

# Introduction to Incoherent Scatter 1

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Norwegian Space Center/  
SRI International

# Incoherent Scatter Radar

- Incoherent
- Scatter
- Radar

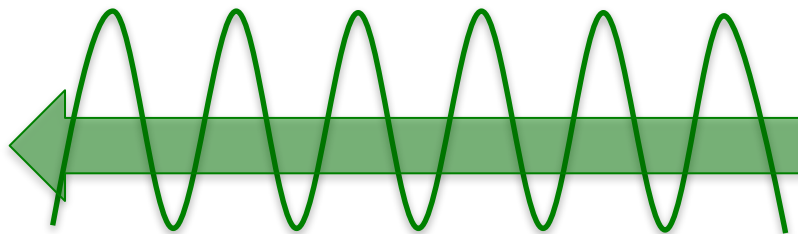
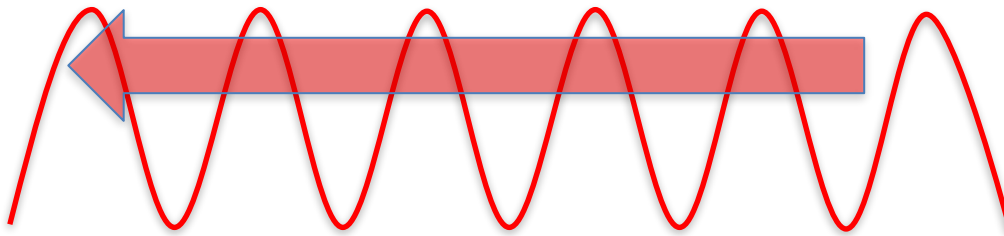
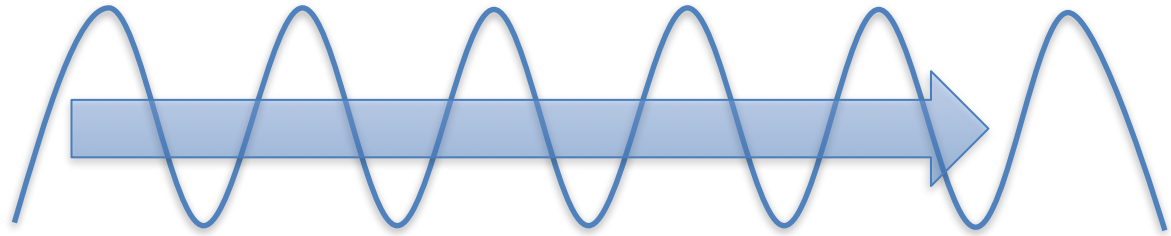
# Incoherent Scatter Radar

- Radar
- Scatter
- Incoherent

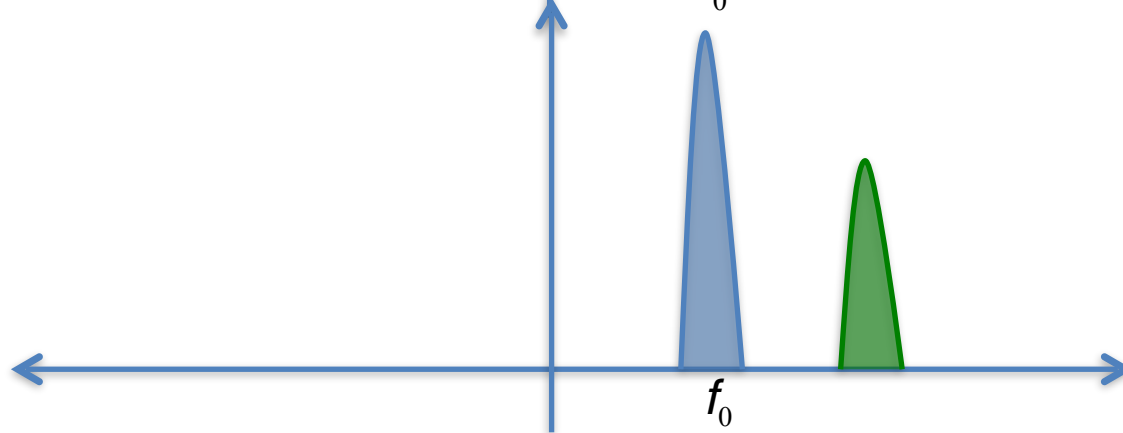
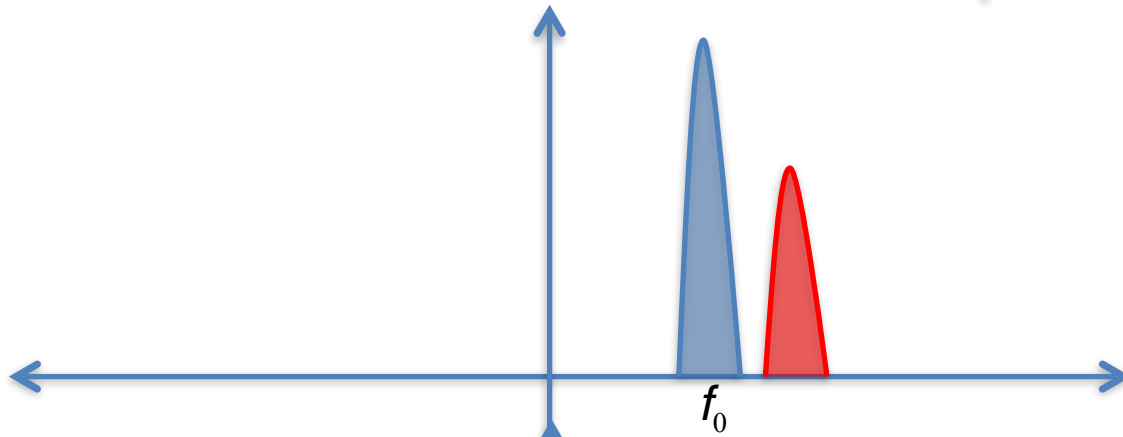
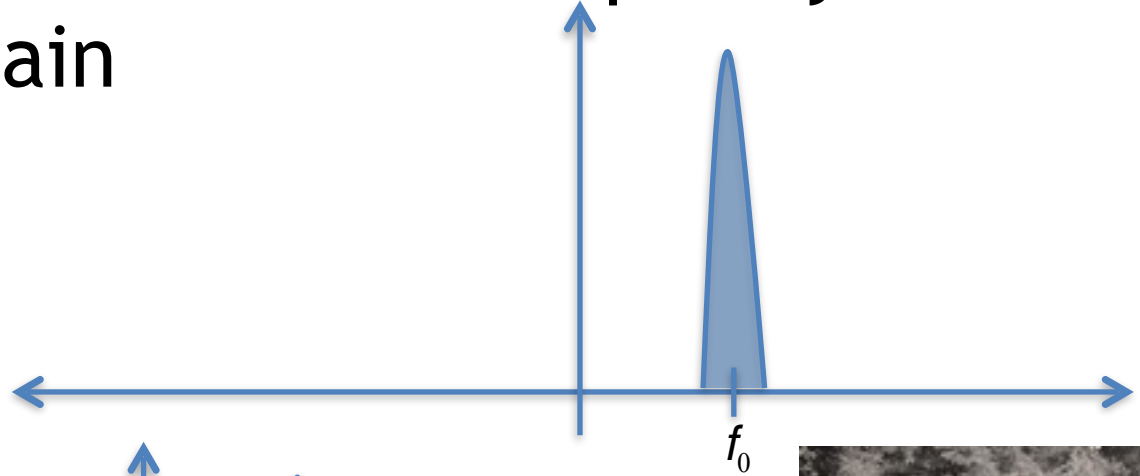
# Radar

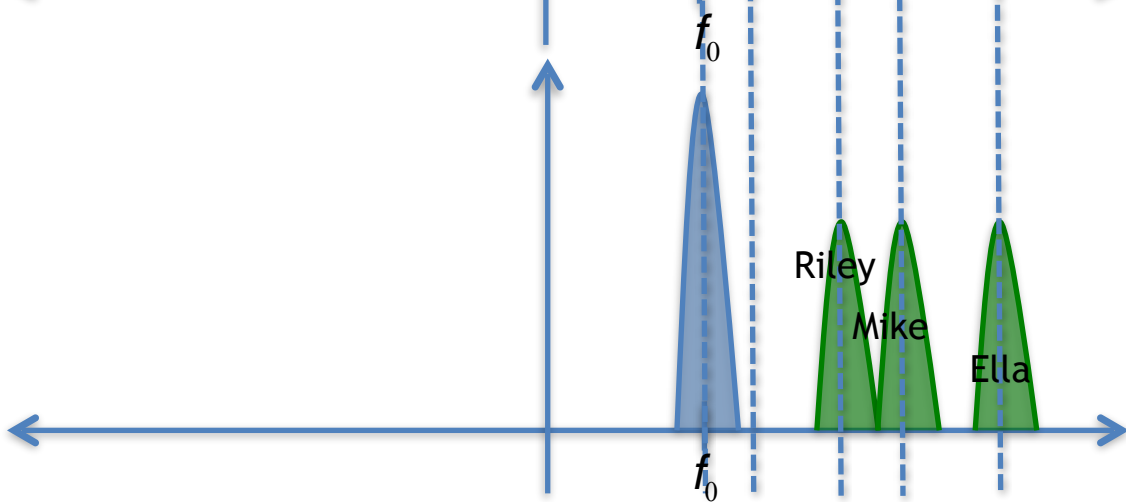
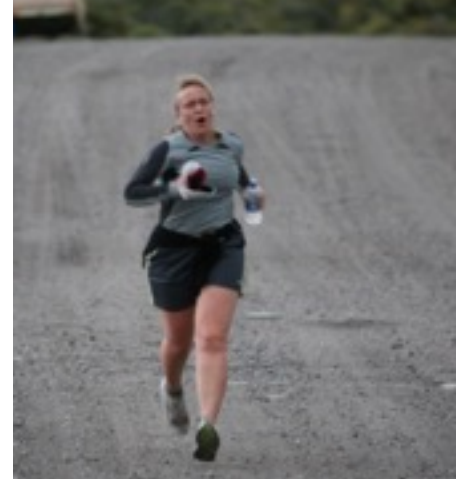
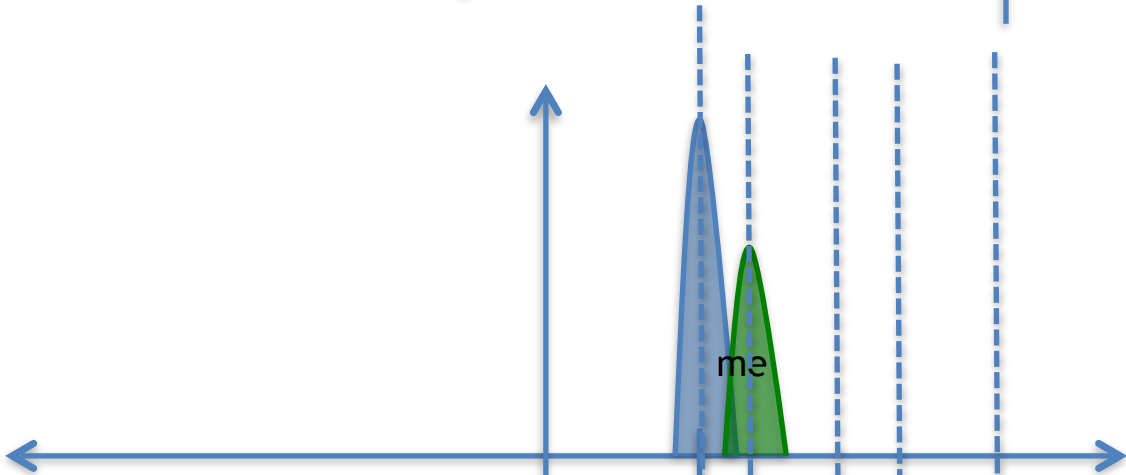
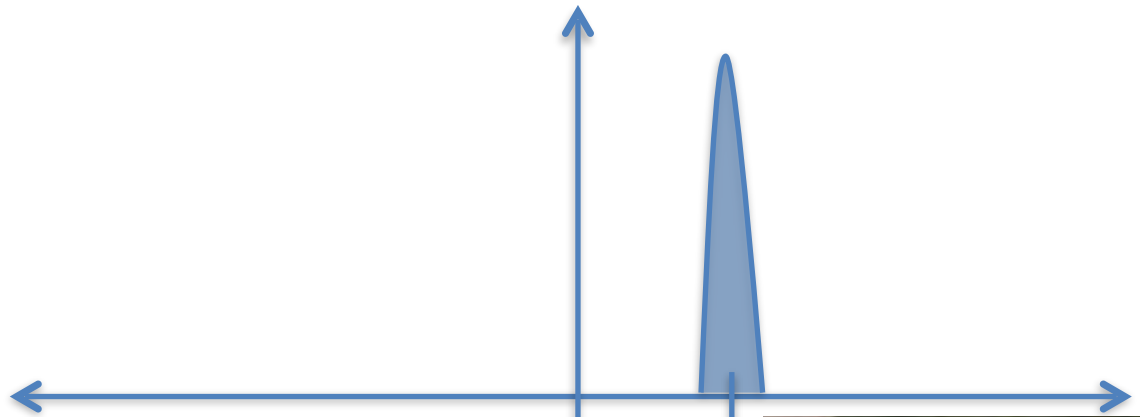
- RADAR (RADio Detection And Ranging)
  - is a technique for detecting and studying remote targets by transmitting a radio wave in the direction of the target and observing the reflection of the wave.
  - Radar is an object detection system which uses radio waves to determine the range, altitude, direction, or speed of objects.  
(wikipedia)

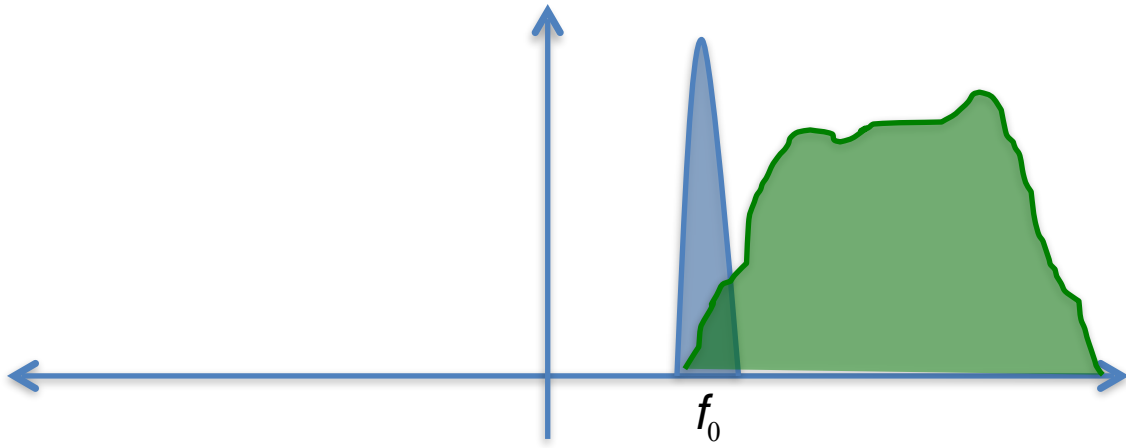
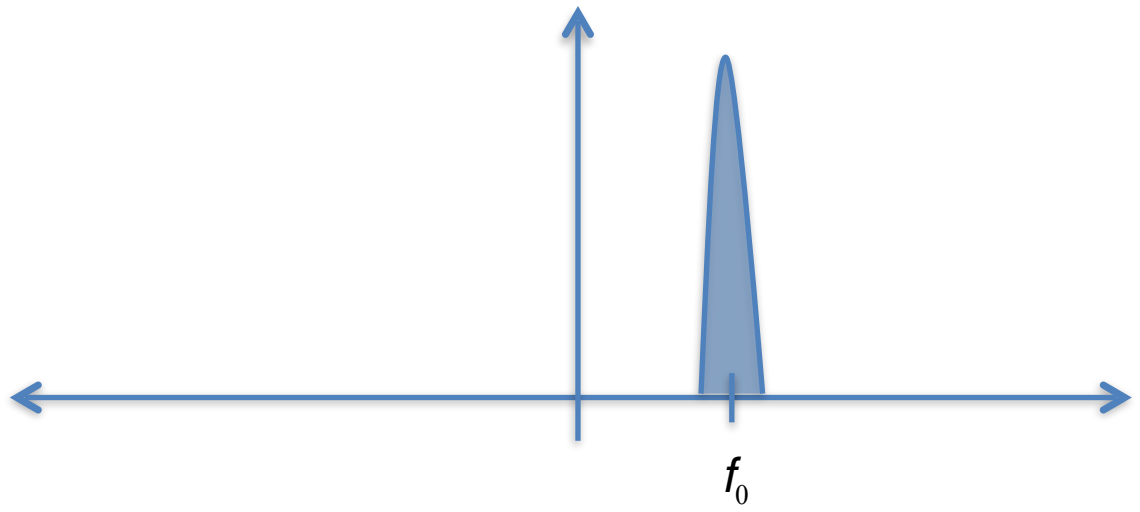
# Doppler Radar - time domain



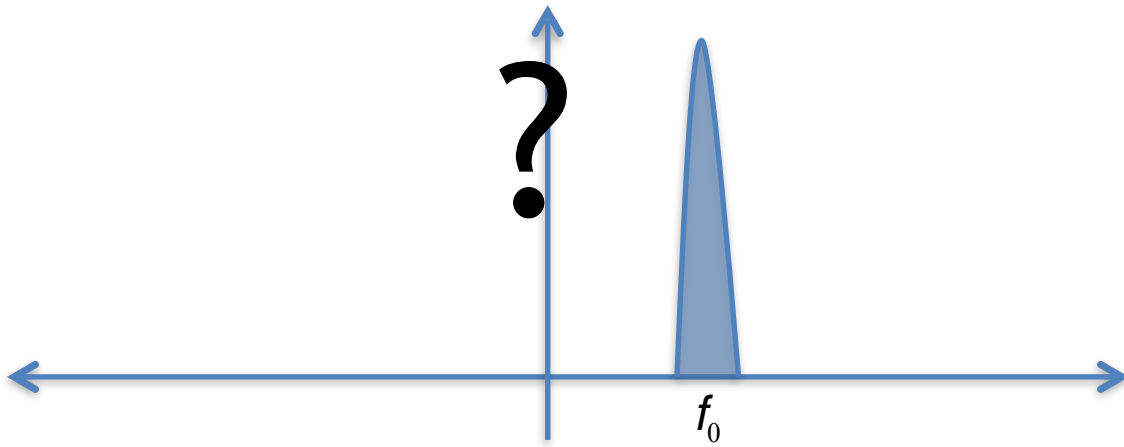
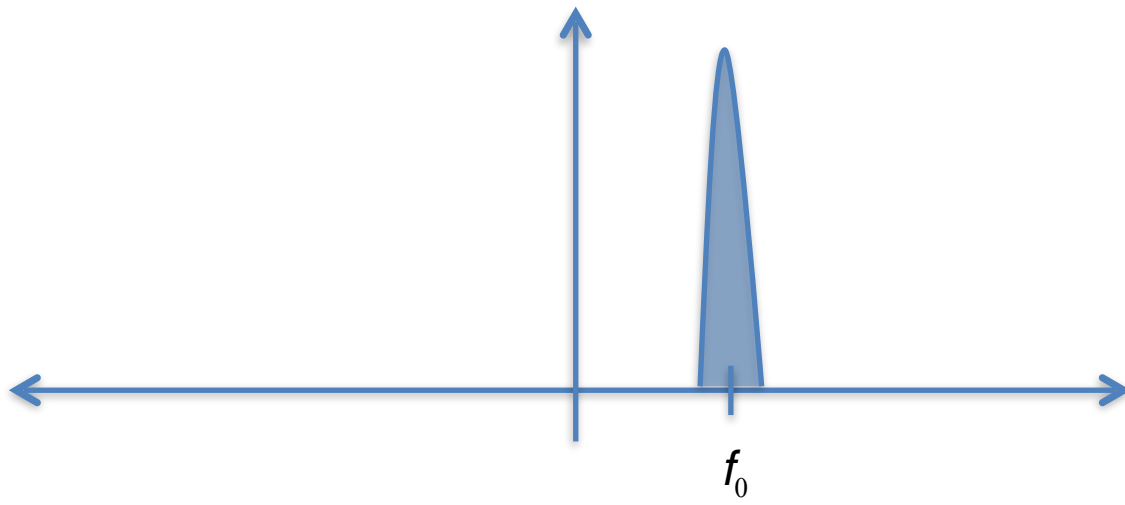
# Doppler Radar - frequency domain

