



Group 4 Experiment Type B: Regional Vector

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Motivation

- We ♥ the ionosphere
- Measuring ion velocity as a function of height and time
- Simultaneous measurements of electron density and LOS ion velocity
- Positional precision
- Mid-latitude summer nighttime anomalous ionospheric electron density enhancement (MSNA)

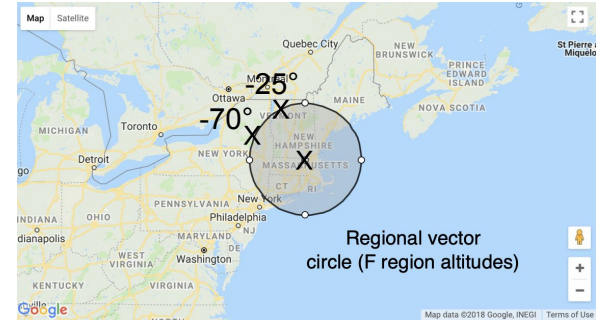


Figure 1. Panel obtained from Dr. Erickson's presentation. Top-down view of Experiment B.

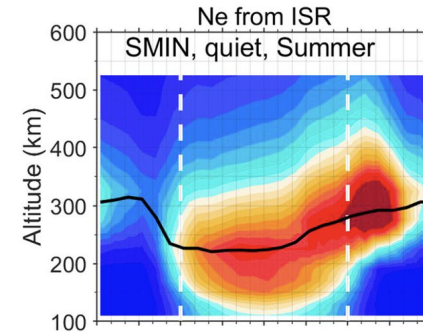


Figure 2. Panel obtained from Cai, Y. et al. (2022, *GRL*).

Review of Experiment B: Regional Vector



8-10pm LT (00-02 UT)

Constant data (~90 elevation) in Zenith

45 deg elevation at both MISA azimuths

Recorded data at two azimuths (-25°, -70°) (Currently MISA azimuth range is limited)

Zenith and MISA: 3 minutes



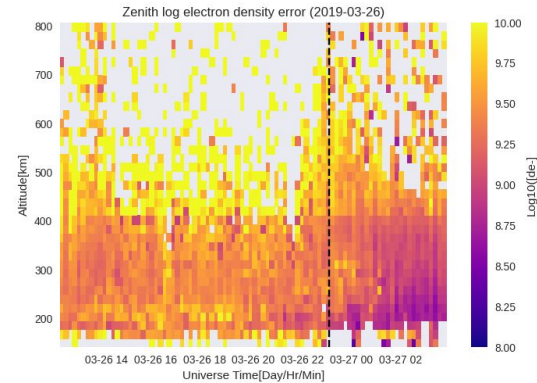
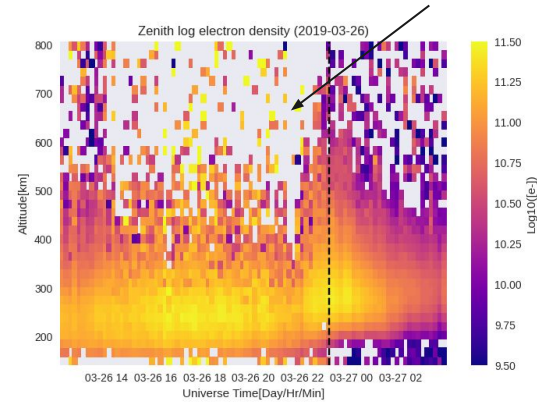
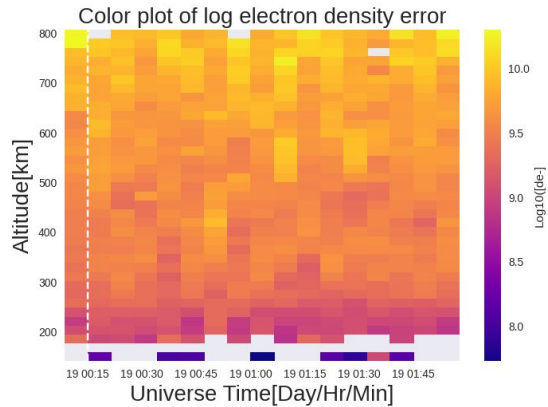
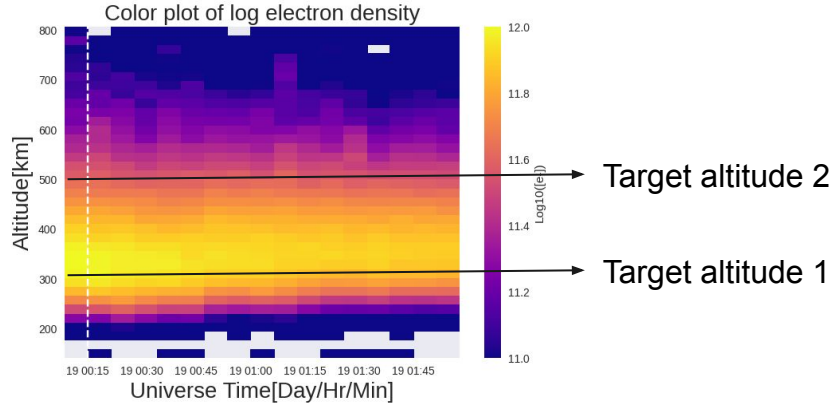
Comparison between two different seasons



