Radar Physics Anthea J. Coster

<u>Outline</u>

Electromagnetic spectrum Radio Waves and Propagation Radar fundamentals Radar equation Range Resolution and pulsed radars Doppler

Useful Fourier transforms





Properties of Waves Relationship Between Frequency and Wavelength

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Speed of light, c c = 3x10⁸ m/sec = 300,000,000 m/sec

Frequency (1/s) =
$$\frac{\text{Speed of light (m/s)}}{\text{Wavelength }\lambda \text{ (m)}}$$

Examples:	Frequency	Wavelength
	100 MHz	3 m
	1 GHz	30 cm
	3 GHz	10 cm
	10 GHz	3 cm



Radio Waves

$$y(x, t) = A\cos(\omega t - kx + \phi_0)$$
Angular Frequency

$$\omega = 2\pi f = 2\pi/T$$
Wavenumber

$$k = 2\pi/\lambda$$
(a) $y(x, t)$ versus x at $t = 0$
Wave phase velocity

$$c = f\lambda = \omega/k = 3x10^8 m/s$$
Frequency $(1/s) = \frac{\text{Speed of light (m/s)}}{\text{Wavelength I (m)}}$

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Properties of Waves Constructive vs. Destructive Addition ιΛ, Σ Σ **Partially Constructive** Constructive (somewhat out of phase) (in phase) Σ MWW. MMMMMD Destructive **Non-coherent signals** (180° out of phase) (noise) 7

Phase Velocity, Group Velocity, Index of Refraction







$$n = \frac{c}{v_{\rm p}}.$$

Index of Refraction
$$n = \frac{c}{v_p}$$
. in the lonosphere

$$n^{2} = 1 - \frac{X}{1 - iZ - \frac{\frac{1}{2}Y^{2}\sin^{2}\theta}{1 - X - iZ}} \pm \frac{1}{1 - X - iZ} \left(\frac{1}{4}Y^{4}\sin^{4}\theta + Y^{2}\cos^{2}\theta(1 - X - iZ)^{2}\right)^{1/2}}$$

n is the index of refraction

$$X = \frac{\omega_N^2}{\omega^2} \quad Y = \frac{\omega_H}{\omega} \quad Z = \frac{\nu}{\omega} \quad \omega_N = \left(\frac{Ne^2}{\varepsilon_0 m_e}\right)^{\frac{1}{2}} \quad \omega_H = \frac{e|B|}{m_e}$$

 ω = the angular frequency of the radar wave,

$$Y_{L} = Y \cos\theta, \quad Y_{T} = Y \sin\theta,$$

 θ = angle between the wave vector \overline{k} and \overline{B} ,

 \overline{k} = wave vector of propagating radiation,

 \overline{B} = geomagnetic field, N = electron density

e = electronic charge, m_e = electron mass, ν = electron collision frequency and ε_0 = permittivity constant.

Refraction and Dispersion



ISR School 2017

From Attila Komjathy, JPL

Illustration of Atmospheric Effects

Elevation Refraction

Range Delay



Radio Propagation in the Ionosphere



Dispersion relation: the concept

Key concept for wave behavior within a propagation medium.

Describes the relationship between SPATIAL frequency (wavelength) and TEMPORAL frequency.

Some wave modes relate wavelength to frequency **linearly**, but waves in most media have **nonlinear** relation between wavelength and frequency.

Linear dispersion example:

EM radiation propagation through free space (wavelength / velocity = c)

Nonlinear dispersion example:

splitting of light through a prism (effective speed of light depends on wavelength due to glass' non-unity index of refraction)



http://weelookang.blogspot. com/2011/10/ejs-opensource-propagation-of.html

ISR 2017 Workshop: Arecibo 2017-07-24 to 2017-07-28 P. J. Erickson Wikipedia CC-3.0

Simple linear case: uniform phase velocity

$$\omega(k) = c \ k$$

Most propagation speeds depend nonlinearly on the wavelength and/or frequency.

NB: for a **nonlinear** dispersion relation, the pulse will typically spread in either spatial frequency or temporal frequency as a function of time.



ISR 2017 Workshop: Arecibo 2017-07-24 to 2017-07-28 P. J. Erickson Plasma dispersion relations

$$\epsilon(\omega, \vec{k}) = \text{function} \left(\frac{\omega^2}{k^2} \right)$$

Dielectric constant of the medium

Insert plasma dispersion relation here

$$n^{2} = \frac{c^{2}k^{2}}{\omega^{2}}$$
$$= 1 - \frac{\omega_{p}^{2}}{\omega^{2}}$$

$$\epsilon(\omega, \vec{k}) = \epsilon_0 (1 - \frac{\omega_p^2}{\omega^2}) \qquad v_p = \operatorname{sqrt}(1/\epsilon\mu_0) \\ v_p = c/n \\ n = c/\operatorname{sqrt}(1/\epsilon\mu_0) \\ n = c^*\operatorname{sqrt}(\epsilon\mu_0) \\ c = 1/\operatorname{sqrt}(\epsilon_0\mu_0) \\ n = \operatorname{sqrt}(\epsilon_\ell \epsilon_0)$$

Polarization



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TEM Waves: *Transverse electromagnetic (TEM) modes* neither electric nor magnetic field in the direction of propagation