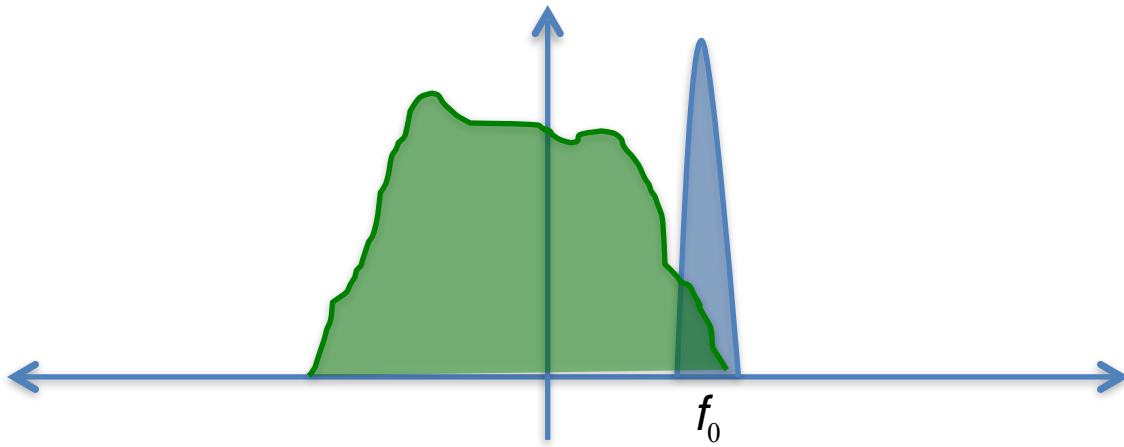
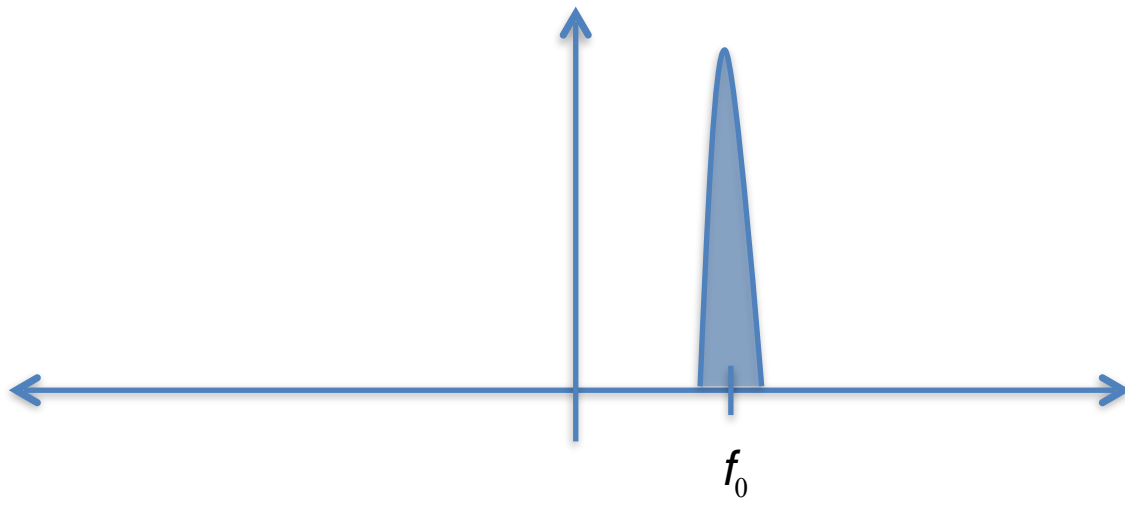










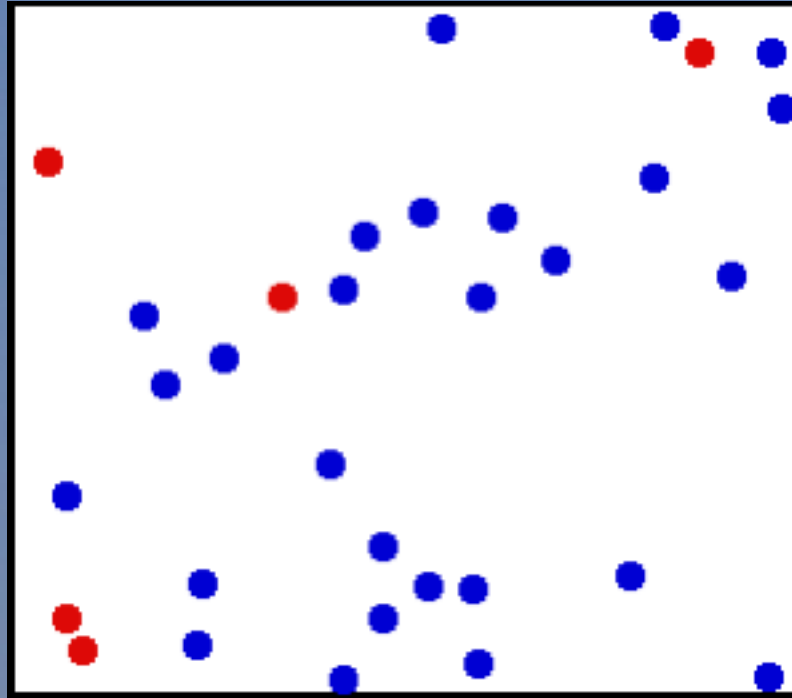


# Thomson scattering

- Thomson scattering is the elastic scattering of electromagnetic radiation by a free charged particle, as described by classical electromagnetism.
- In the low-energy limit, the electric field of the incident wave (radar wave) accelerates the charged particle, causing it, in turn, to emit radiation at the same frequency as the incident wave, and thus the wave is scattered.
- As long as the motion of the particle is non-relativistic (i.e. its speed is much less than the speed of light), the main cause of the acceleration of the particle will be due to the electric field component of the incident wave, and the magnetic field can be neglected. The particle will move in the direction of the oscillating electric field, resulting in electromagnetic dipole radiation.



# Thermal fluctuating electrons



# Radar Equations

Hard target:

$$P_r = \frac{P_t G_t A_r \sigma}{(4\pi)^2 R^4}$$

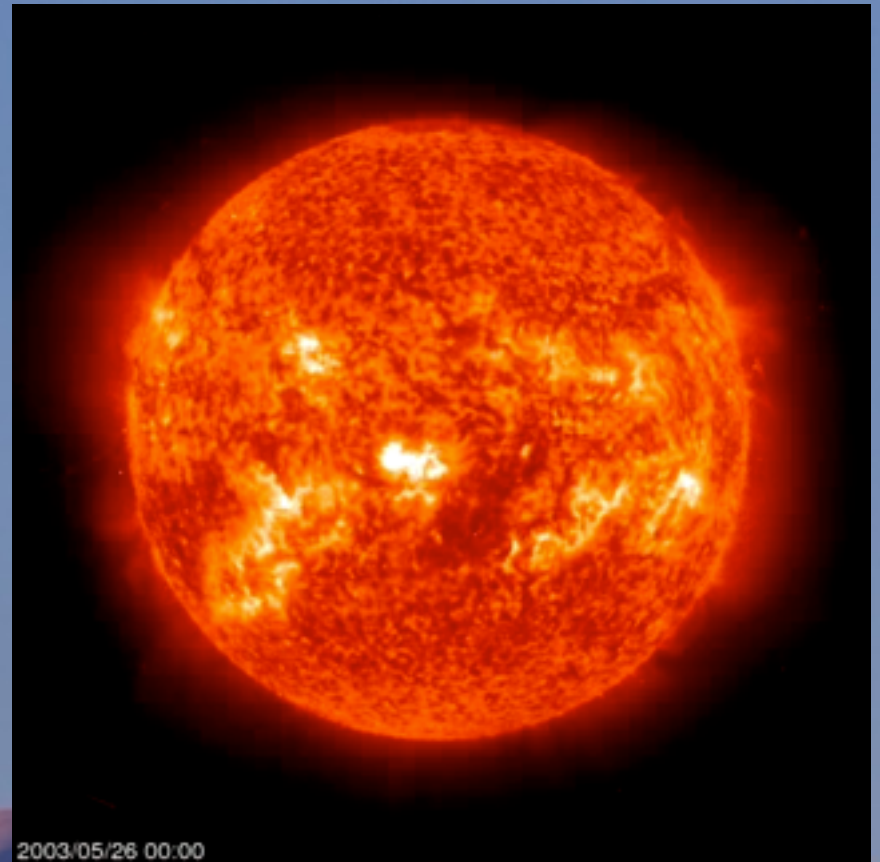
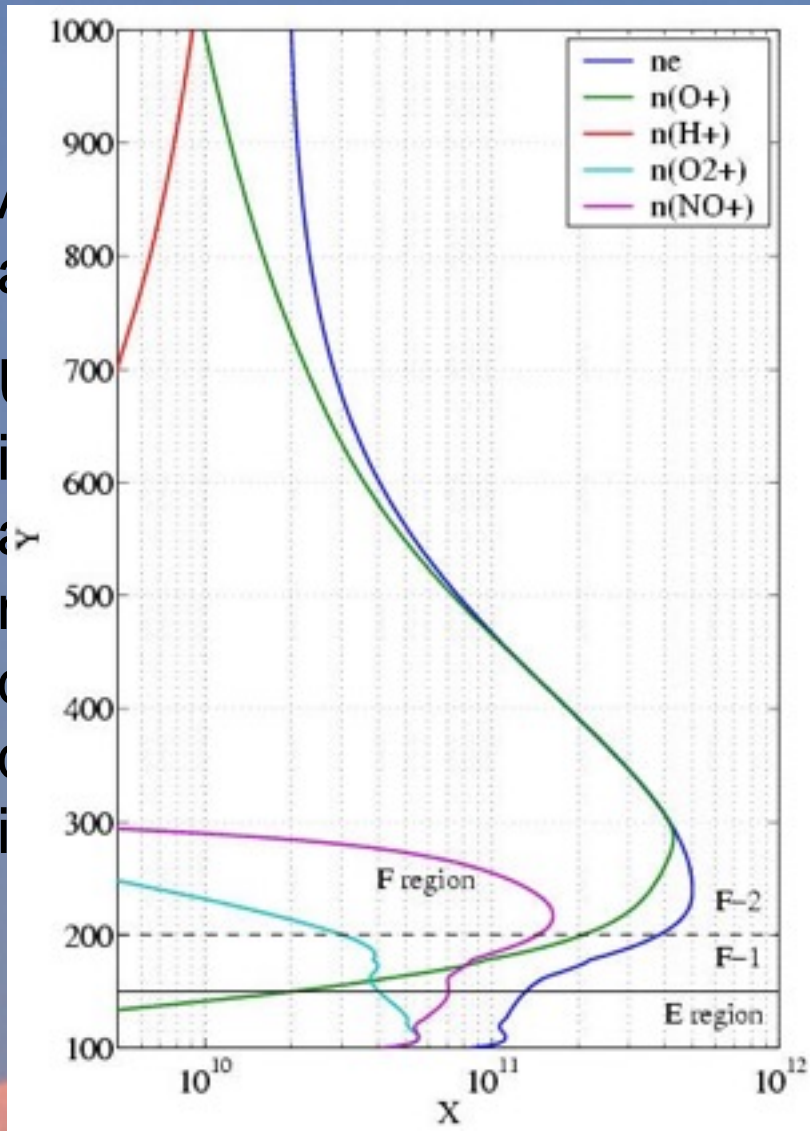
Incoherent Scatter Radar

$$P_r = \frac{C c_0 G \lambda^2}{2(4\pi)^2} \frac{P_t \tau_p}{R^2} \frac{\sigma_e n_e(R)}{(1 + k^2 \lambda_D^2)(1 + k^2 \lambda_D^2 + T_r)}$$

# The ionospheric plasma

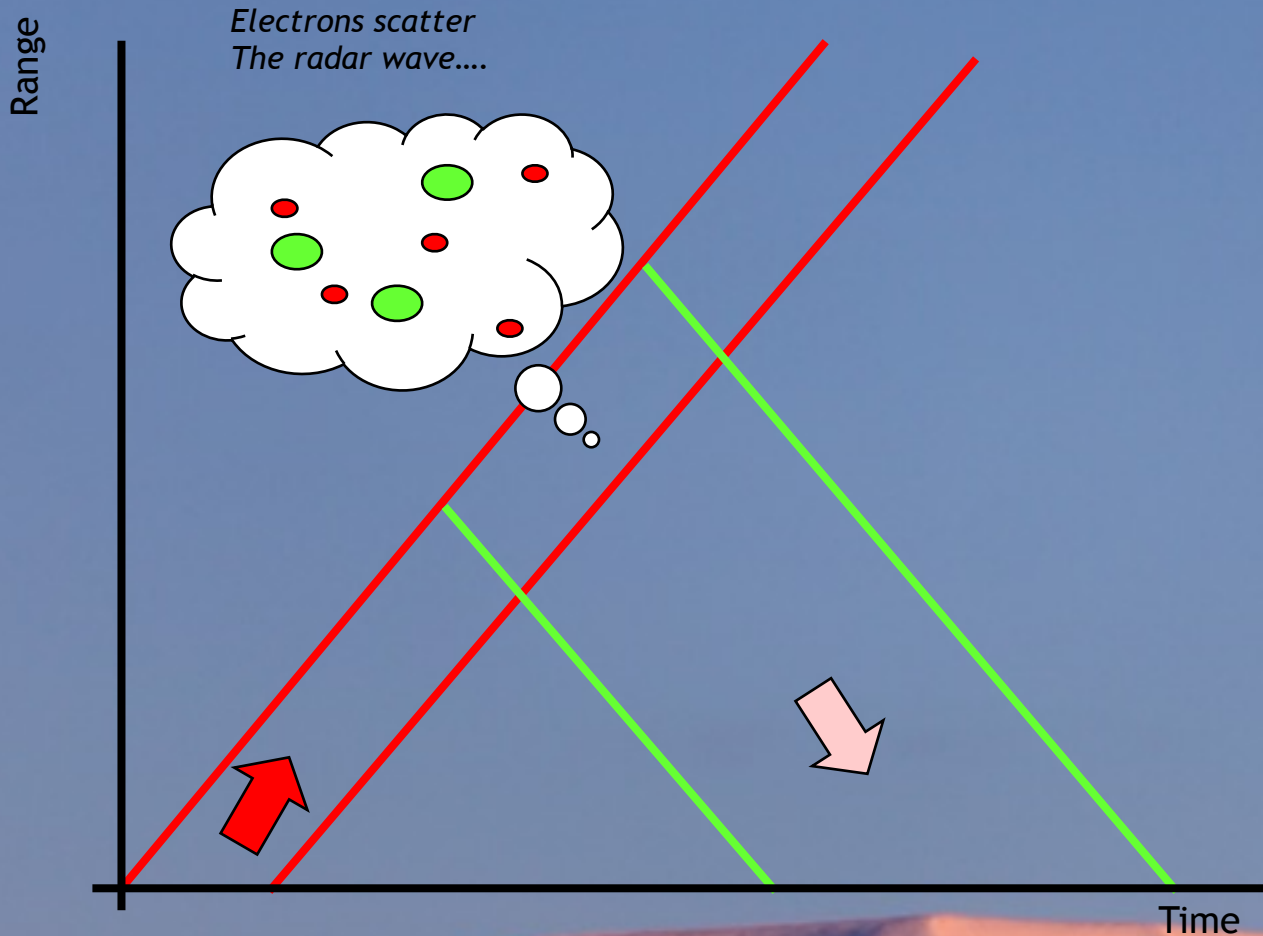
- So now we need electrons in the ionosphere to scatter the radar wave off...

# ...what Anita said this morning...





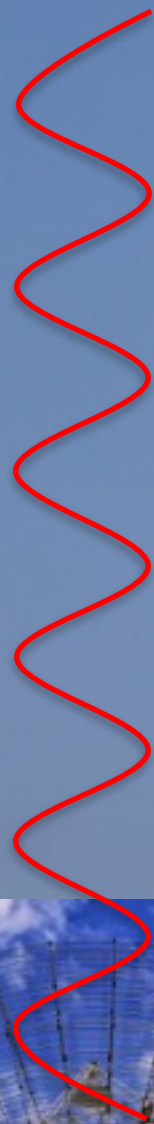
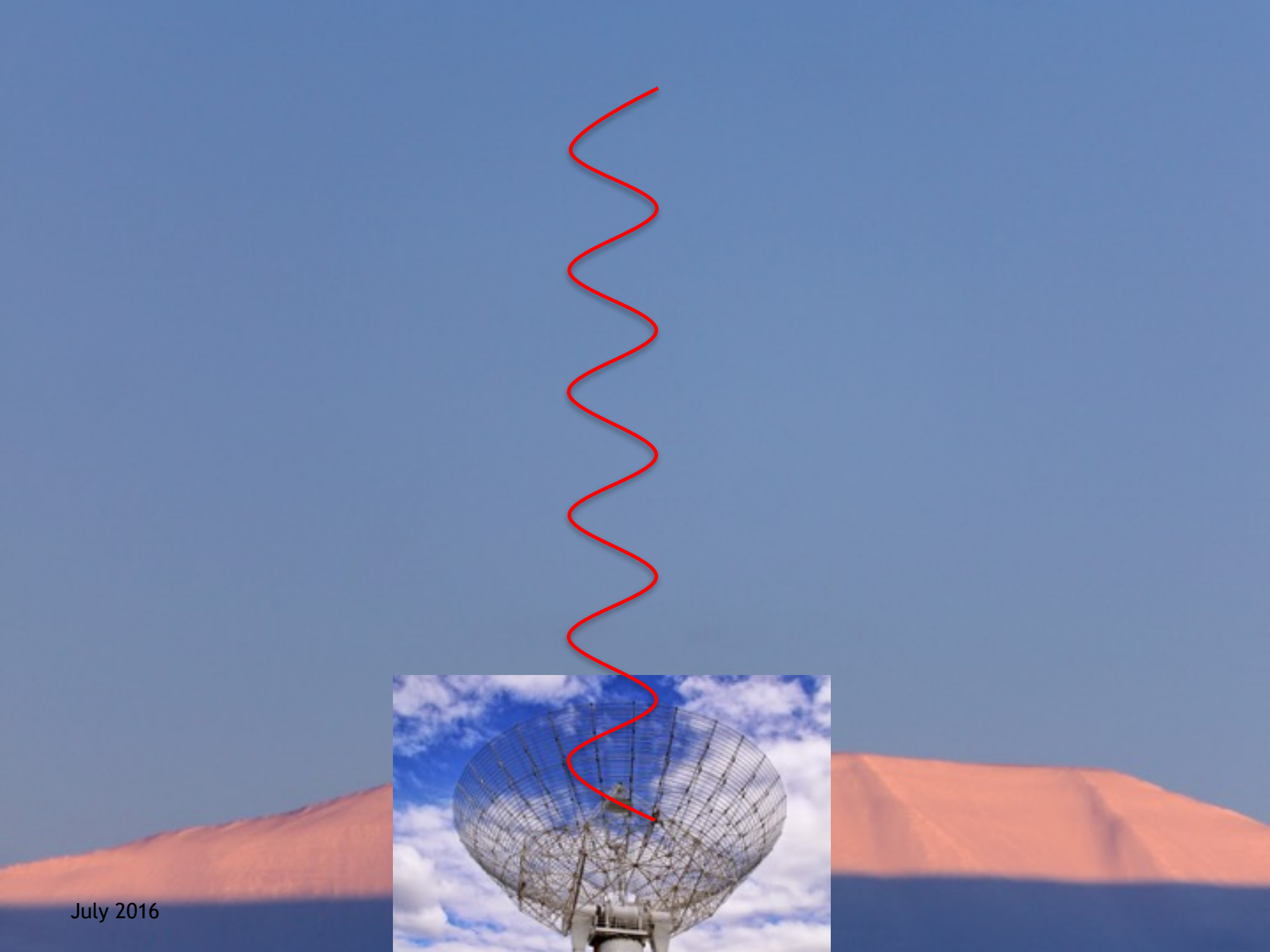
# How ISRs work...



