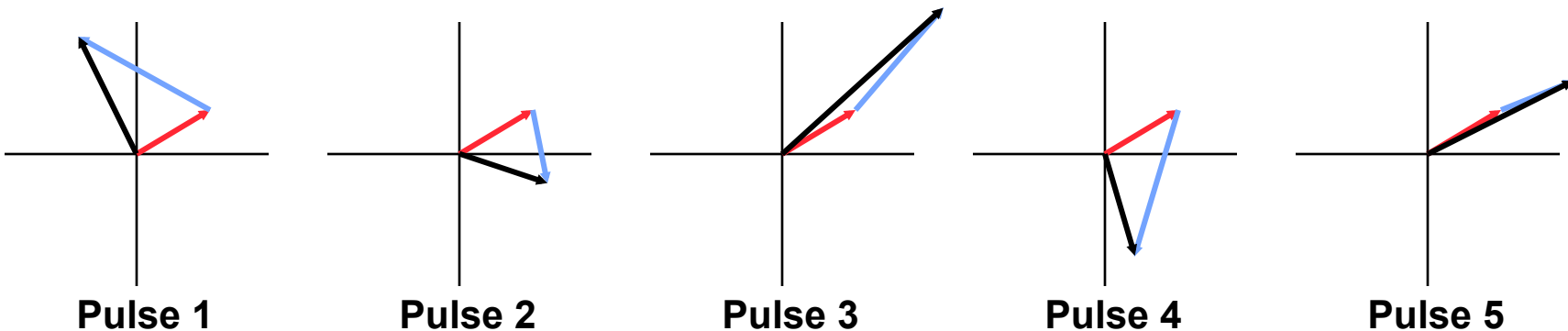


# Detection of Signals in Noise





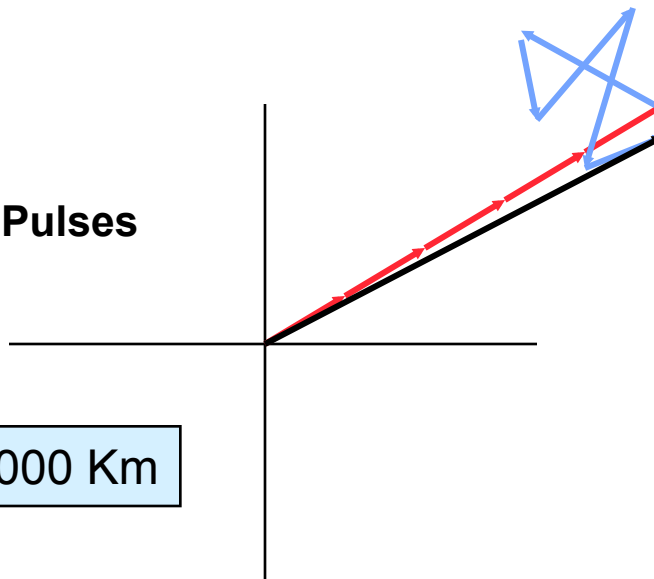
# Coherent Integration



- Coherent target returns