Electromagnetic waves in free space propagate in TEM mode







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 - Radar equation
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RADAR RAdio Detection And Ranging



Radar observables:

- Target range
- Target angles (azimuth & elevation)
- Target size (radar cross section)
- Target speed (Doppler)
- Target features (imaging)

Radar Block Diagram



Radar Range Equation





Antennas







Antennas

•Four primary functions of an antenna for radar applications

- Impedance transformation (free-space intrinsic impedance to transmission-line characteristic impedance)
- Propagation-mode adapter (free-space fields to guided waves)
- Spatial filter (radiation pattern direction-dependent sensitivity)
- Polarization filter (polarization-dependent sensitivity)



Impedance transformer

•Intrinsic impedance of free-space, $\eta_o \equiv E/H$ is

$$\eta_0 = \sqrt{\mu_0/\epsilon_0} = 120 \ \pi \cong 376.7 \ \Omega$$

- •Characteristic impedance of transmission line, $\rm Z_{o}$ = $\rm V/I$
- •A typical value for Z_0 is 50 Ω .

•Clearly there is an impedance mismatch that must be addressed by the antenna. $_{26}^{26}$

Propagation-mode adapter

•During both transmission and receive operations the antenna must provide the transition between these two propagation modes.



Spatial filter

•Antennas have the property of being more sensitive in one direction than in another which provides the ability to spatially filter signals from its environment.





Radiation pattern of directive antenna.

Radiation Pattern - Antenna Gain



Polarization filter

Antennas have the property of being more sensitive to one polarization than another. This provides the ability to filter signals based on its polarization.

Example: Satellite tracking receive on both right-circular and leftcircular

Propagation Medium - Losses

Radio waves are affected by the medium they propagate in. Effects dependent on the refractive index of the medium and wave frequency

Radio waves are also reflected off of the surface

- Atmospheric attenuation
- Reflection off of earth's surface
- Over-the-horizon diffraction
- Atmospheric refraction







Attenuation usually measured in dB

SNR dB = $10\log_{10} \frac{signal power}{noise power}$

<u>dB value</u>	times by
<u>+30 dB</u>	1000
+20 dB	100
+3 dB	2
<u>-10 dB</u>	0.1
<u>-201</u> dB	0.01

Radar equation



Radar cross section tells us about the target properties

It is the effective target cross section as seen by the radar

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Radar Cross Section (RCS)



Radar Cross Section (RCS, or s) is the <u>effective</u> crosssectional area of the target as seen by the radar

measured in m², or dBm²

Hard targets vs. Soft targets



Volume scattering - lonosphere

- Volume scattering cross section σ_v has area/volume units
- Signal is proportional to range resolution
- What about the ionosphere ?
 Cross section of a single electron = 10⁻²⁸ m²
 Cross section of a bunch of electrons in a 10 km³ volume in the ionosphere assuming electron density = 10¹² /m³, is 10¹⁰ x 10¹² x 10⁻²⁸ = 10⁻⁶ m² !!)
 CAN be measured by an incoherent scatter radar.

Radar Range Equation





What the radar transmits: Pulses and waves



Cycles in a pulse.

PFISR frequency = 449 MHz Long pulse length = 480 μs # of cycles = 215520 ! Radar waveforms modulate the waves with on-off sequence

Pulsed Radar



Duty cycle = Pulse Length/IPP (10%) Average power = Peak power x Duty cycle (100 kW) PRF (Pulse Repetition Frequency) = 1/IPP (1kHz)

Duty cycle for a CW (continuous wave) radar 100%

Range Resolution

Range resolution is set by pulse length

Pulse length = τ_p , Range resolution = $c\tau_p/2$ for a single target.

Maximum unambiguous range



$$MUR = c*IPP/2$$

Pulse duration vs. Range resolution

Pulse Duration	Range Resolution
0.1 nsec	1.5 cm
1.0 nsec	15 cm
10 nsec	1.5 m
100 nsec	15 m
1 μsec	150 m
10 μsec	1.5 km
100 μsec	15 km
1 msec	150 km

What is a typical F region ISR pulselength?40

Radar Waveforms

What do radars transmit?



Radar Waveforms (cont'd.)





Signal Processing Pulse Compression

Problem: Pulse can be very long; does not allow accurate range measurement



Solution: Use pulse with changing frequency and signal process using "matched filter"



Detection of Signals in Noise



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- Doppler and Doppler Radars

Moving target - Doppler



Doppler

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Positive Doppler = target moving **toward** the observer **Negative** Doppler = target moving **away** from the observer

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 $f = c/\lambda$

Sign conventions

The Doppler frequency is negative (lower frequency, red shift) for objects receding from the radar

The Doppler frequency is positive (higher frequency, blue shift) for objects approaching the radar

These "color" shift conventions are typically also used on radar displays of Doppler velocity

Red: Receding from radar

Blue: Toward radar





Doppler shift frequency

Tx signal: $cos(2\pi f_o t)$

Return from a moving target: $cos[2\pi f_o(t + 2R/c)]$

If target is moving with a constant velocity: $R = R_o + v_o t$ then,

Return: $\cos[2\pi(f_o + f_o 2v_o/c)t + 2\pi f_o R_o/c]$ Doppler frequency: $-2f_o v_o/c = -2v_o/\lambda_o$

Pulsed Doppler Radar system



LUNCHTIME !!!

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