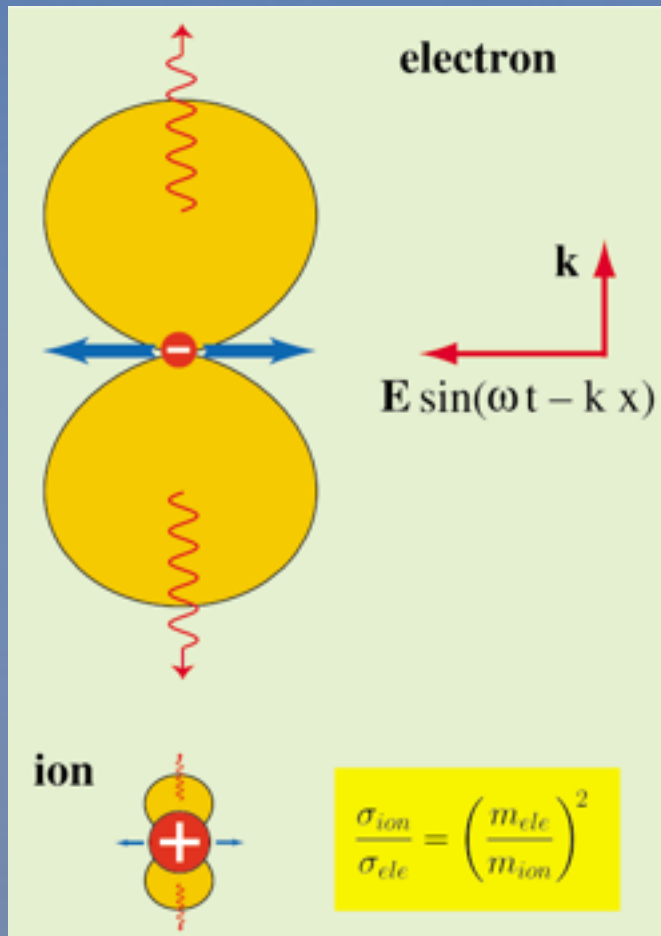
High power transmitter

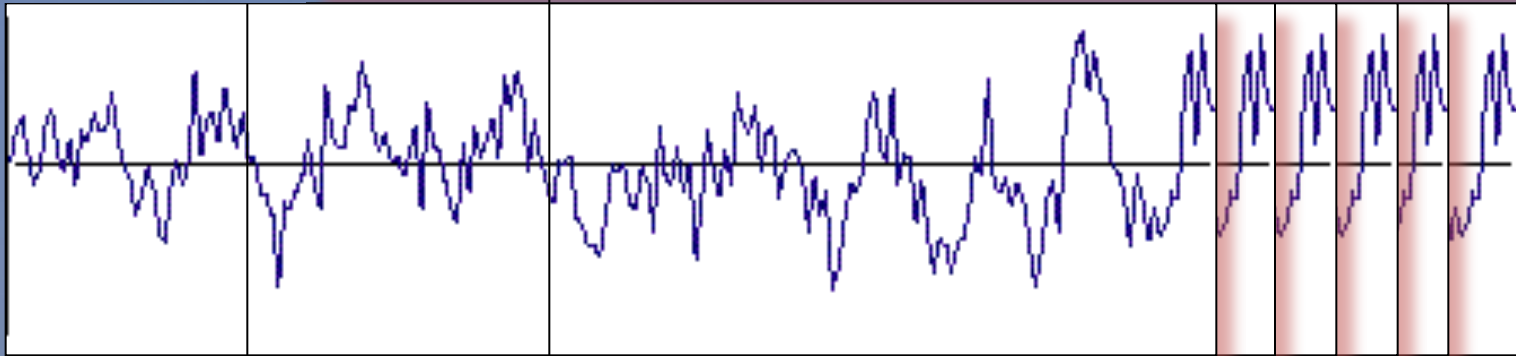
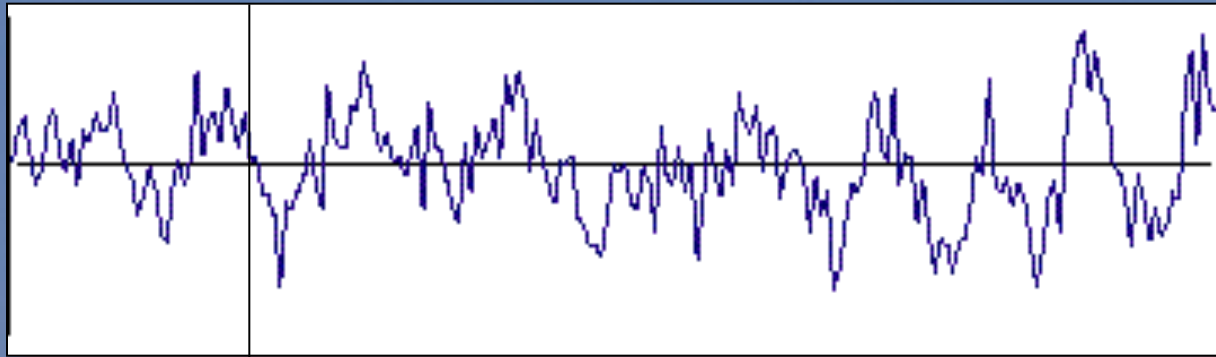
Very sensitive receiver

Only  $\sim 0.00000000000000000001\%$  of the transmitted power is returned!



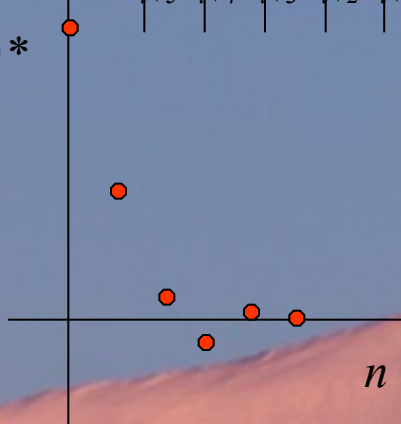
July 2016





$i+5$   $i+4$   $i+3$   $i+2$   $i+1$   $i$

$$\sum i.(i+n)^*$$

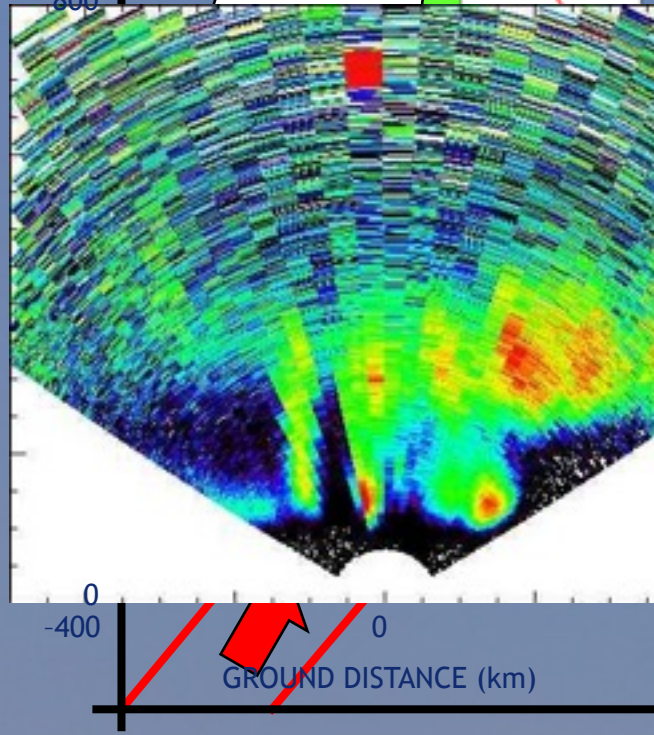


Fourier Transform

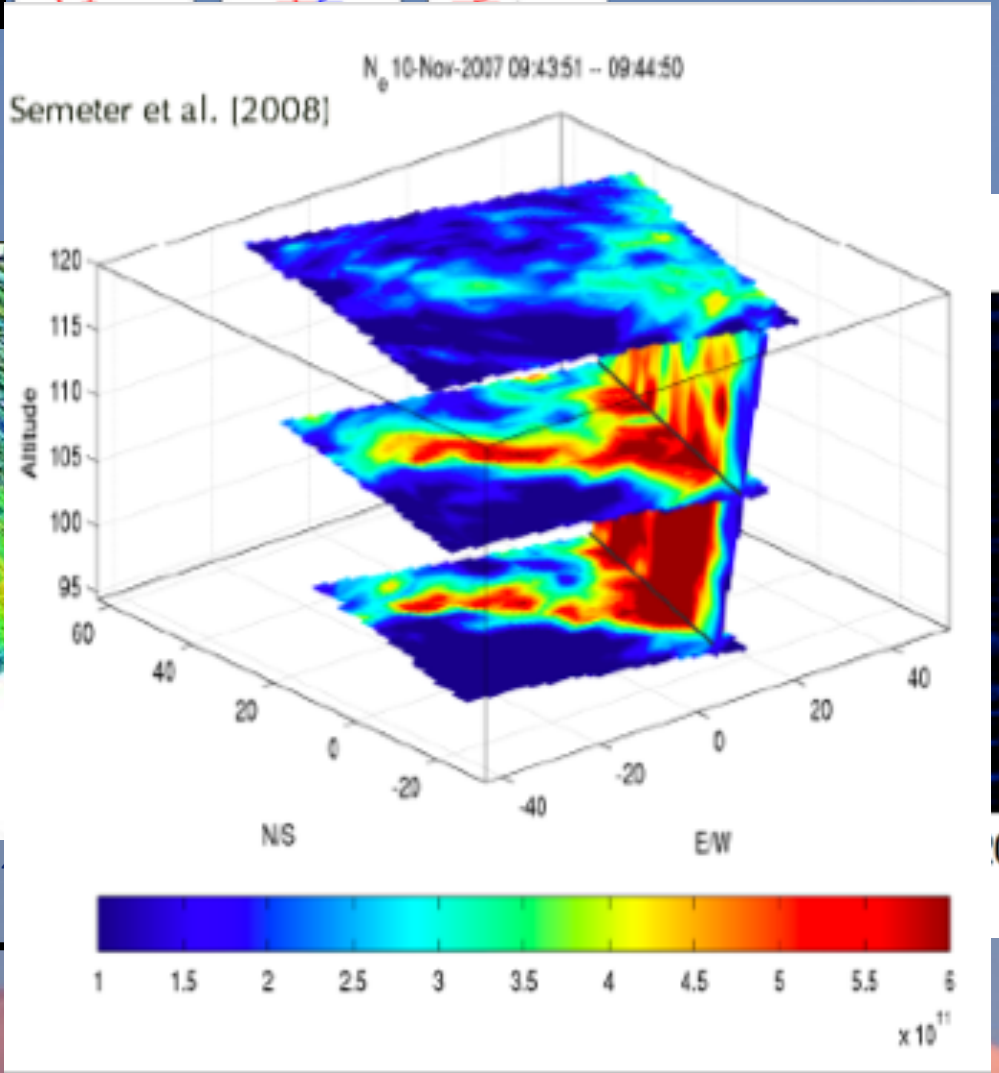
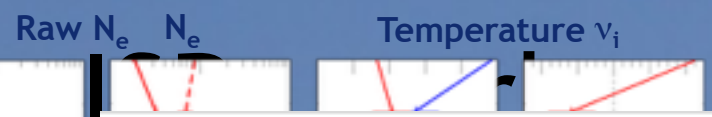


ALTITUDE (km)

Range



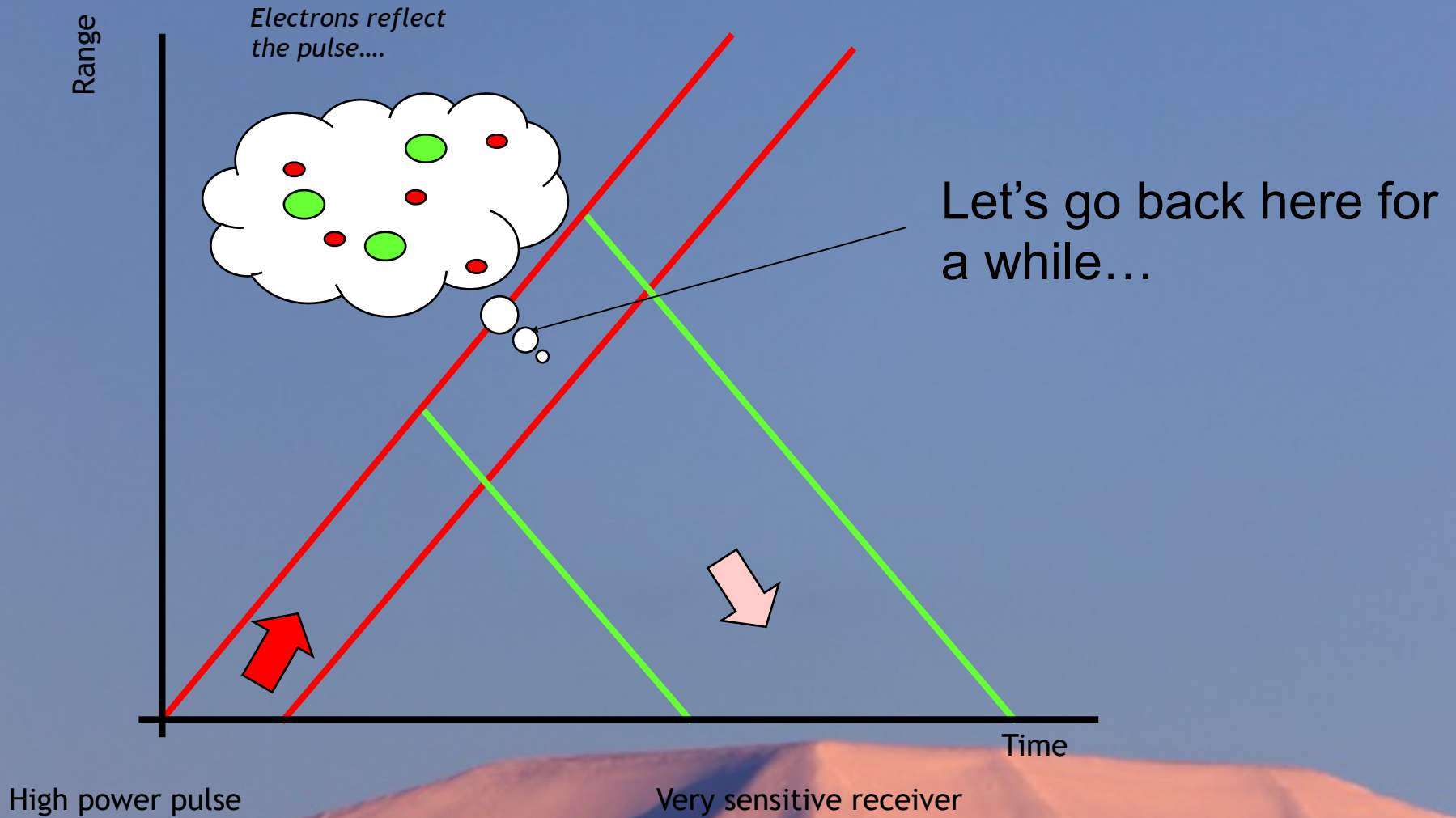
High power pulse



Only ~0.00000000000000000001% of the transmitted power is returned!

With incoherent Scatter Radars we can determine statistical properties of the charged particle distributions

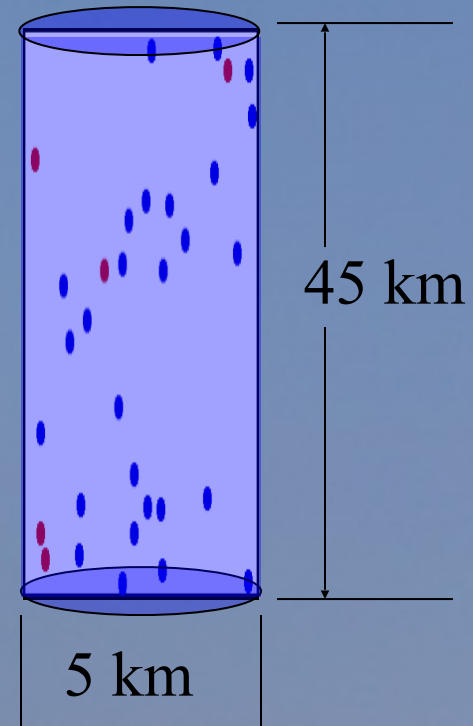
# How ISRs work...



# Total cross section estimate:

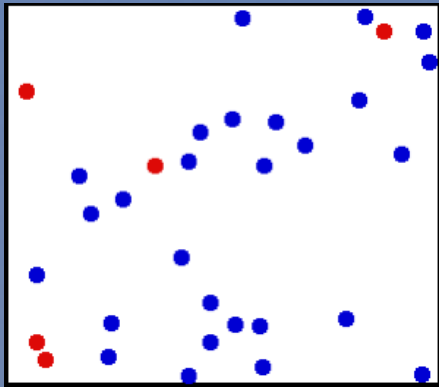
Consider an antenna with a 1-degree beam measuring the ionospheric plasma at 300 km range and using a 300 microsecond pulse.

If the electron density is  $10^{12} \text{ m}^{-3}$ , the total number of electrons scattering into a given measurement is  $\sim 8.8 \times 10^{23}$ . This yields a total cross-section of  $88 \text{ mm}^2$  – we need a big radar!





# For TRUE incoherent scatter...



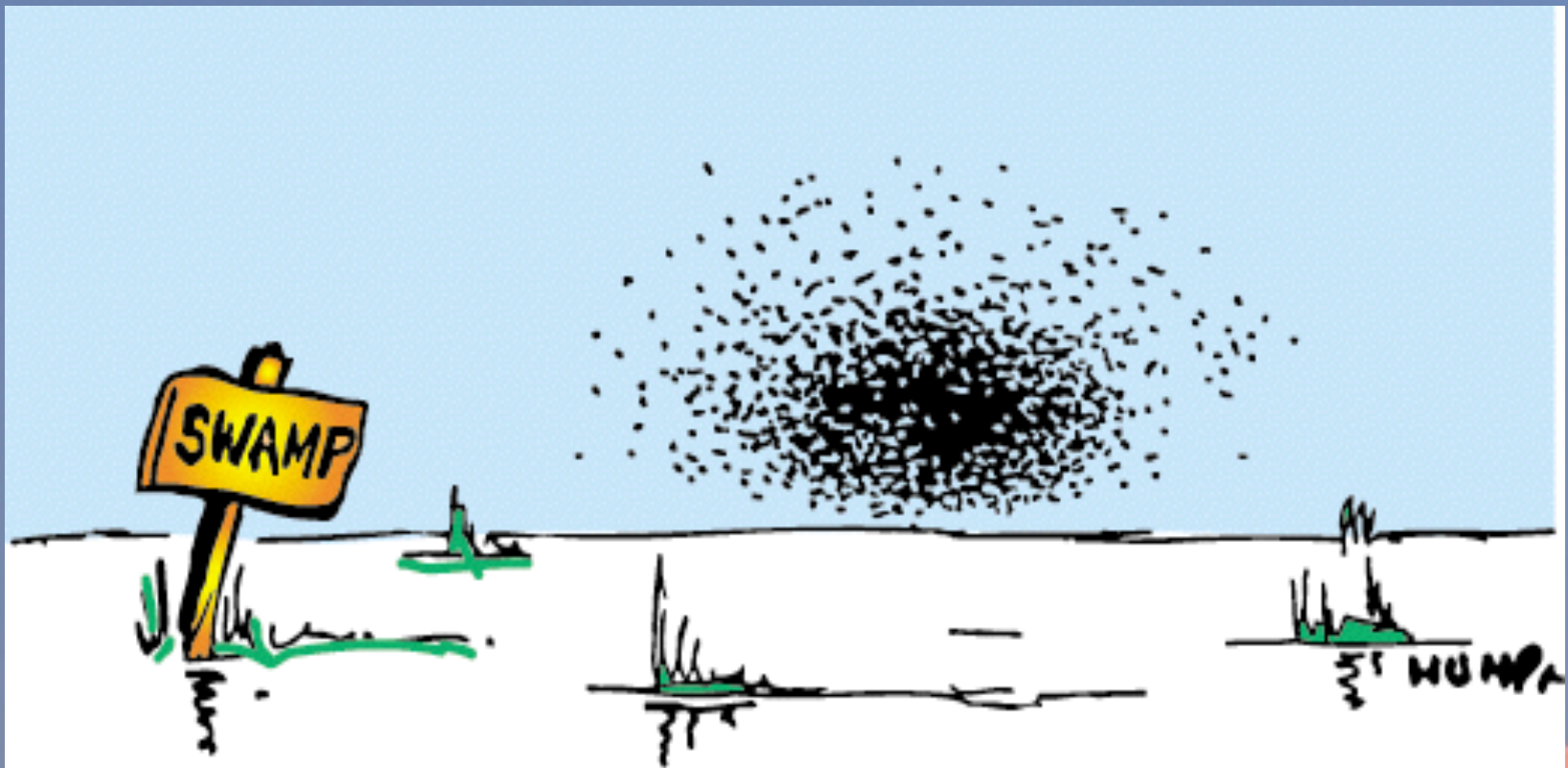
no collective interactions

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

$$S_e(\mathbf{k}, \omega) = N_e \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$



# Incoherent scattering - the short story



# Incoherent scattering - the short story



- We only see scattering from the electrons  
...but they also tell the story about the ion  
dynamics...

# Collective behavior...

- There are a number of wave modes existing inherently in the ionospheric plasma...