- Noise samples at low SNR

- Resultant signal

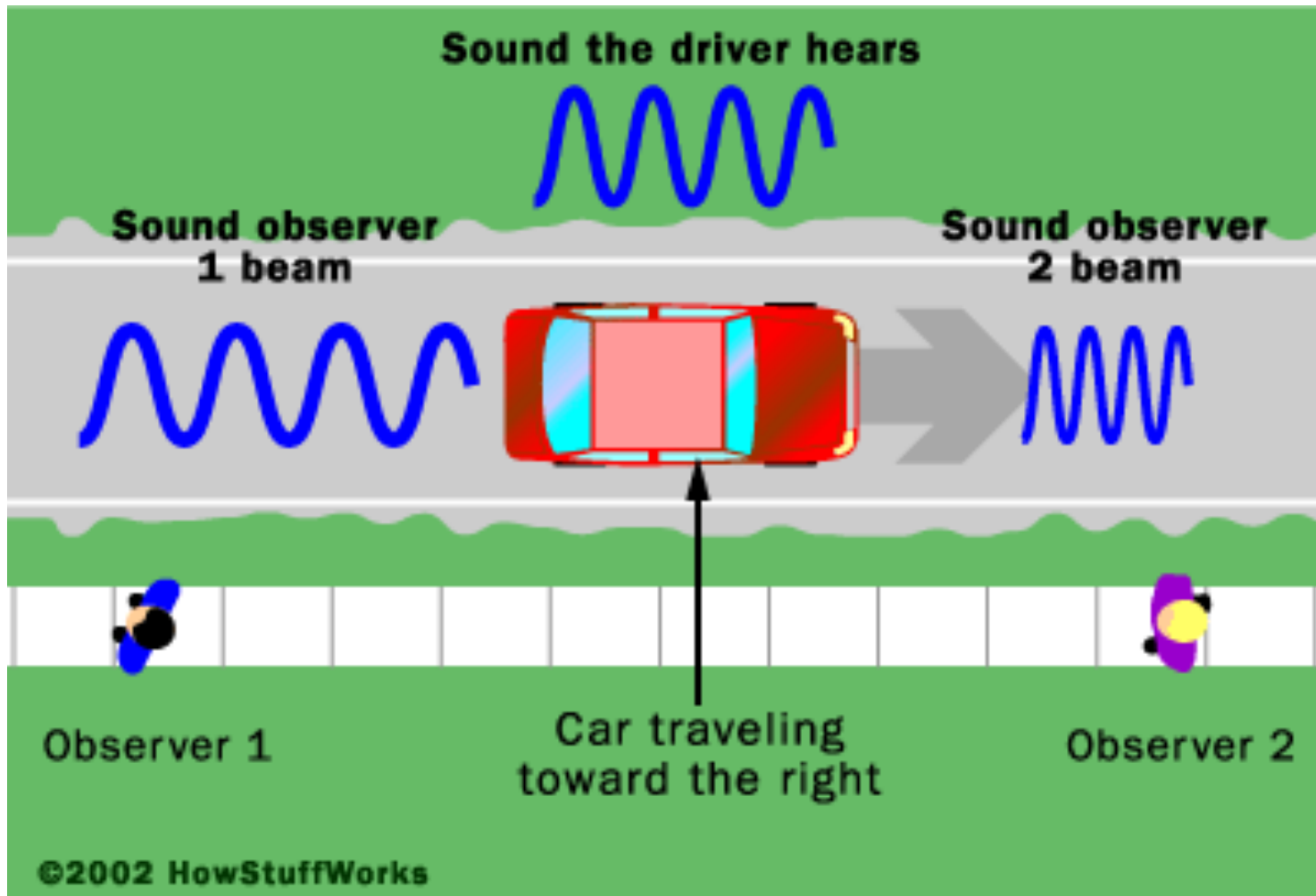
Coherently Integrated Pulses



Deep space targets at 30,000 – 40,000 Km