# Langmuir waves

- High frequency electrostatic waves
- Dispersion relation:

$$\omega_r = (\omega_{pe}^2 + 3k^2 v_{the}^2)^{1/2} = \omega_p (1 + 3k^2 \lambda_{De}^2)^{1/2}$$

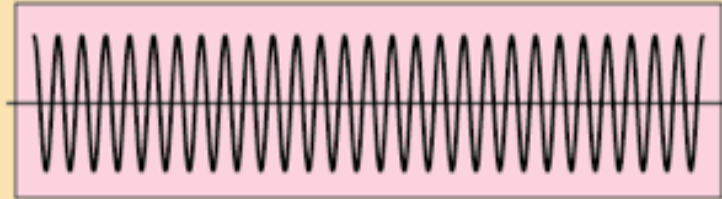
$$\omega_i = -c \frac{\omega_{pe}}{(k \lambda_{De})^3} \exp(-\frac{1}{2} k^2 \lambda_{De}^2), \quad c = \sqrt{\frac{\pi}{8}} e^{-3/2}$$

# Ion acoustic waves

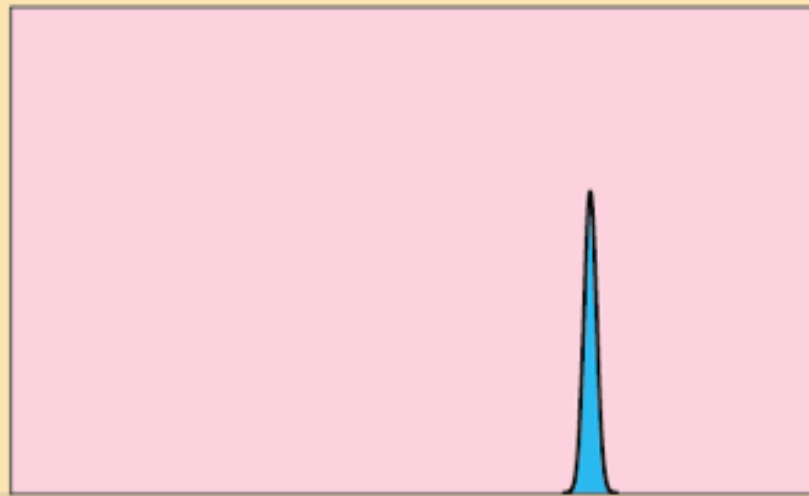
\* Ion acoustic waves:

$$(63) \quad \omega_r = \frac{u c_s}{1 + u^2 \tau_{ee}^2}, \quad c_s = \left( \frac{k_B T_e + 3k_B T_i}{m_i} \right)^{1/2}$$

$$(64) \quad \omega_i = -\sqrt{\frac{\pi}{8}} \frac{\omega_r}{(1 + u^2 \tau_{ee}^2)^{3/2}} \left[ \left( \frac{T_e}{T_i} \right)^{3/2} \exp \left( -\frac{T_e/T_i}{2(1 + u^2 \tau_{ee}^2)} \right) + \sqrt{\frac{m_e}{m_i}} \right]$$



time



frequency

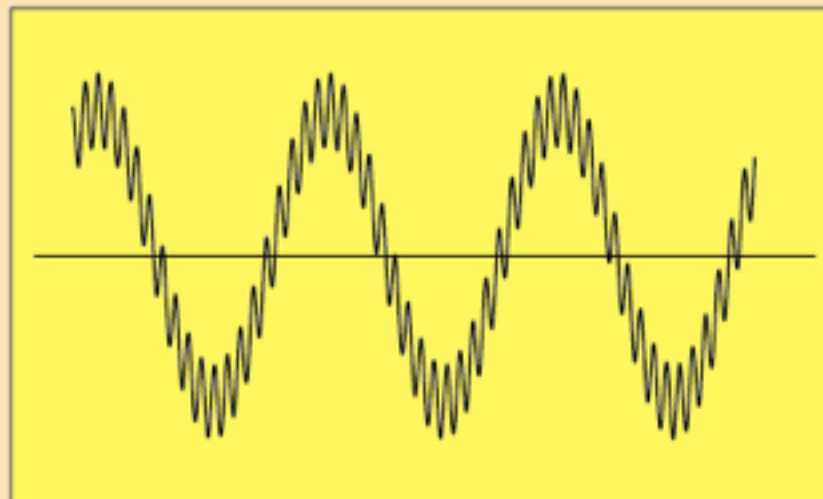


time

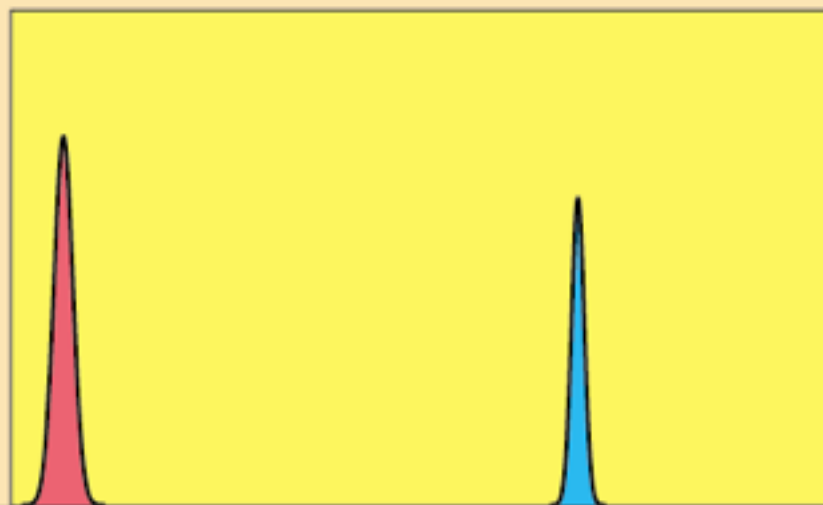


frequency



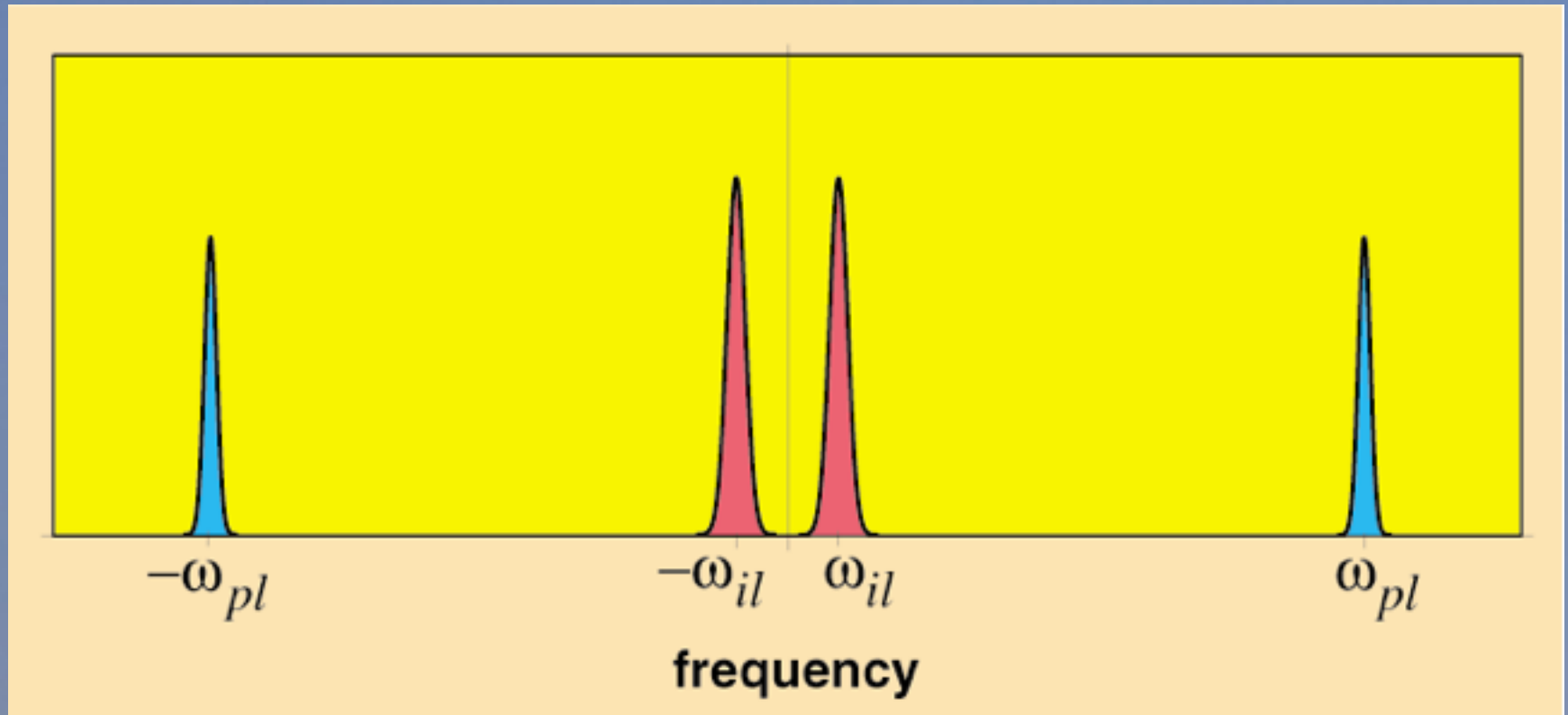


time



frequency

# Plasma Wave Approach (cont'd)



# Landau wave-particle interactions

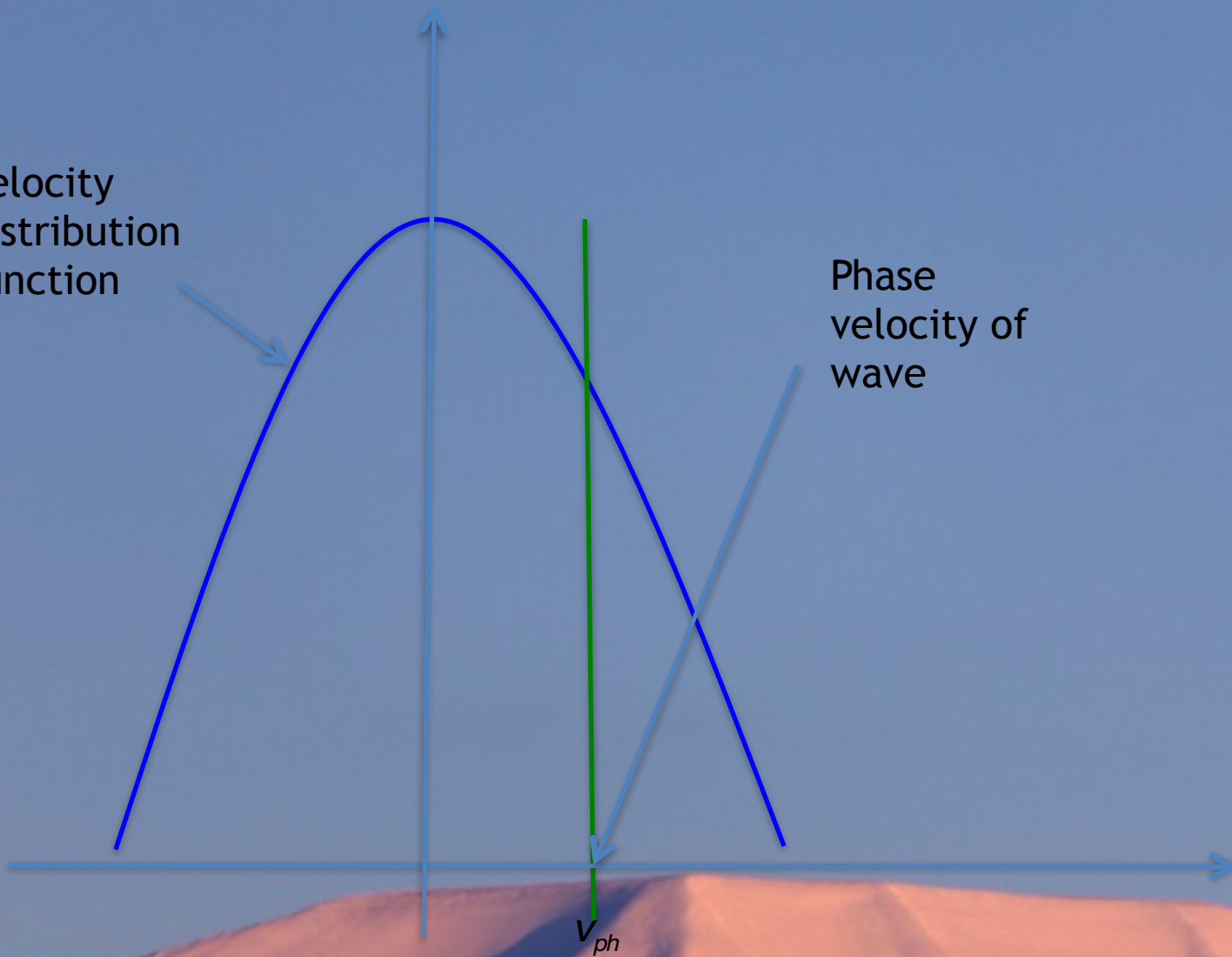


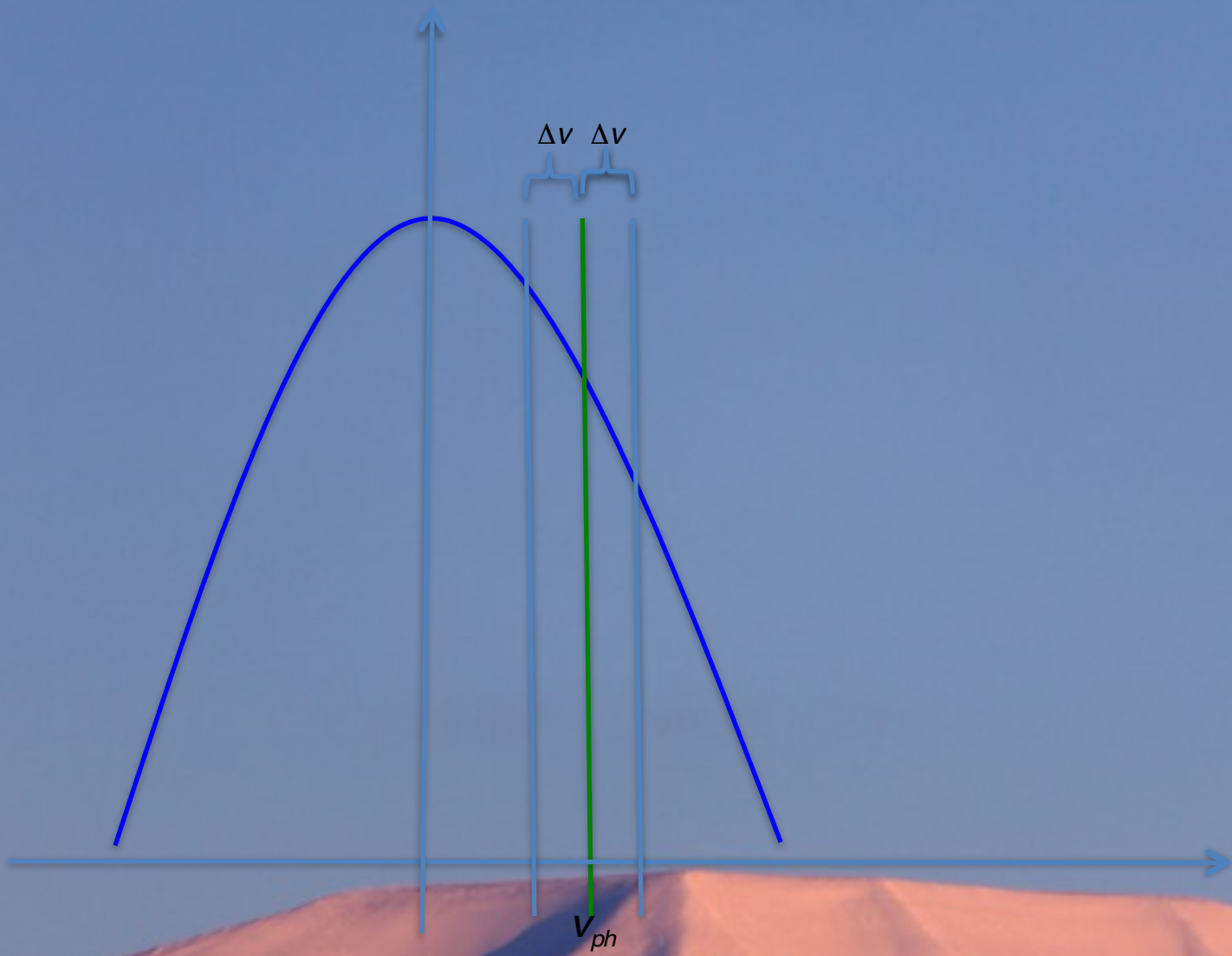
particle  
gains  
energy

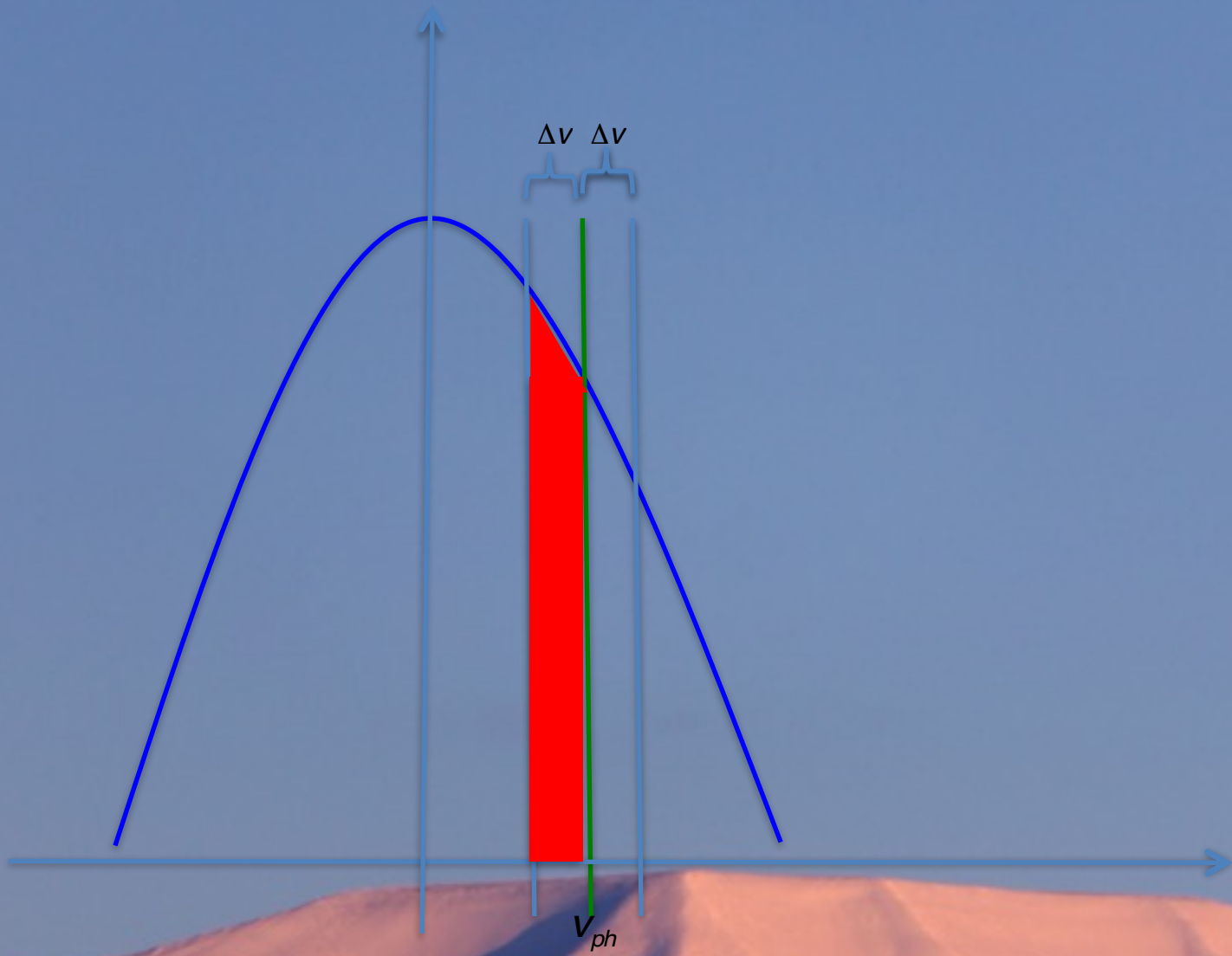
wave  
gains  
energy

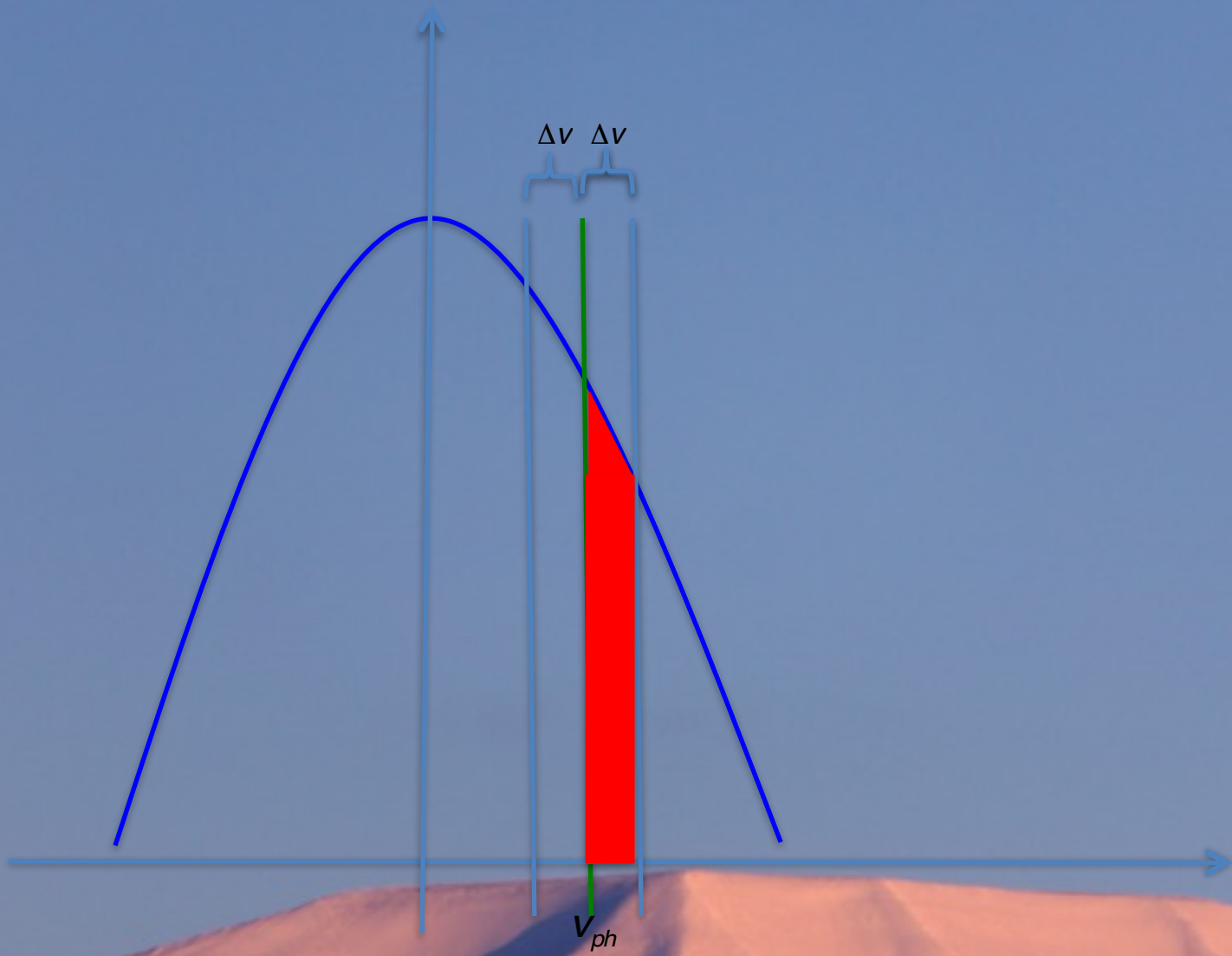
Velocity  
distribution  
function

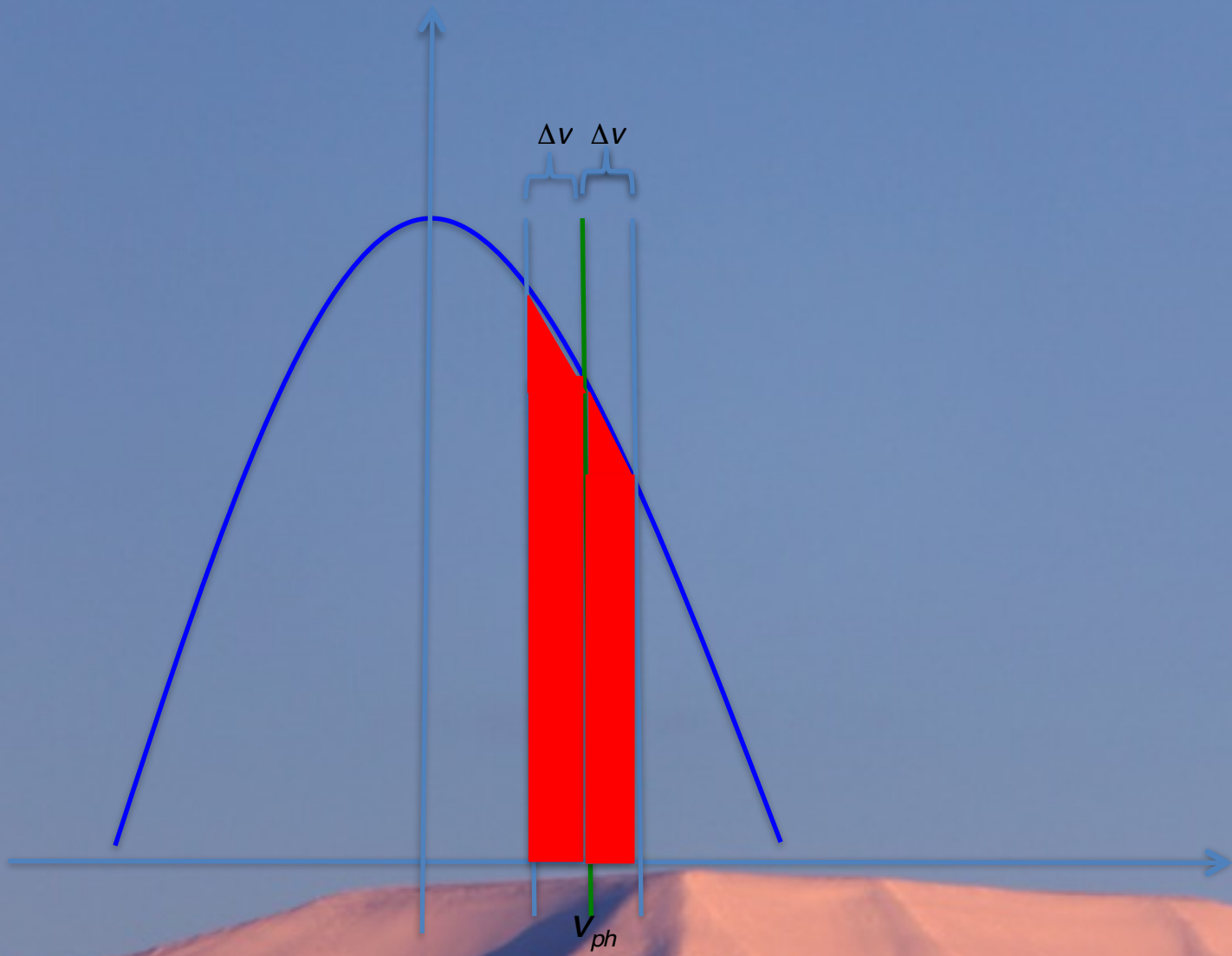
Phase  
velocity of  
wave











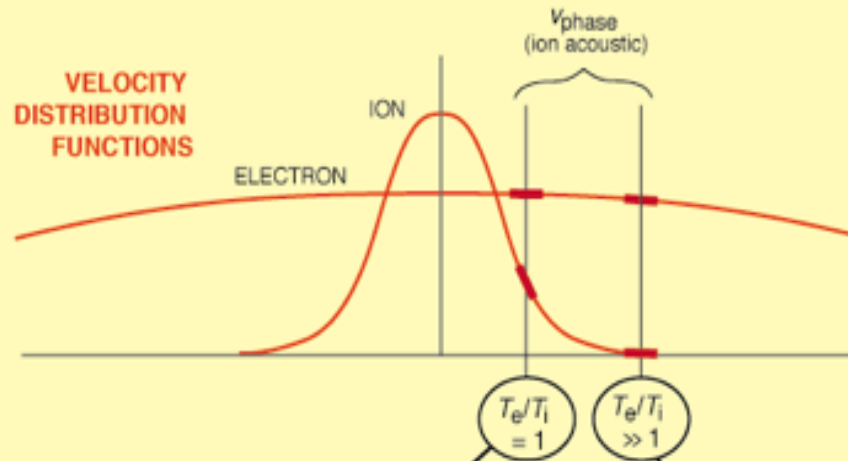


## THE EFFECT OF LANDAU DAMPING ON THE INCOHERENT SCATTER ION LINE SPECTRUM

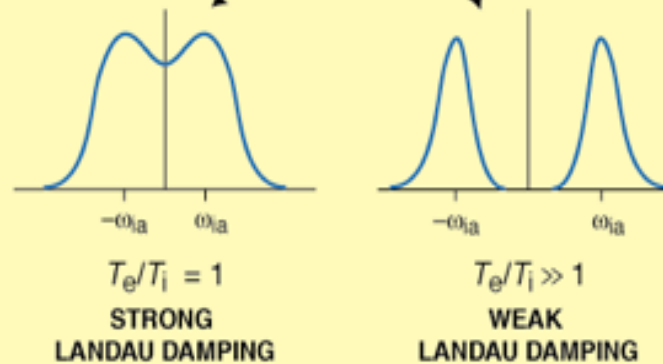
**ION-ACOUSTIC  
DISPERSION  
EQUATION**

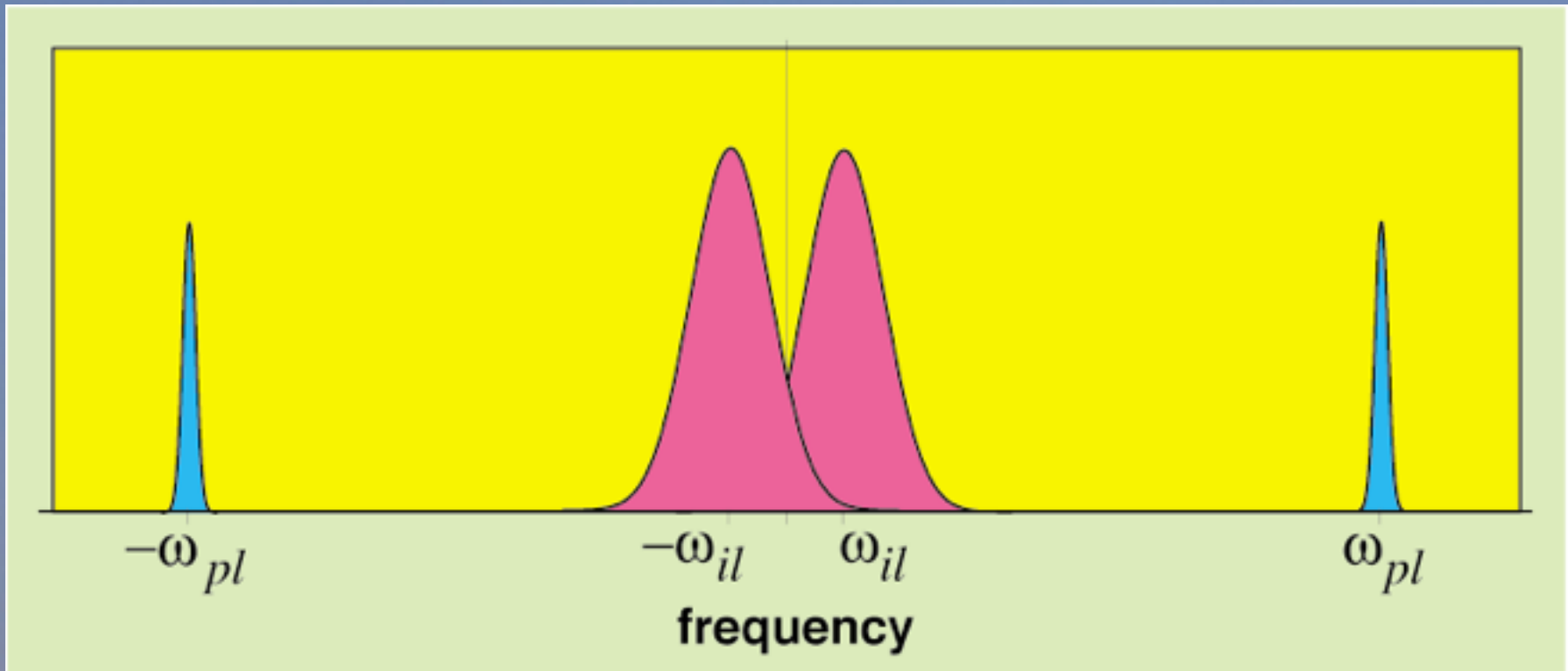
$$\omega_{ia} = k v_{\text{phase}} = k \left( \frac{T_e + 3T_i}{m_i} \right)^{1/2}$$

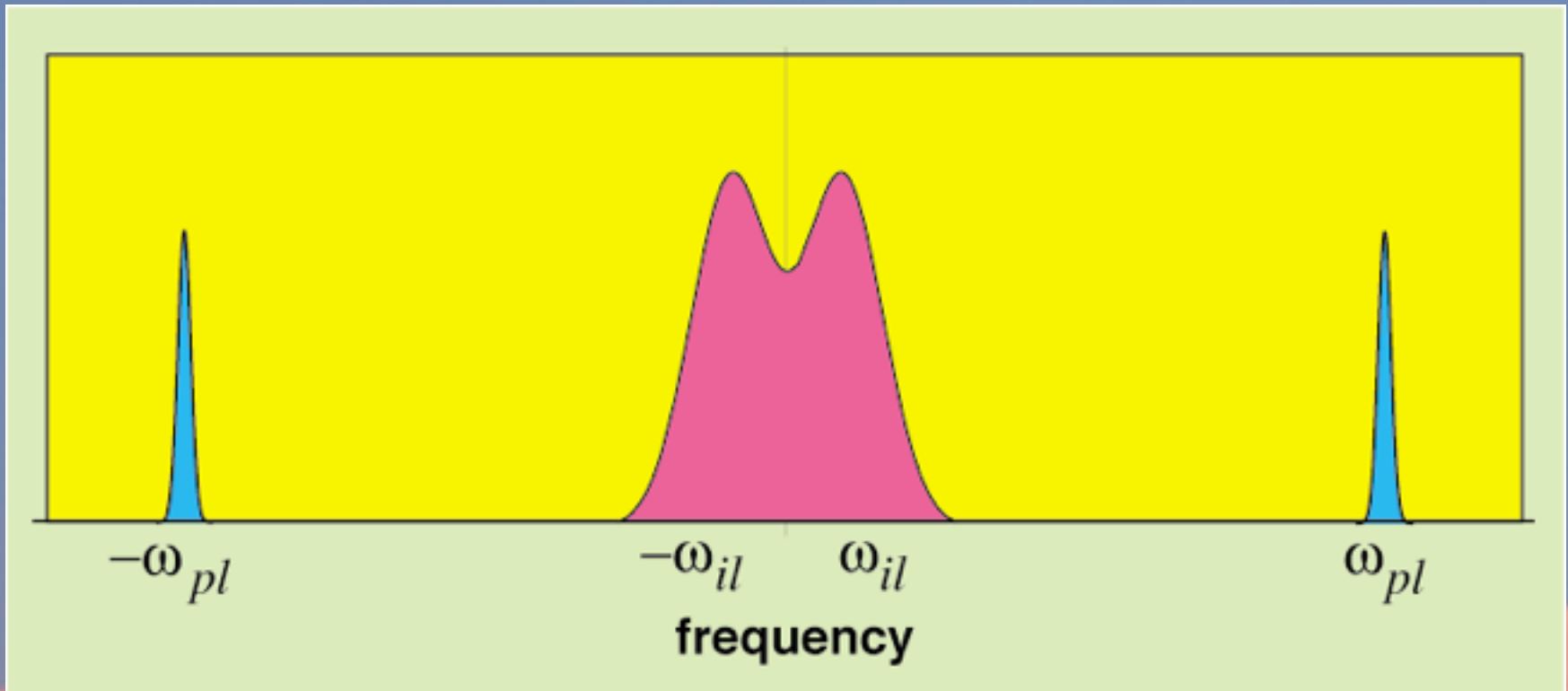
**VELOCITY  
DISTRIBUTION  
FUNCTIONS**



**INCOHERENT  
SCATTER  
ION LINE  
SPECTRA**







## Incoherent Scattering Spectrum

$$S_c(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

Plasma line

Ion line

electric susceptibility  $\chi_{e,i}(\mathbf{k}, \omega)$

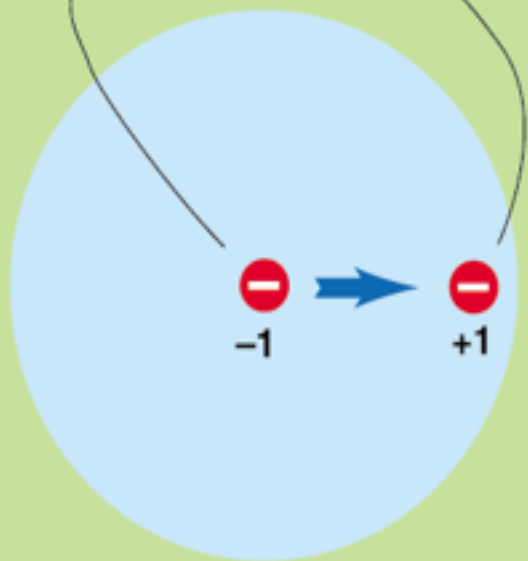
dielectric constant function  $\epsilon(\mathbf{k}, \omega)$

velocity distribution function  $f_{e,i}(\mathbf{v})$

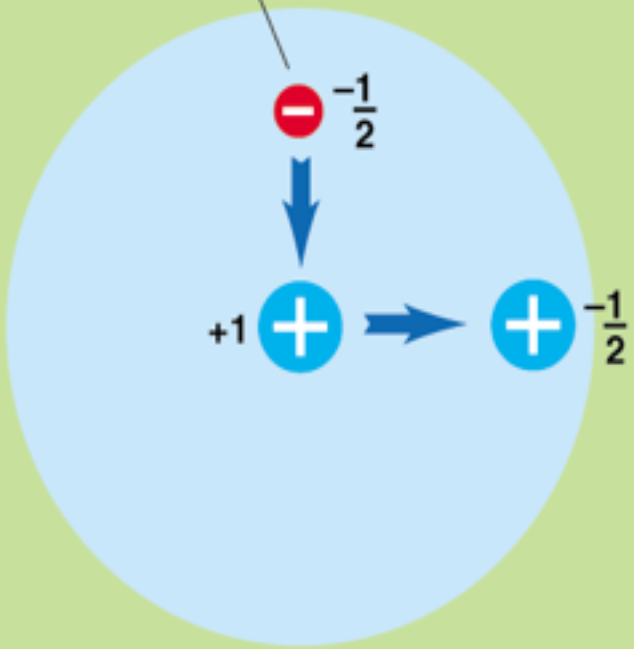
**Plasma Line  $S_{PL}(\mathbf{k}, \omega)$**