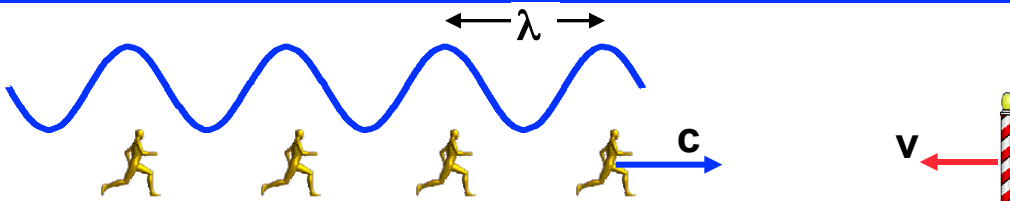
# Doppler Effect



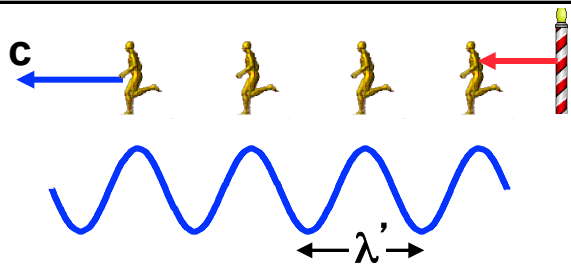
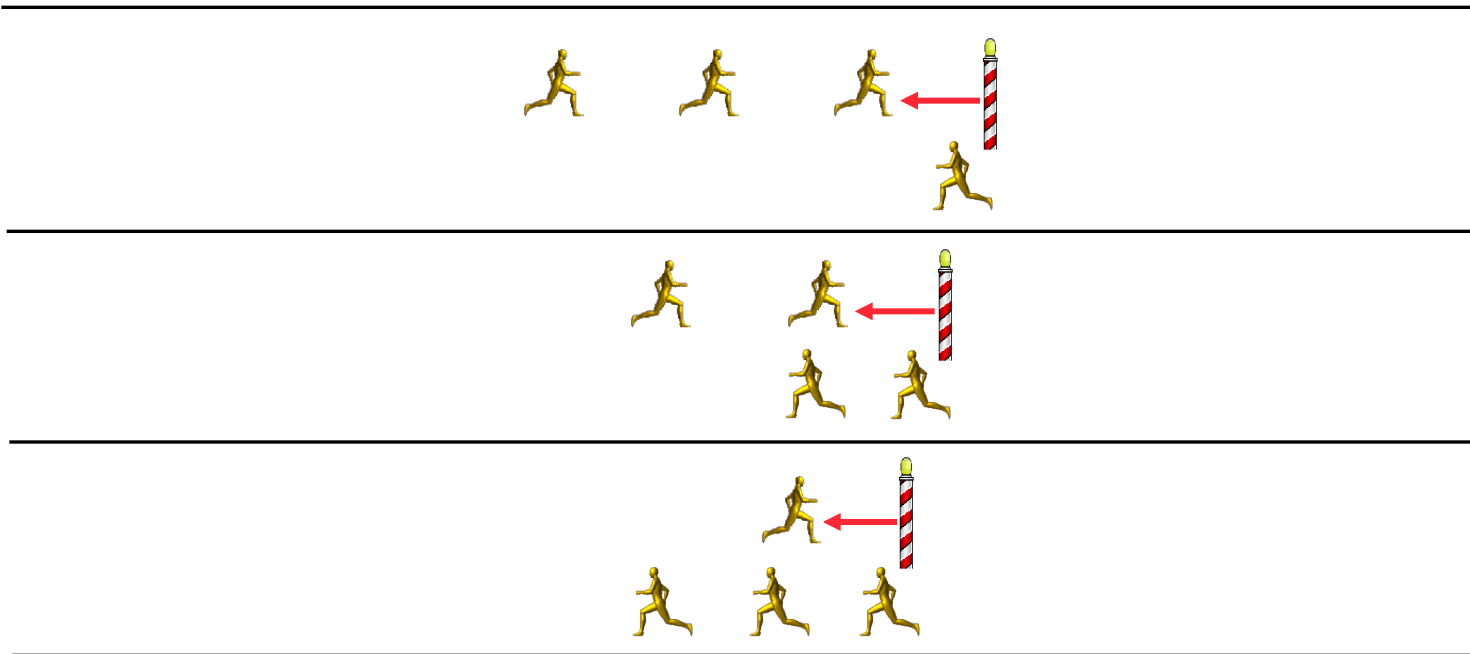