**Ion Line  $S_{IL}(\mathbf{k}, \omega)$**

$$S_c(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

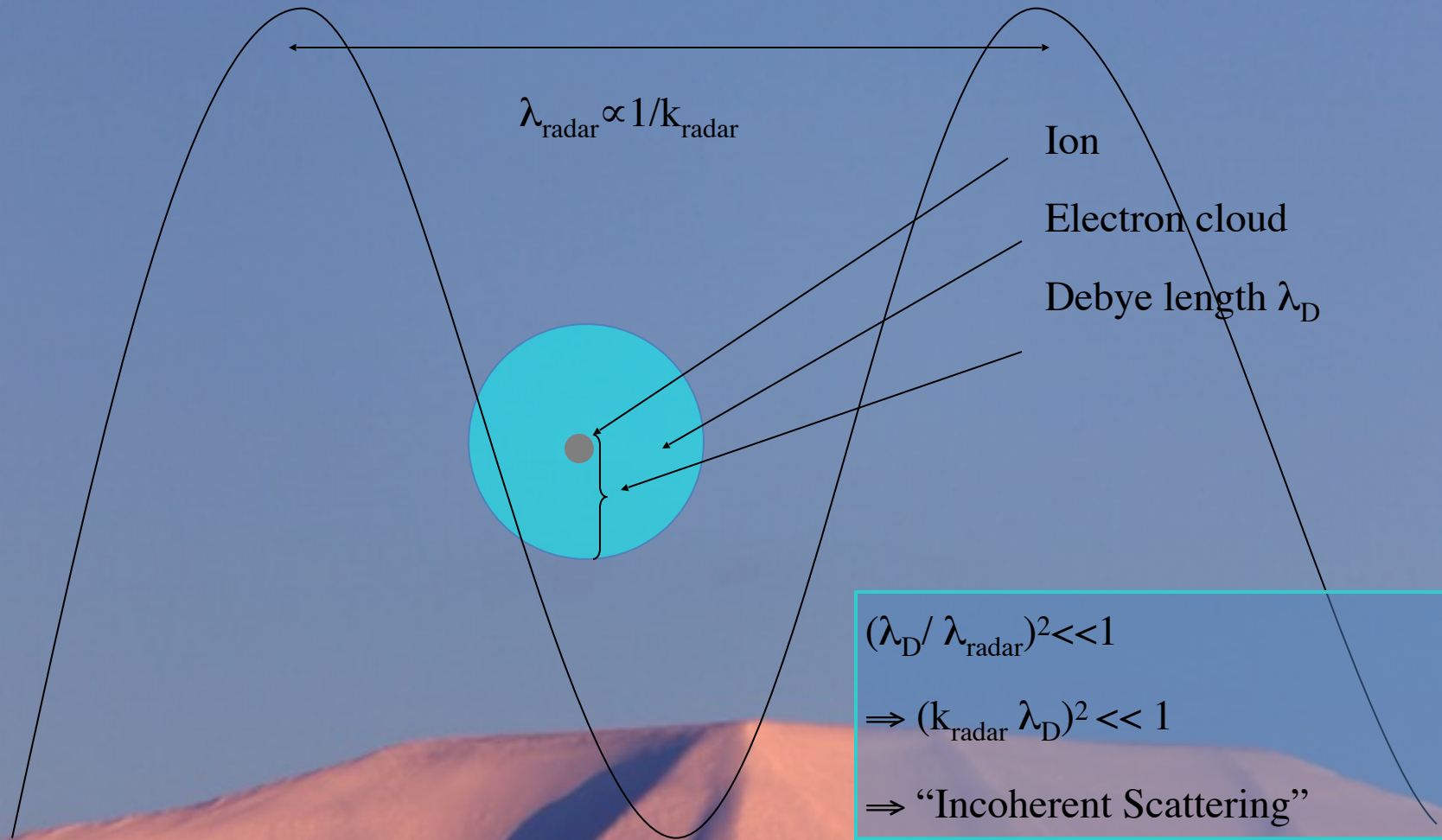


**electron with cloud**



**ion with cloud**

# Debye length dependence



**Plasma Line**  $S_{PL}(\mathbf{k}, \omega)$

**Ion Line**  $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

**Plasma Line**  $S_{PL}(\mathbf{k}, \omega)$

**Ion Line**  $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

$$\epsilon(\mathbf{k}, \omega) = 0$$

$$\omega_{pl}(k) \approx \omega_{pe} (1 + 3\lambda_D^2 k^2)$$

$$\omega_{ia}(k) \approx k \sqrt{\frac{T_e + 3T_i}{m_i}}$$



Plasma Line  $S_{PL}(\mathbf{k}, \omega)$

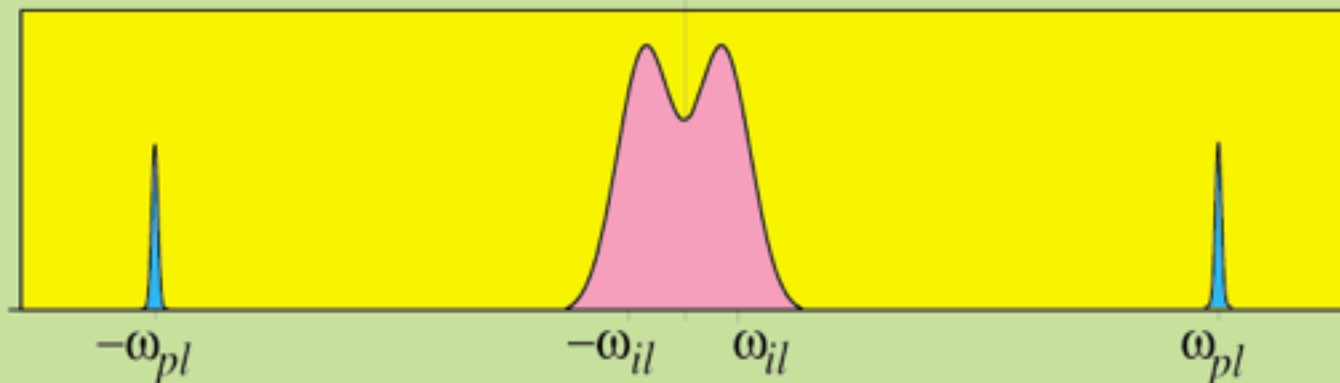
Ion Line  $S_{IL}(\mathbf{k}, \omega)$

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

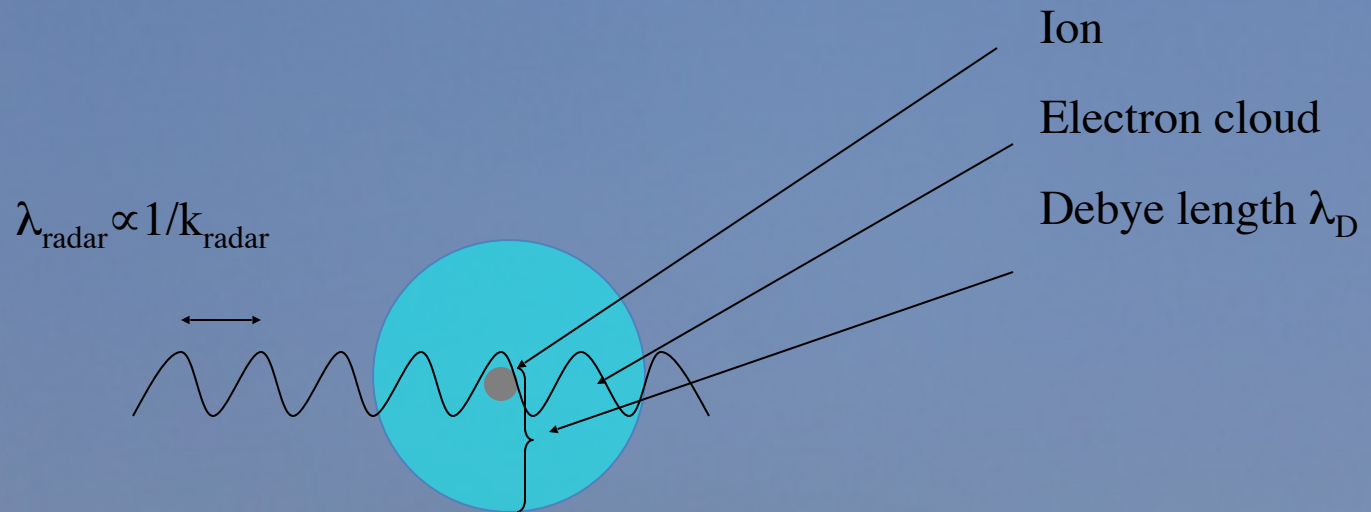
$$\epsilon(\mathbf{k}, \omega) = 0$$

$$\omega_{pl}(k) \approx \omega_{pe} (1 + 3\lambda_D^2 k^2)$$

$$\omega_{ia}(k) \approx k \sqrt{\frac{T_e + 3T_i}{m_i}}$$



# Debye length dependence



$$(\lambda_D / \lambda_{\text{radar}})^2 > 1$$

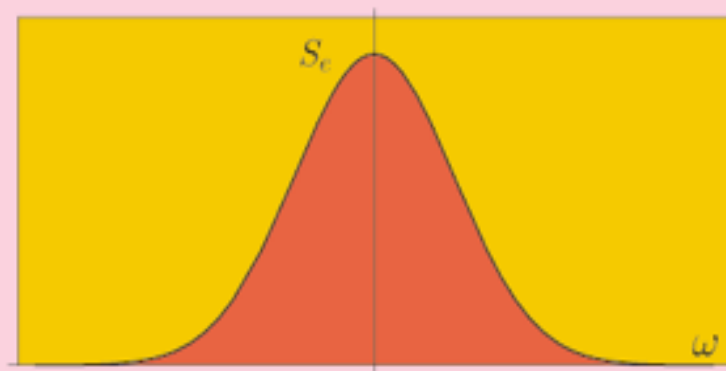
$$\Rightarrow (k_{\text{radar}} \lambda_D)^2 > 1$$

$\Rightarrow$  No collective interactions

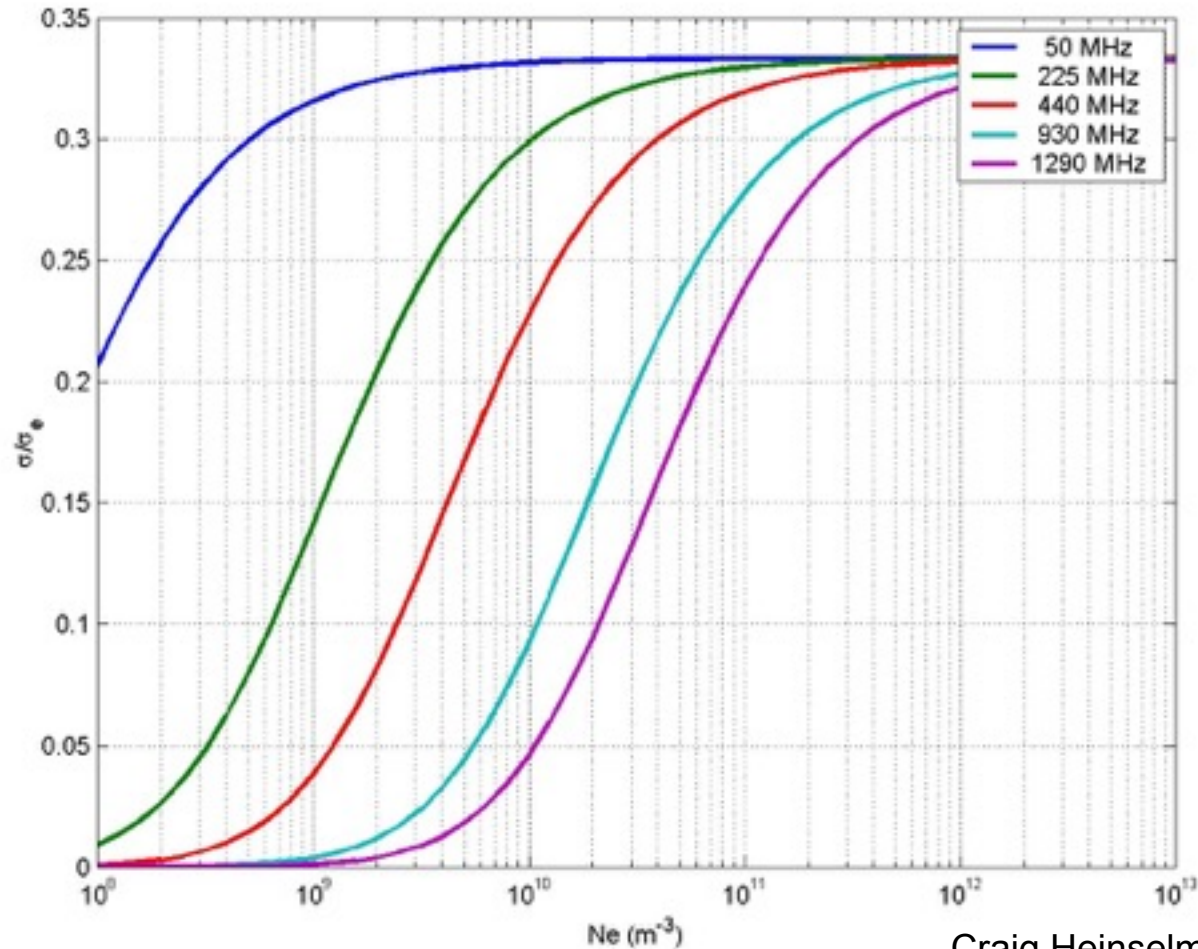
no collective interactions

$$S_e(\mathbf{k}, \omega) = N_e \left| 1 - \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v}) + N_i \left| \frac{\chi_e(\mathbf{k}, \omega)}{\epsilon(\mathbf{k}, \omega)} \right|^2 \int d\mathbf{v} f_i(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$

$$S_e(\mathbf{k}, \omega) = N_e \int d\mathbf{v} f_e(\mathbf{v}) \delta(\omega - \mathbf{k} \cdot \mathbf{v})$$



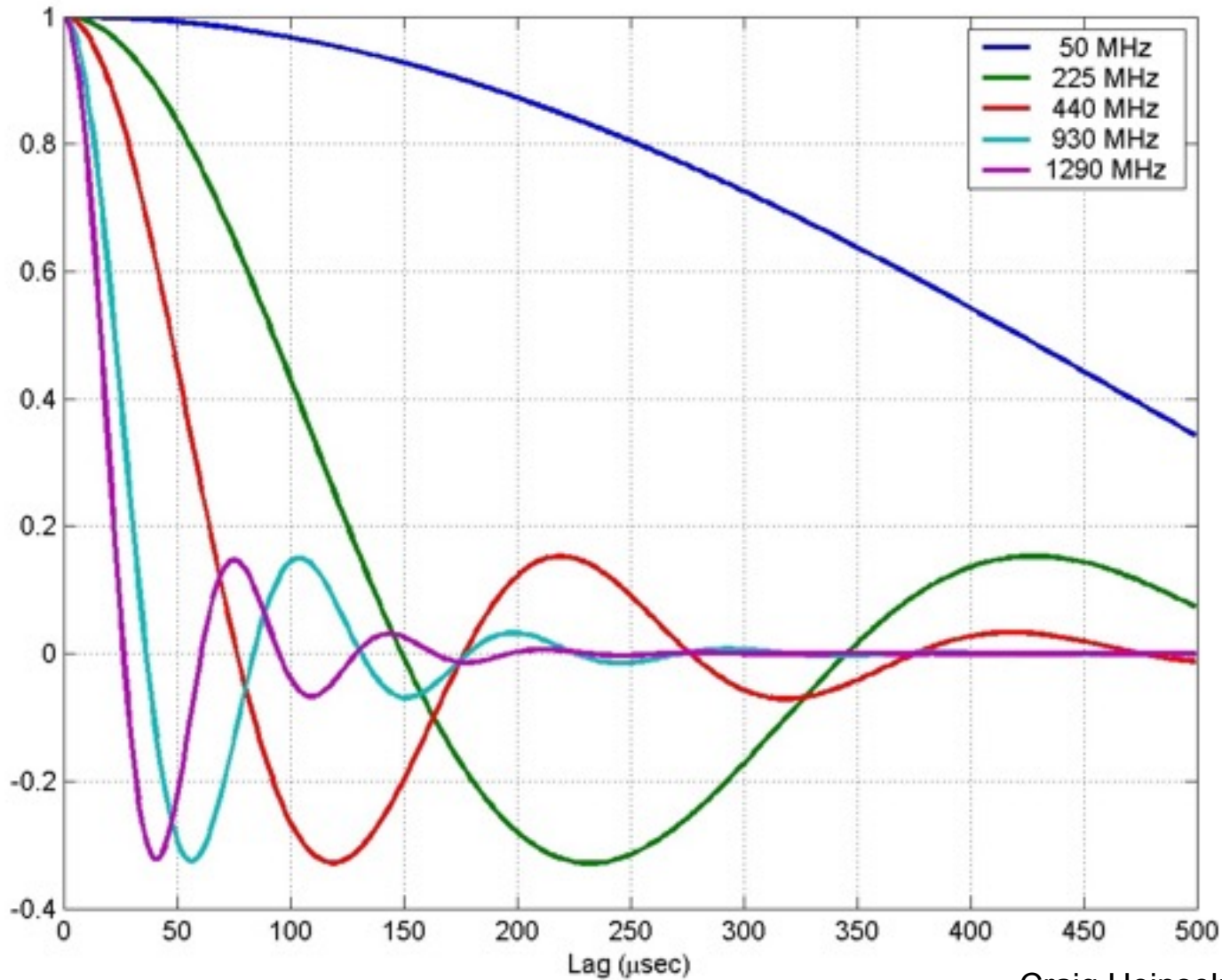
# Debye Length Dependencies



Parameters  
Ti: 1000 K  
Te: 2000 K

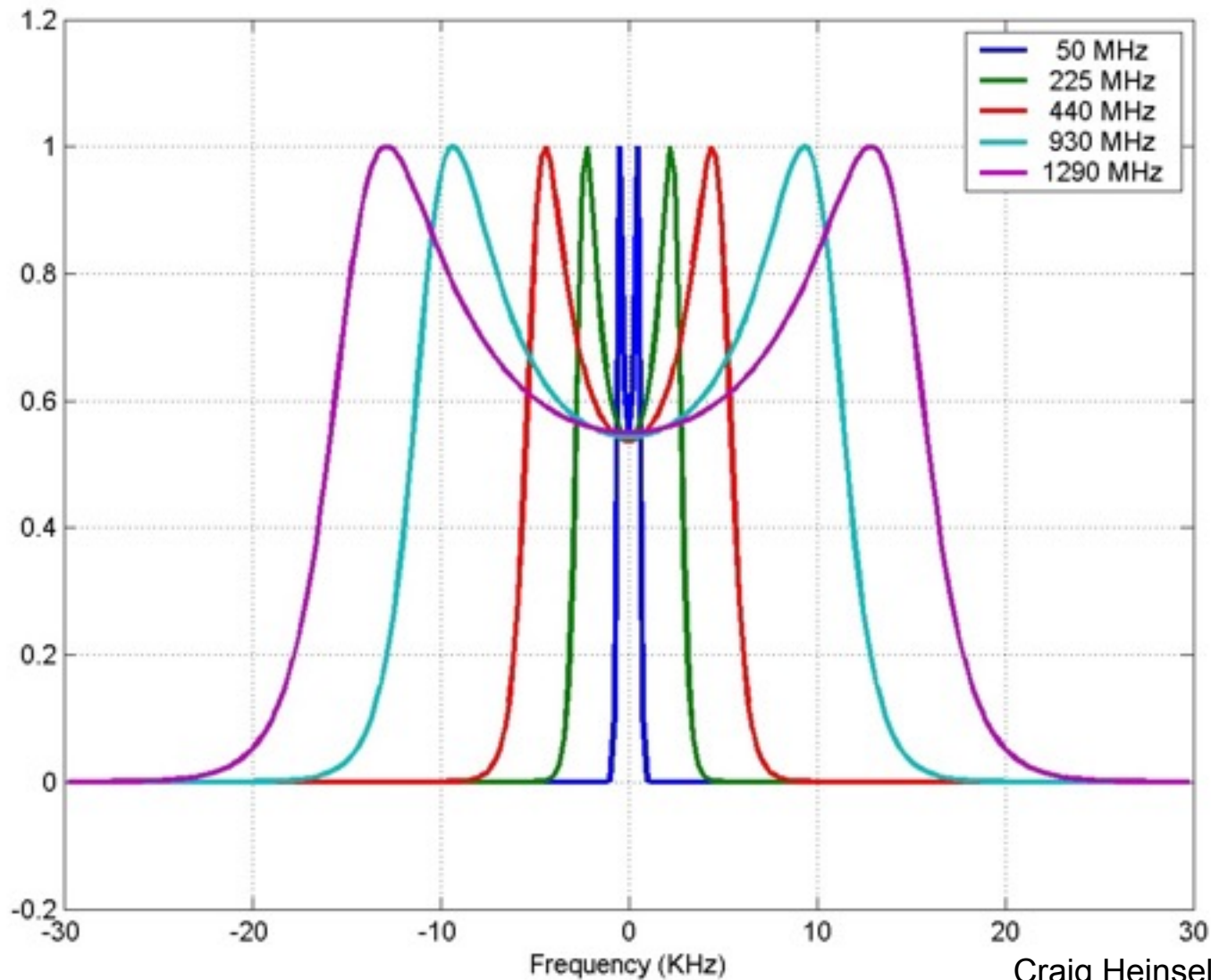
Craig Heinselman

# Radar Frequency Dependencies



Parameters  
Ne:  $10^{12} \text{ m}^{-3}$   
Ti: 1000 K  
Te: 2000 K  
Comp: 100% O<sup>+</sup>  
 $v_{in}$ :  $10^{-6} \text{ KHz}$

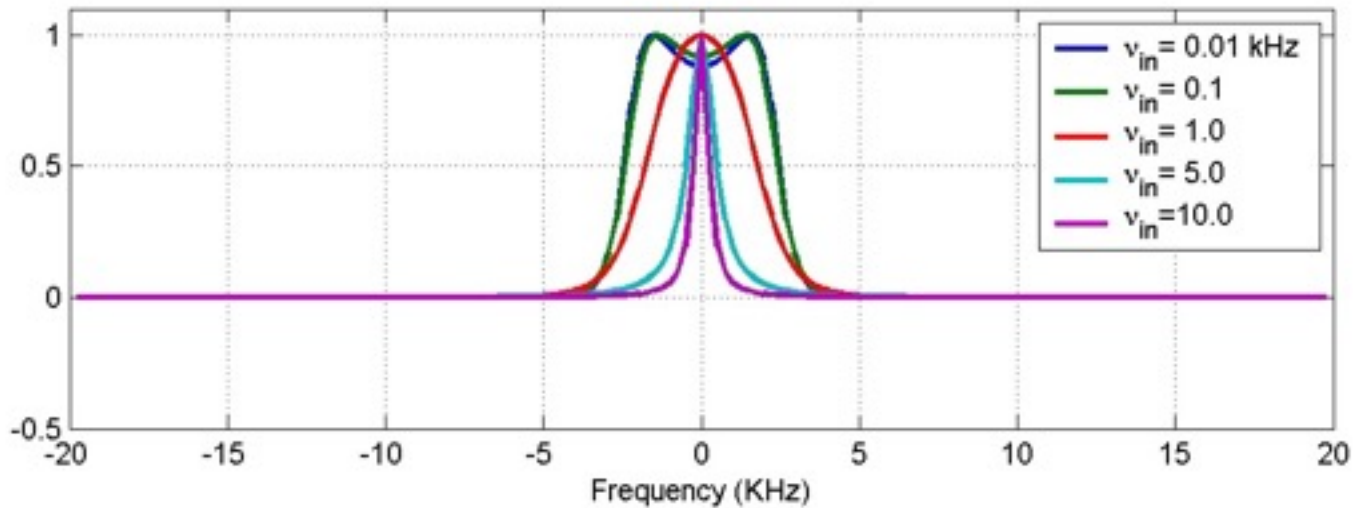
# Radar Frequency Dependencies



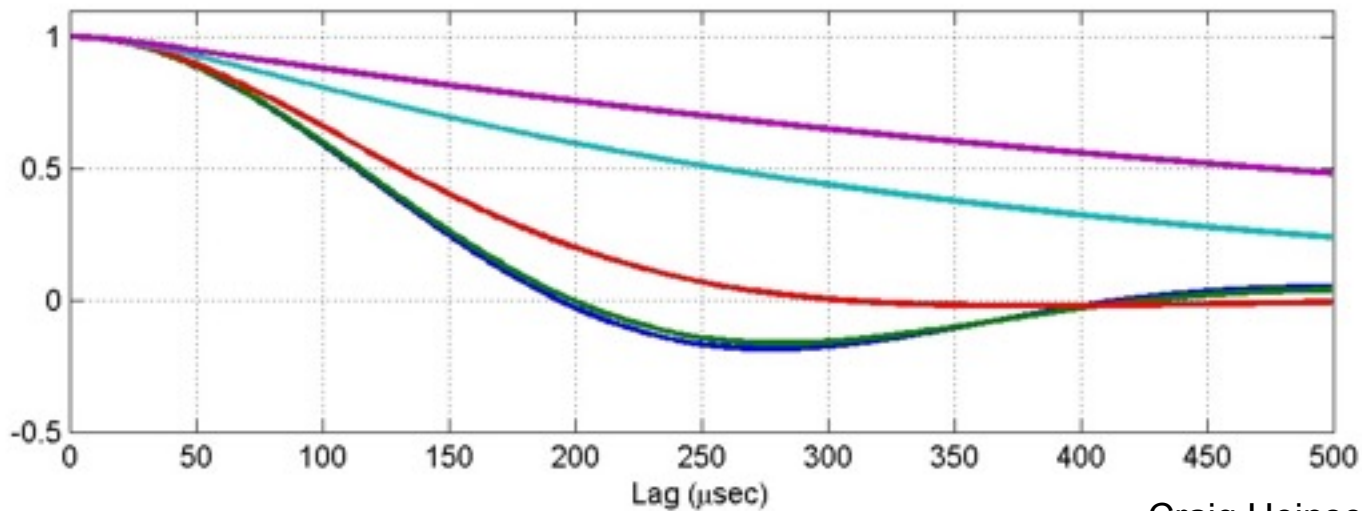
Parameters  
Ne:  $10^{12} \text{ m}^{-3}$   
Ti: 1000 K  
Te: 2000 K  
Comp: 100% O<sup>+</sup>  
 $v_{in}$ :  $10^{-6} \text{ KHz}$

With the frequency of the radar chosen (which is a one time thing!), how does the spectra depend on geophysical parameters?

# Ion-Neutral Collision Frequency

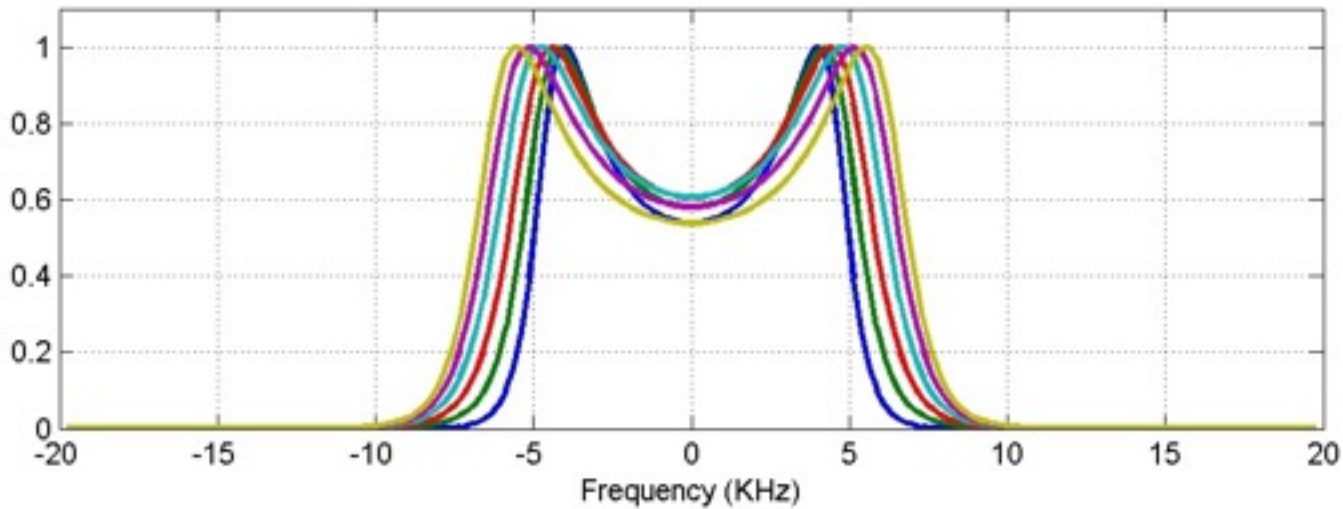


Parameters  
Freq: 449 MHz  
Ne:  $10^{12} \text{ m}^{-3}$   
Ti: 500 K  
Te: 500 K  
Comp: 100% NO<sup>+</sup>

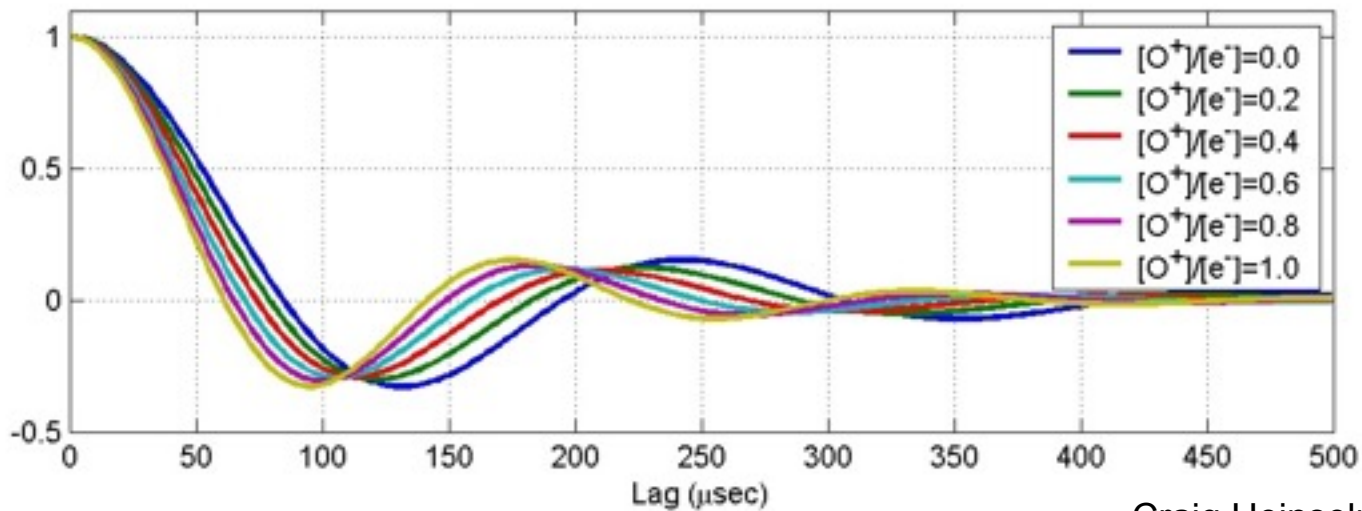




# Ion Composition ( $O^+$ vs. $NO^+$ )

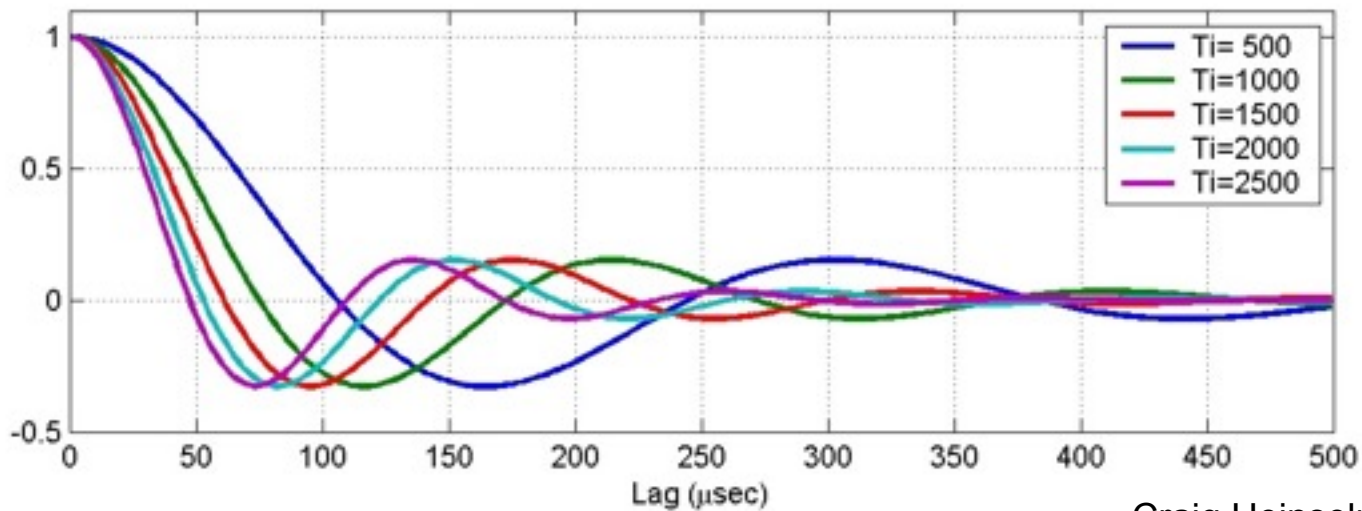
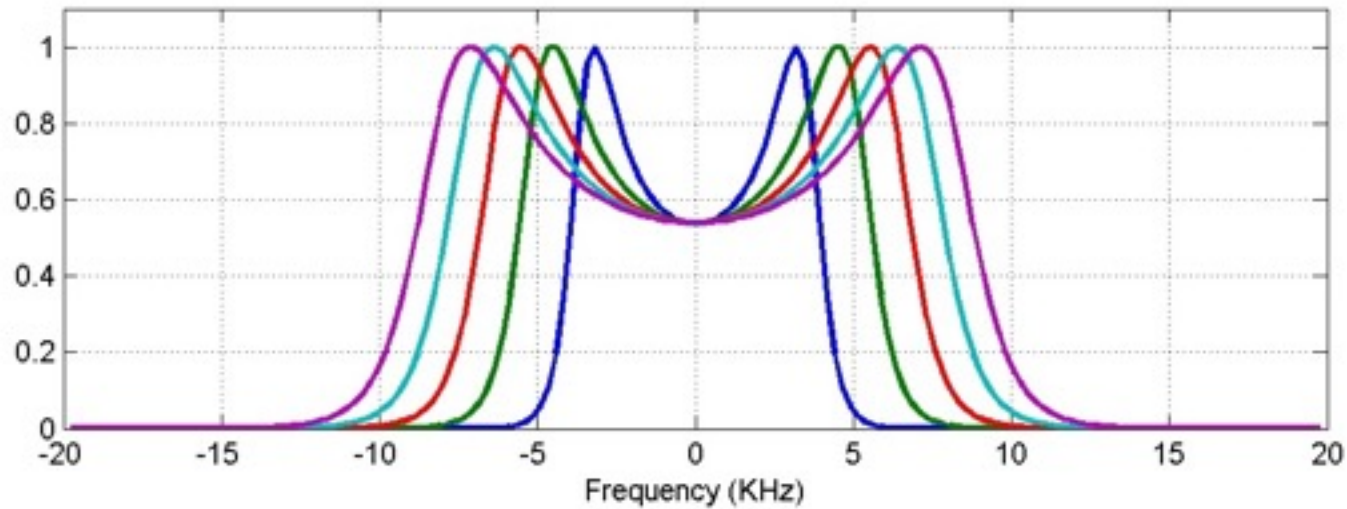


Parameters  
Freq: 449 MHz  
Ne:  $10^{12} \text{ m}^{-3}$   
Ti: 1500 K  
Te: 3000 K  
 $v_{in}$ :  $10^{-6} \text{ KHz}$

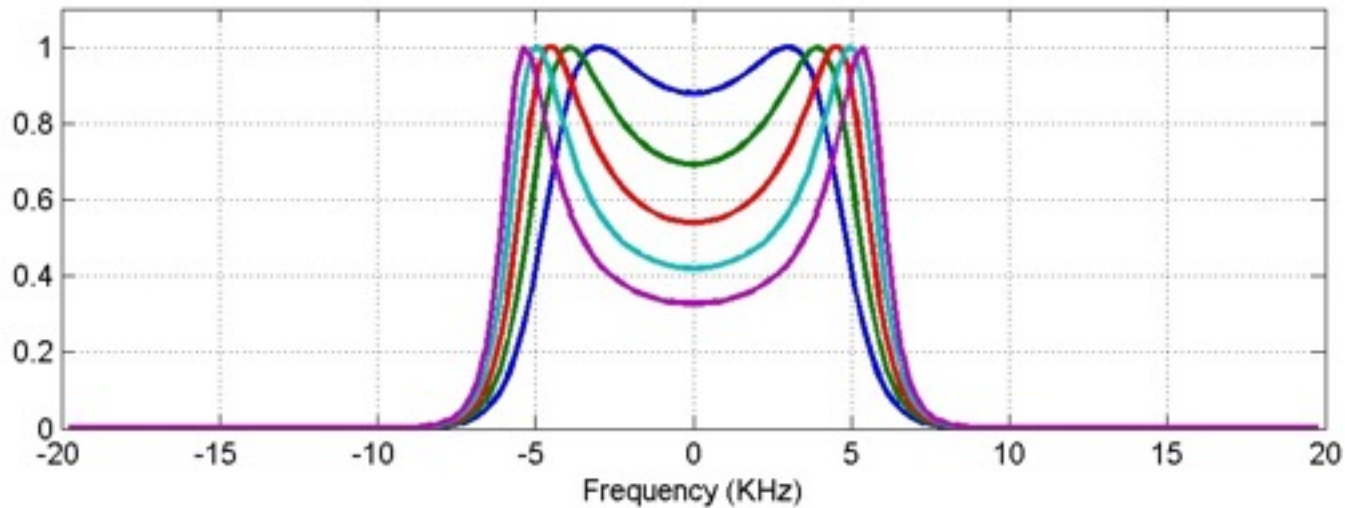


# Ion Temperature

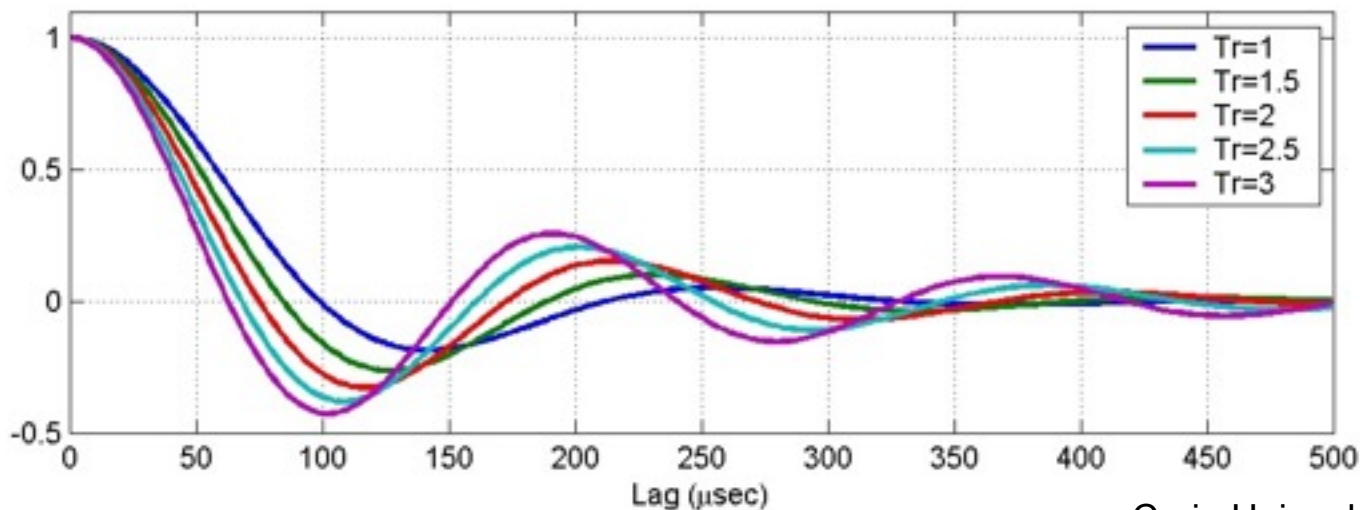
Parameters  
Freq: 449 MHz  
Ne:  $10^{12} \text{ m}^{-3}$   
Te:  $2 * T_i$   
Comp: 100% O<sup>+</sup>  
 $v_{in}$ :  $10^{-6} \text{ KHz}$



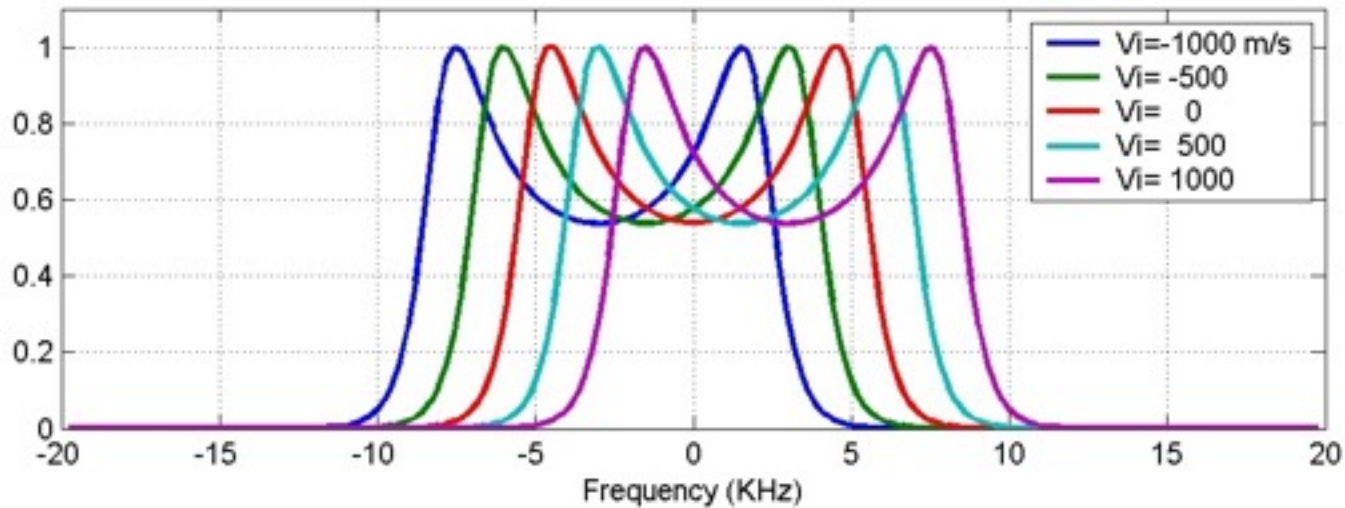
# Electron/Ion Temperature Ratio



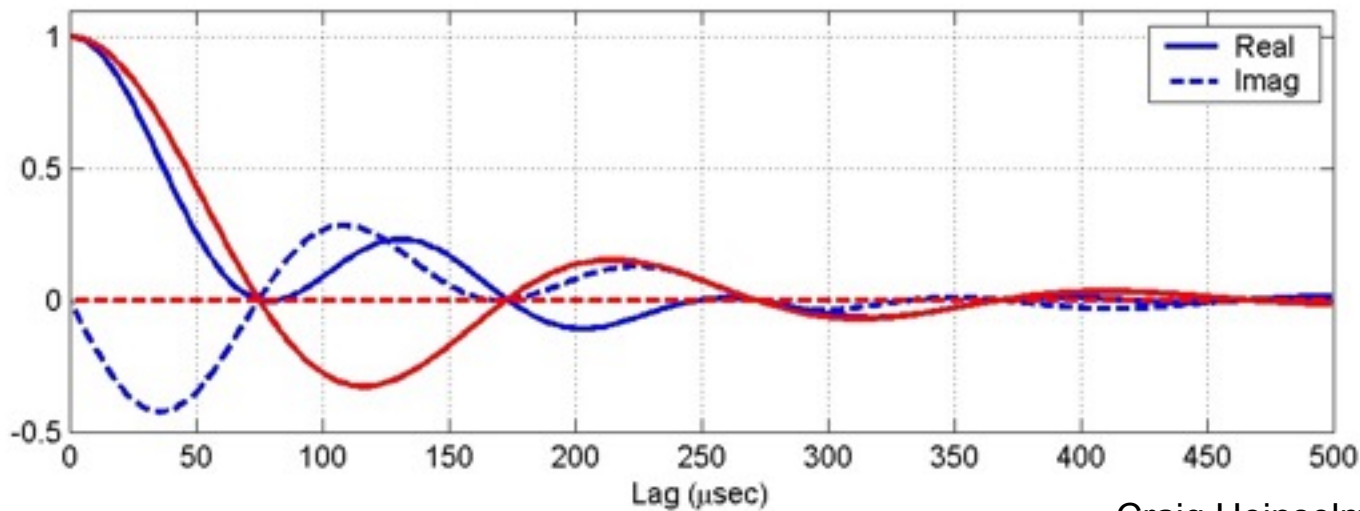
Parameters  
Freq: 449 MHz  
Ne:  $10^{12} \text{ m}^{-3}$   
Ti: 1000 K  
Comp: 100% O<sup>+</sup>  
 $v_{in}$ :  $10^{-6} \text{ KHz}$



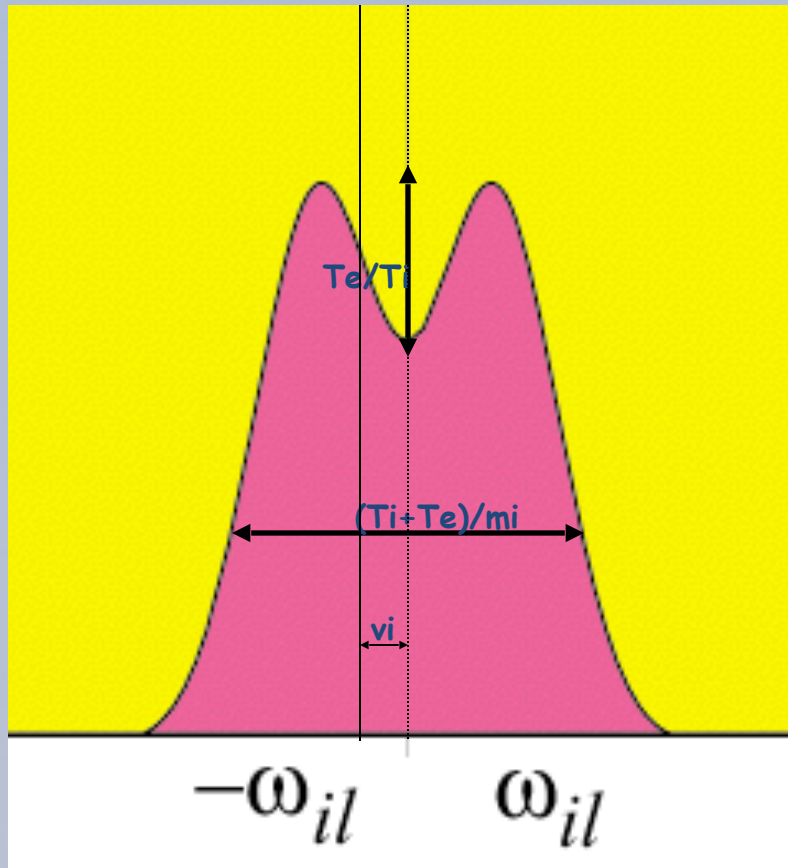
# Ion Velocity



Parameters  
Freq: 449 MHz  
Ne:  $10^{12}$  m $^{-3}$   
Ti: 1000 K  
Te: 2000 K  
Comp: 100% O $^+$   
 $v_{in}$ :  $10^{-6}$  KHz