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# Doppler Shift Concept



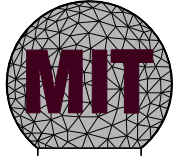
$$f = \frac{c}{\lambda}$$



$$f' = f \pm (2v/\lambda)$$

**Doppler shift**



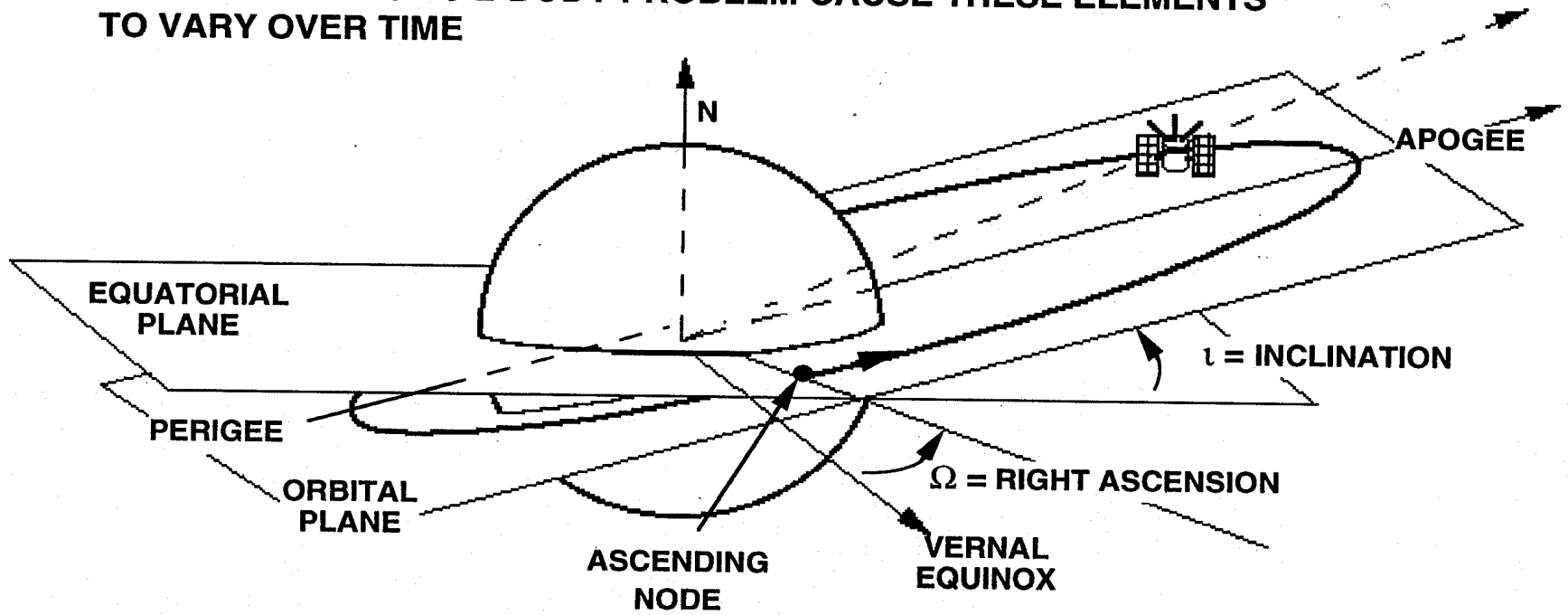


# Outline

- Introduction
  - Movie
  - QUIZ !!!
- History
- The basics
  - Radar
  - Satellite Tracking