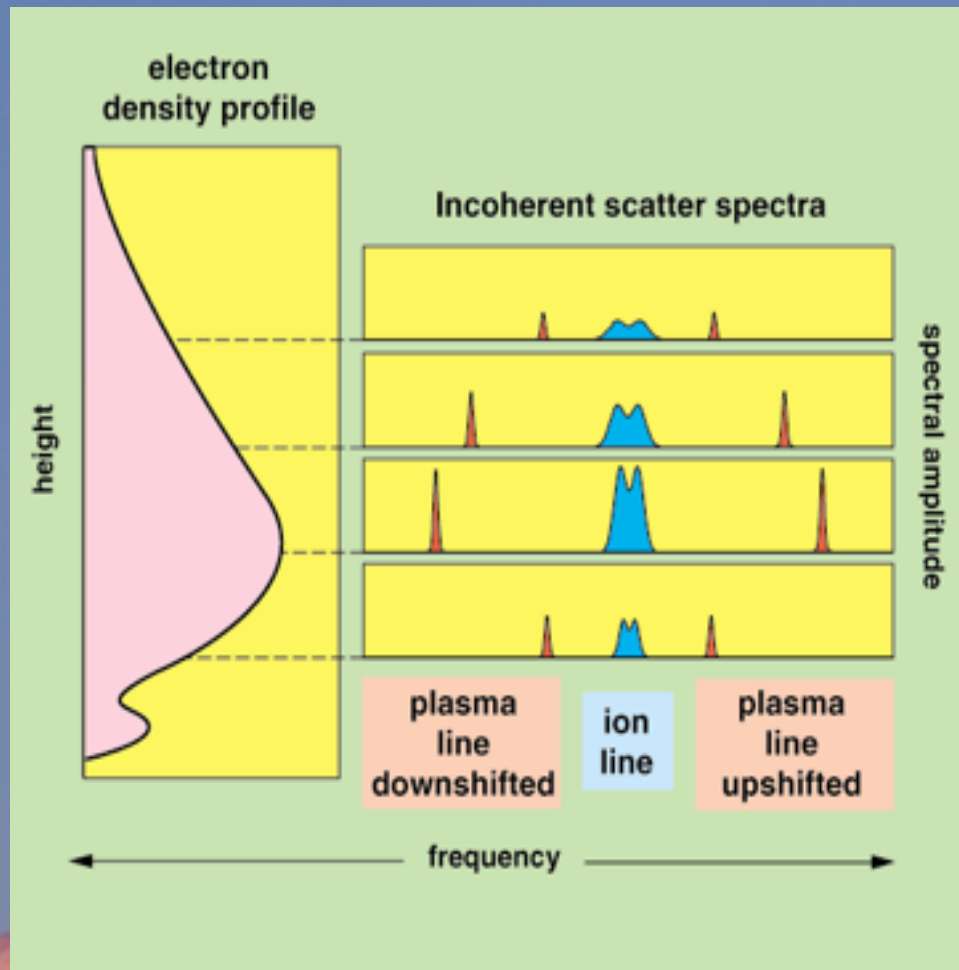


...or to sum up...

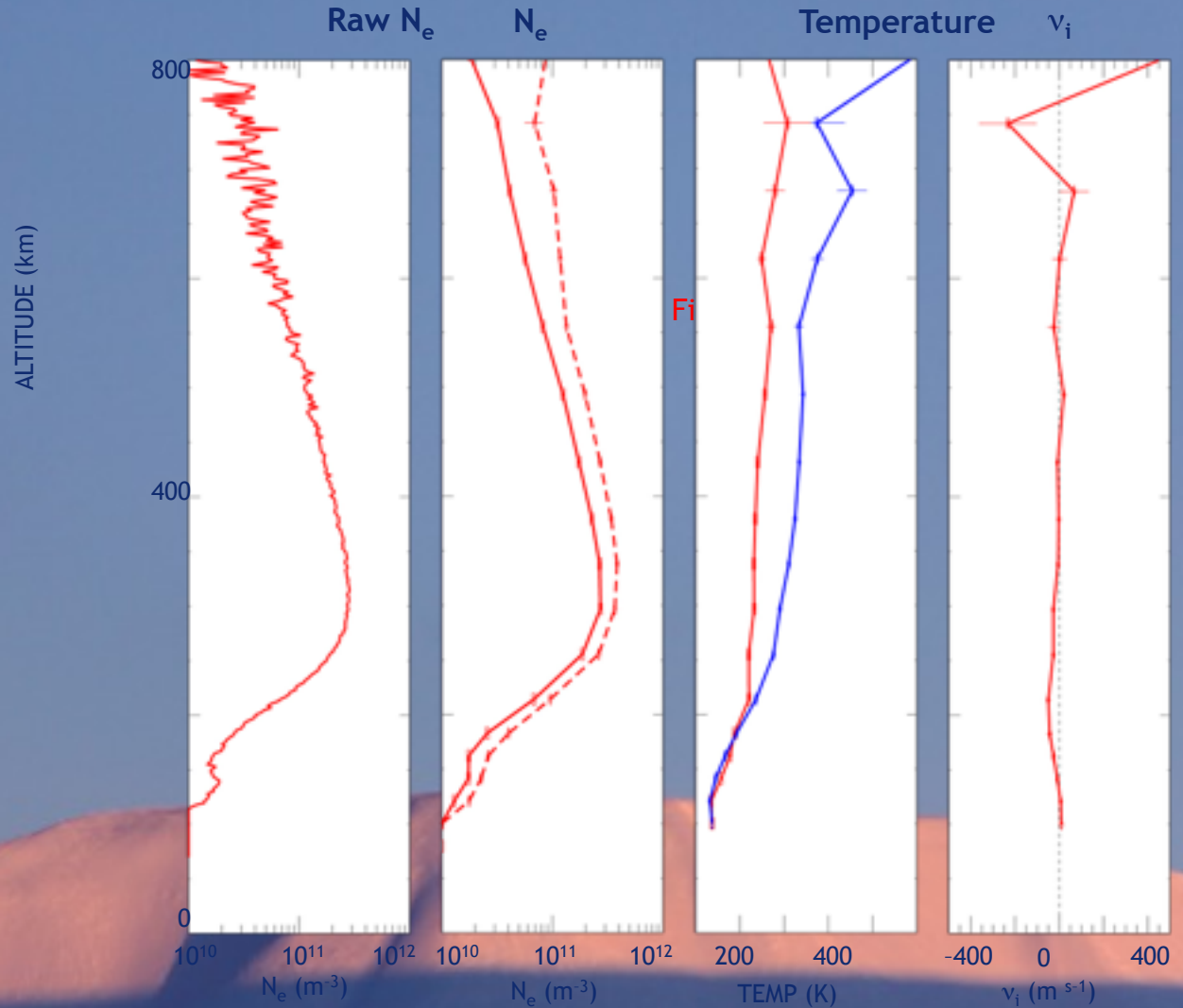
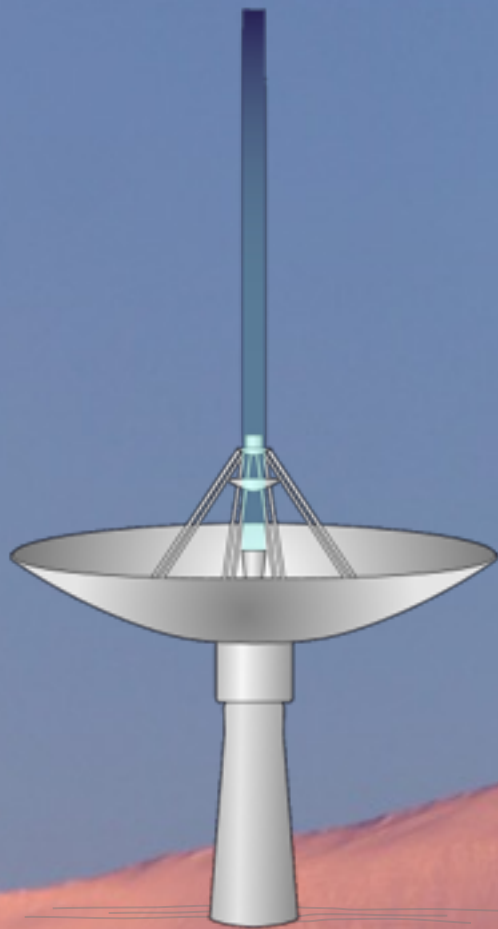


- Ion (and electron) temperature ( $T_i$  and  $T_e$ ) to ion mass ( $m_i$ ) ratio from the width of the spectra
- Electron to ion temperature ratio ( $T_e/T_i$ ) from “peak\_to\_valley” ratio
- Electron (= ion) density from total area (corrected for temperatures)
- Ion velocity ( $v_i$ ) from the Doppler shift

# Spectral space as a function of altitude



# Plasma Parameter Profile



July 2016

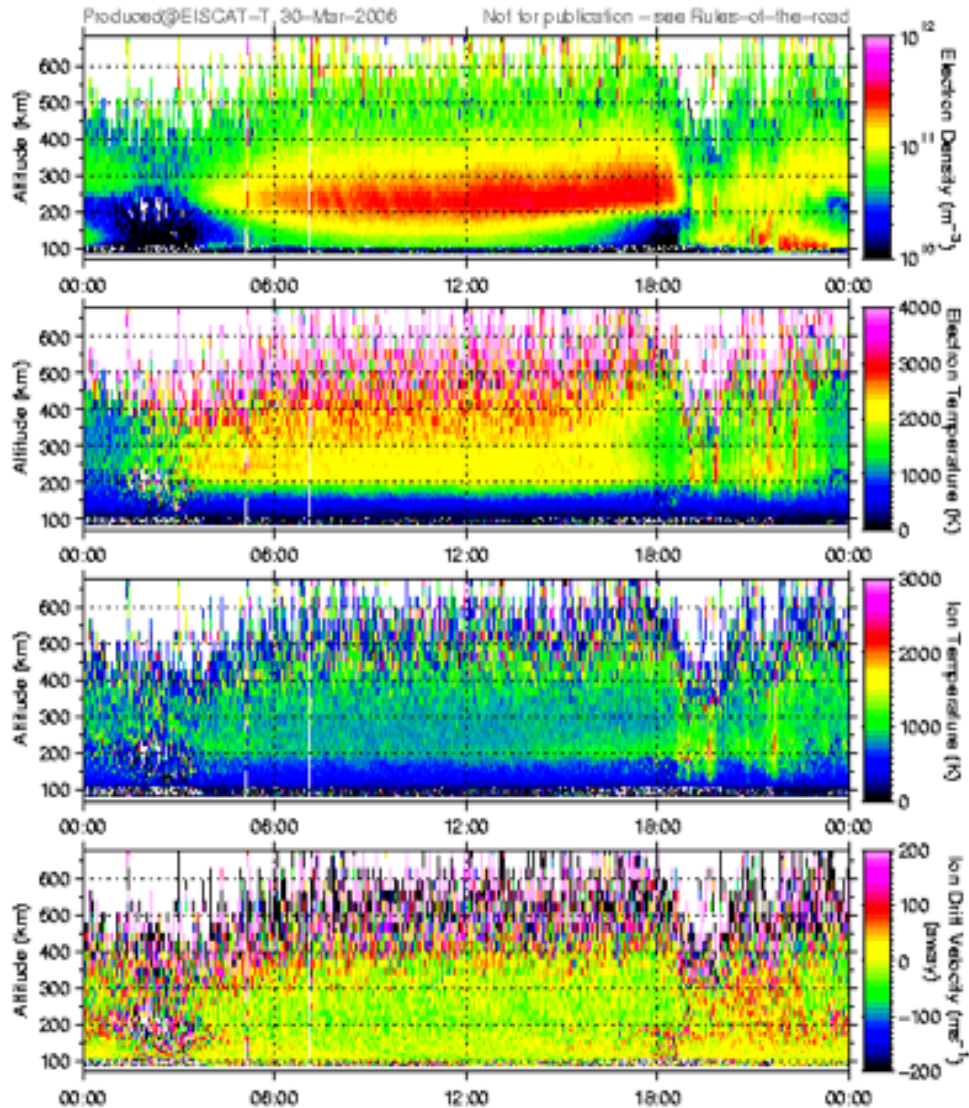
ISR Summer School Sodankylä



# EISCAT Scientific Association

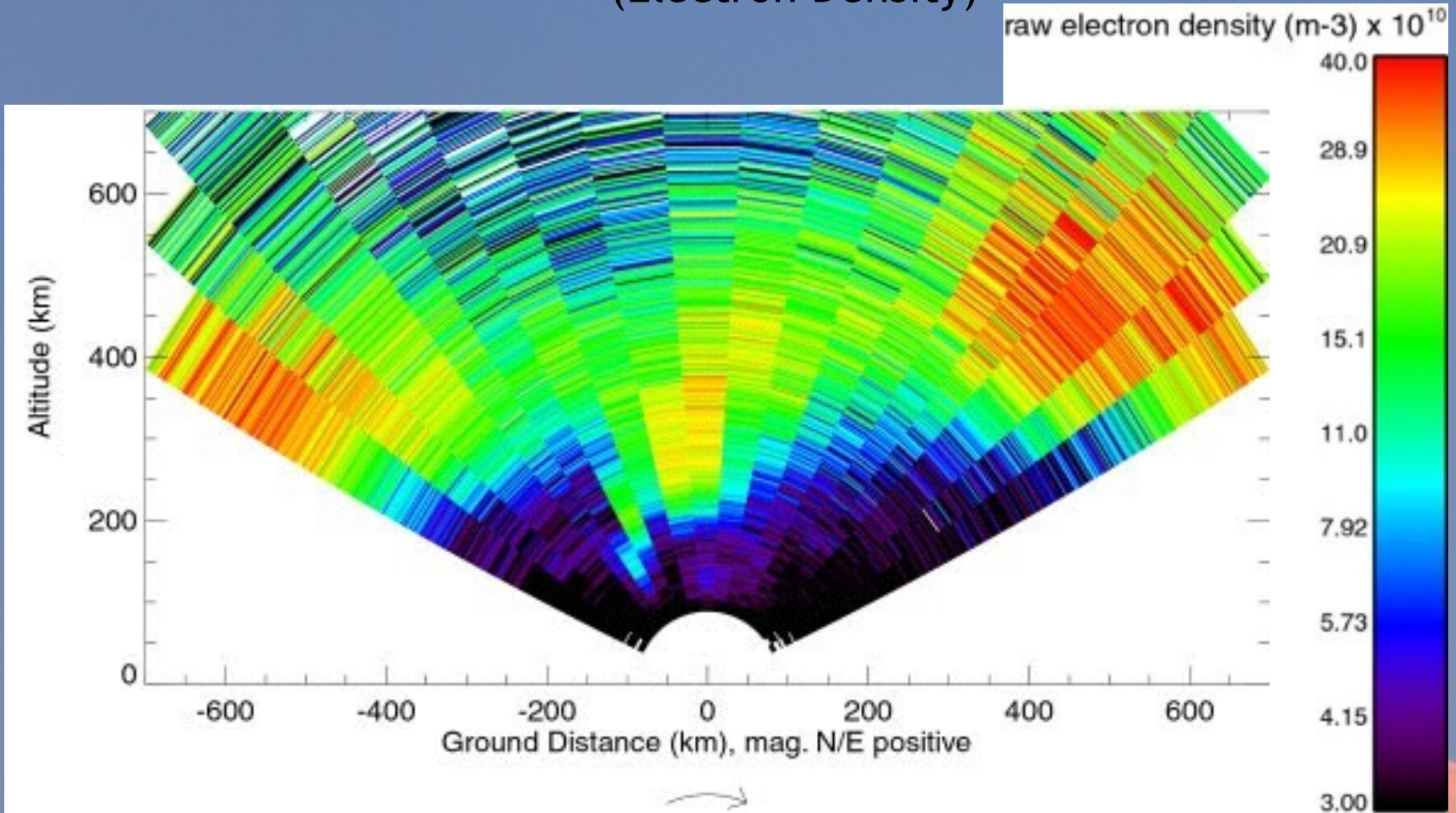
## EISCAT UHF RADAR

CP, uhf, tau2pl, 29 March 2006

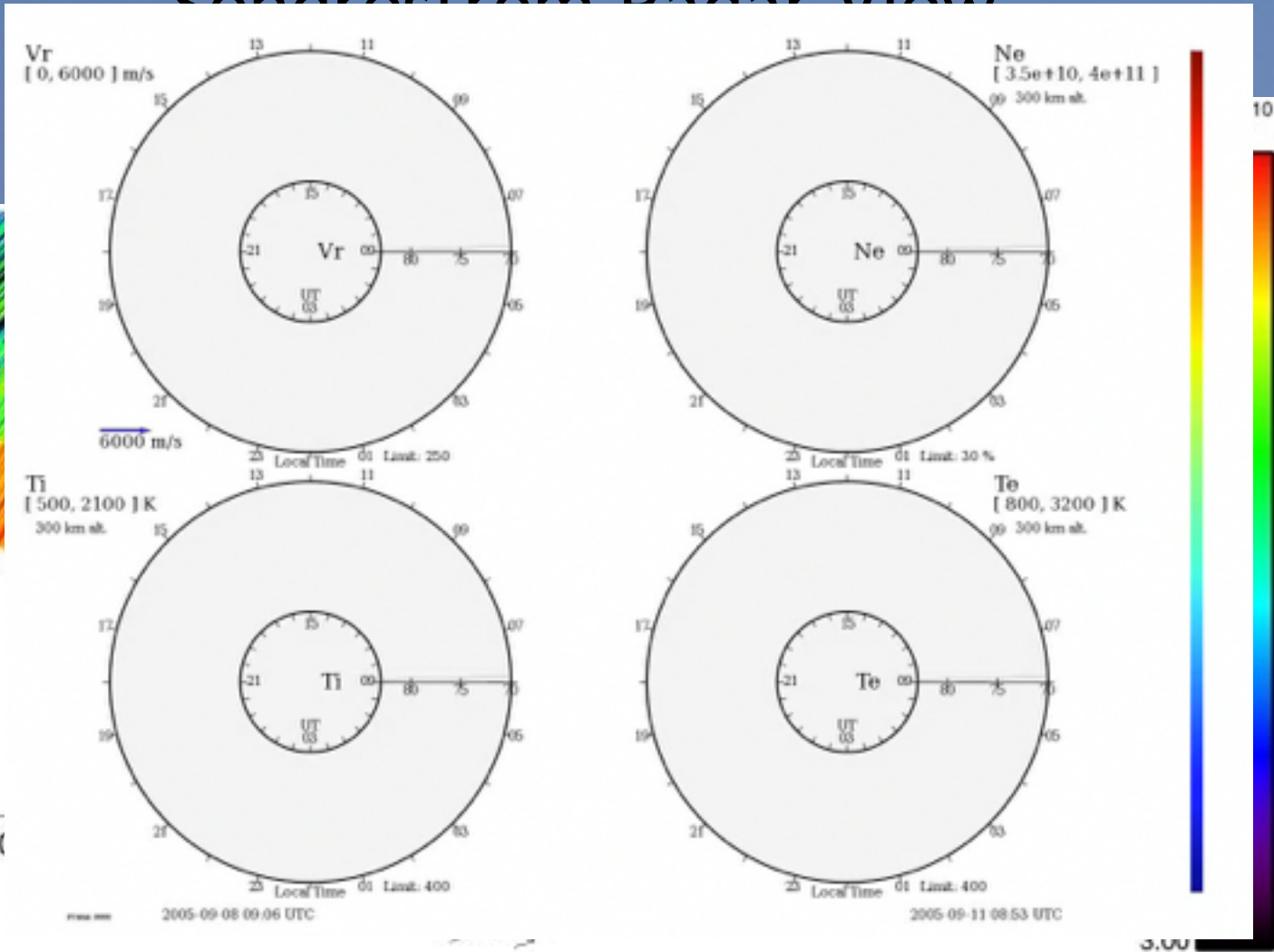
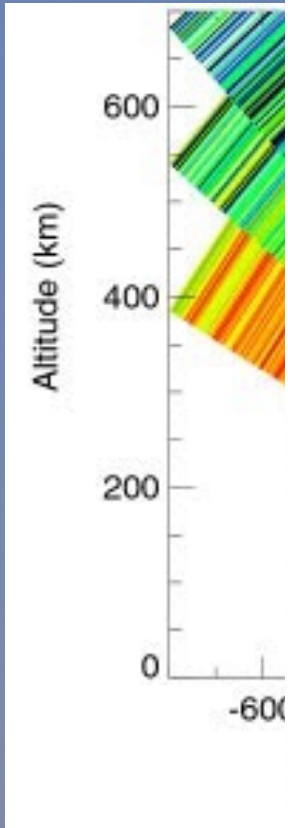




# Sondrestrom Radar View (Electron Density)



# Sondrestrom Radar View



And this is the level data we will work on in the MADRIGAL session...