# SATELLITE ORBITAL MECHANICS

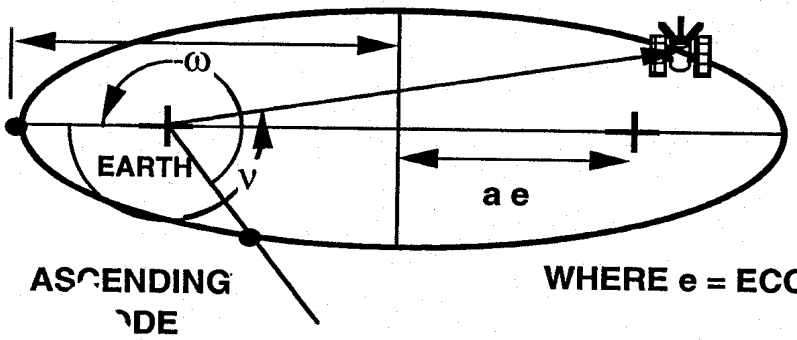
SATELLITE ORBIT DESCRIBED BY KEPLERIAN ELEMENT SET ( $t, \Omega, e, \omega, M, a, T$ )  
PERTURBATIONS TO 2-BODY PROBLEM CAUSE THESE ELEMENTS TO VARY OVER TIME



= ARGUMENT OF PERIGEE

$a$  = SEMIMAJOR AXIS

$v$  = TRUE ANOMALY

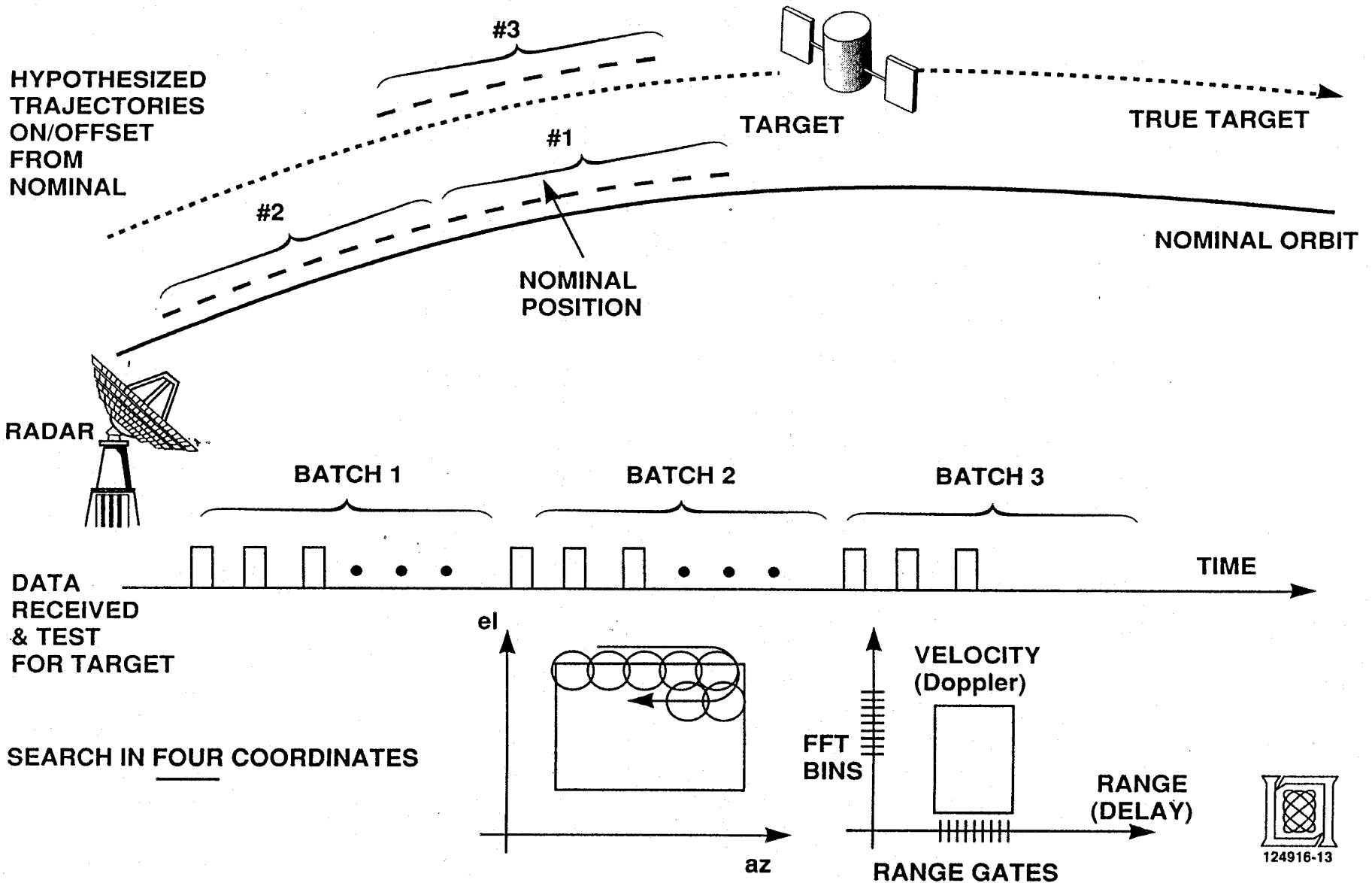


TRUE ANOMALY  $v$   
IS REPLACED BY  
MEAN ANOMALY  $M$   
 $T$  IS EPOCH

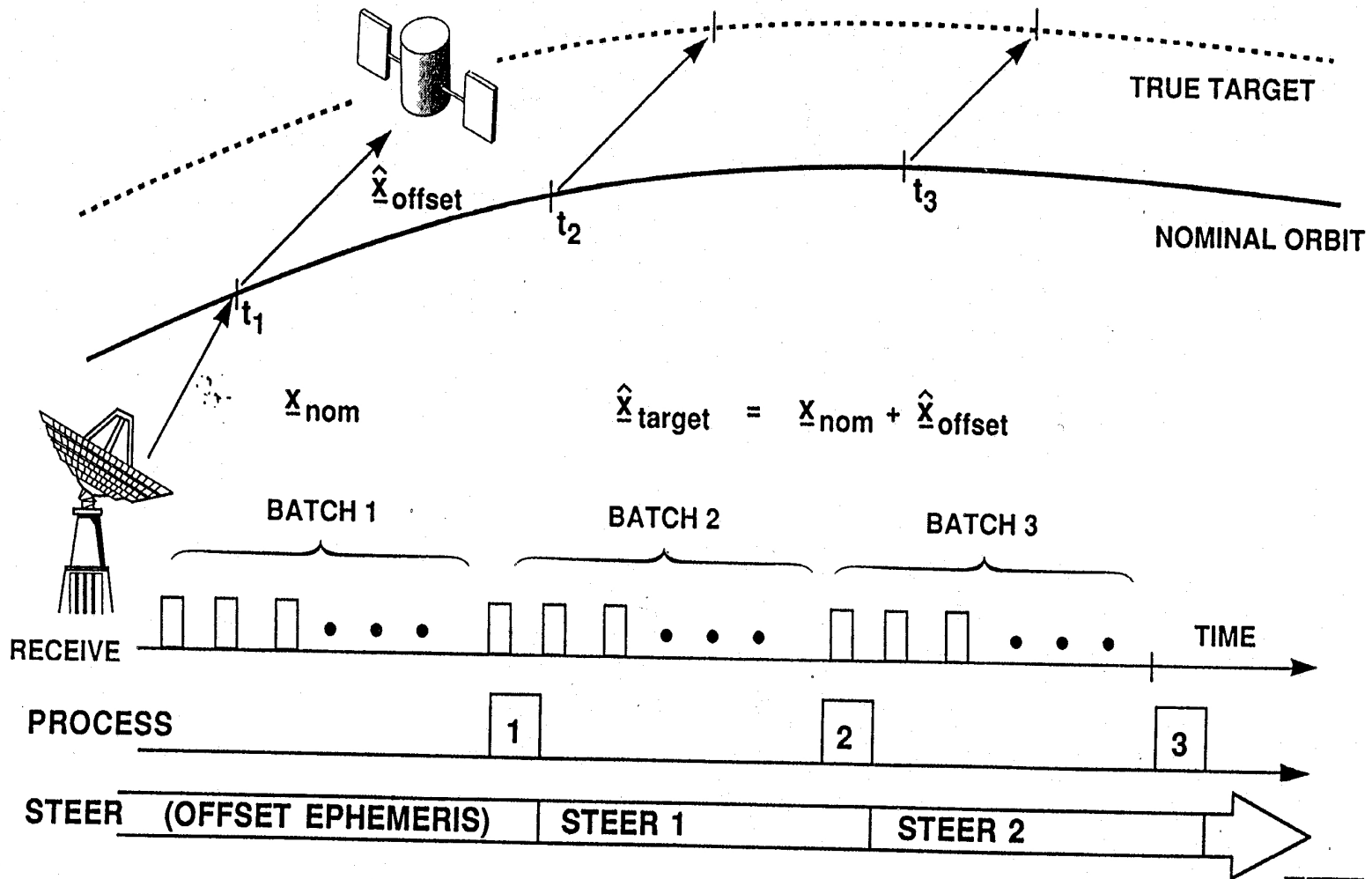
WHERE  $e$  = ECCENTRICITY

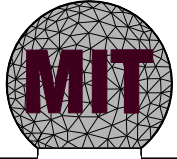
# EPHEMERIS-GUIDED SEARCH

14



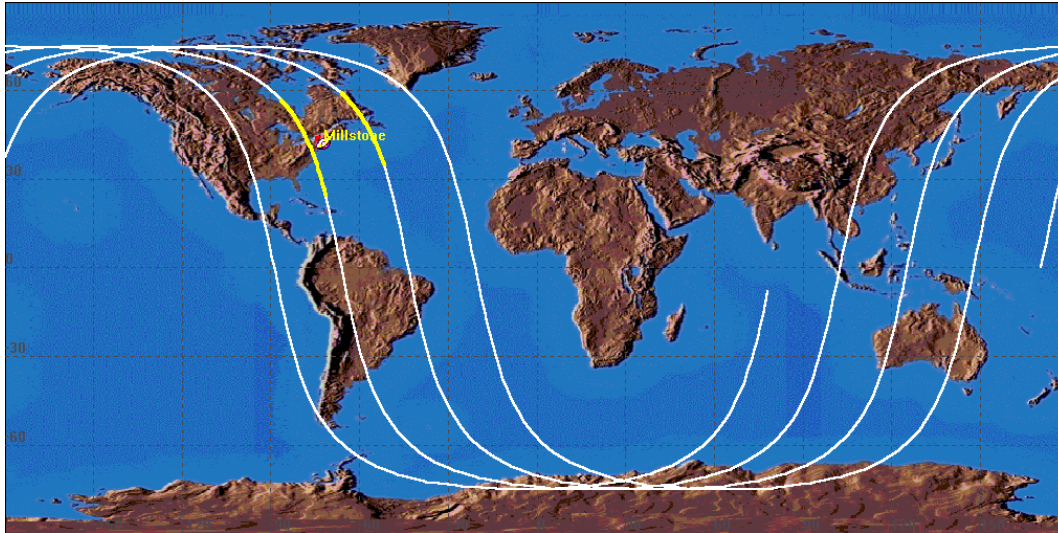
# EPHEMERIS-GUIDED TRACK





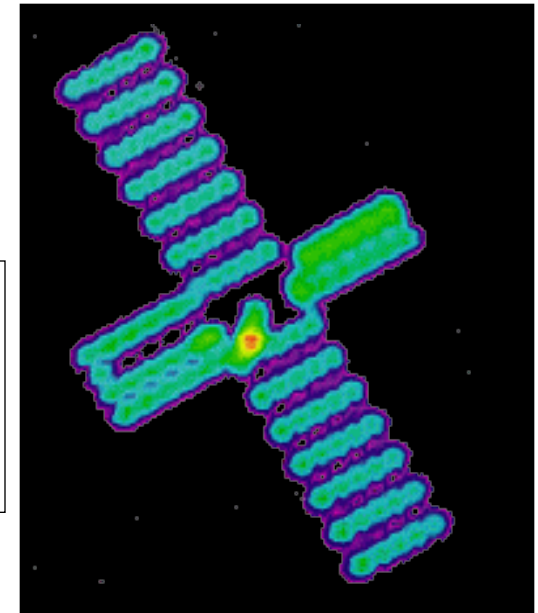
# Space Surveillance Data Products

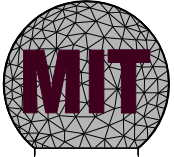
HAYSTACK OBSERVATORY



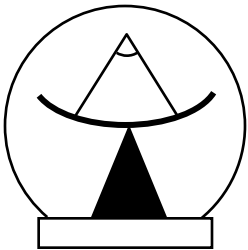
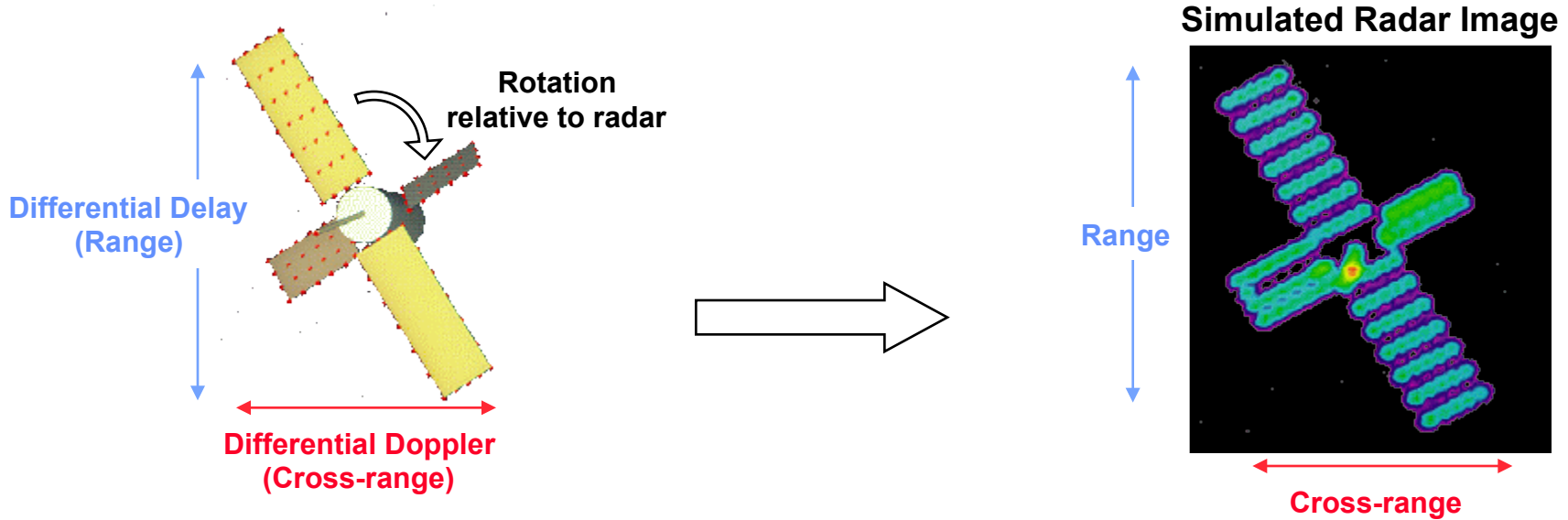
- Where is it?
  - Metric data gives orbital position

- What is it?
  - Image analysis gives size and shape
- What is it doing?
  - Motion analysis gives attitude





# Radar Imaging of Spacecraft



## Characteristics:

- Available on-demand
- all weather
- day and night
- Resolution independent of range

## Benefits:

- Shape / Size Estimate
- Operational Mode Determination
- Launch/Status Monitoring
- Damage Assessment
- Motion Determination