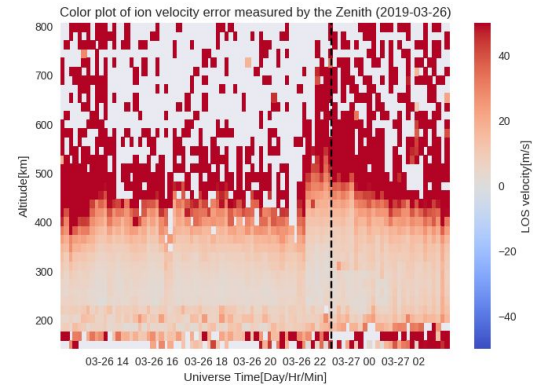
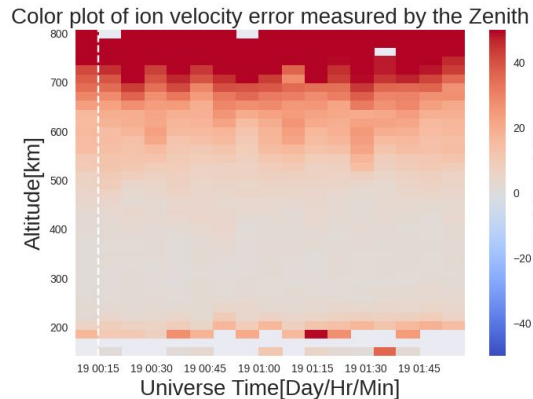
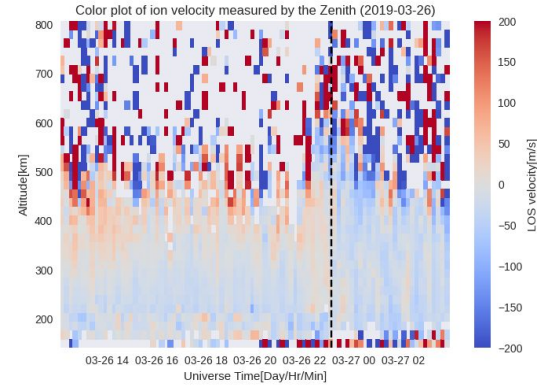
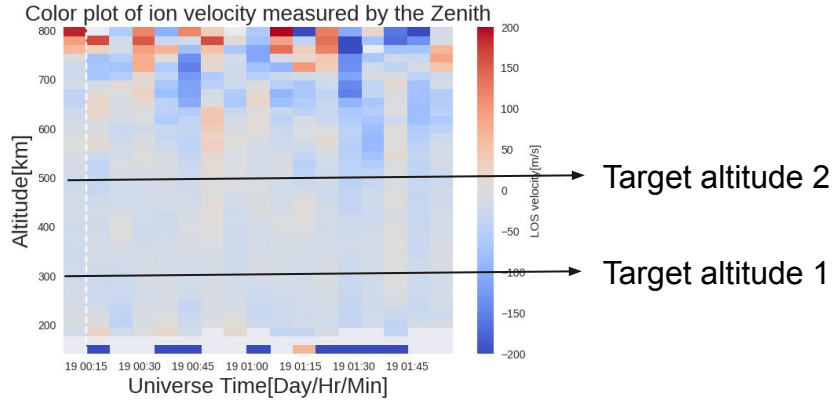
- Ionospheric behavior comparison for July-21-2022 v.s. March-26-2019
 - Electron Density
 - Enhancement at a range of altitude
 - Zenith Line of Sight velocity
 - Velocity components in magnetic field coordinates
- Different MISA azimuths between the two runs
 - July-21-2022: Azimuths = [-25, -70] deg. Difference = 45 deg.
 - March-26-2019: Azimuths = [-12, -40.5] deg. Difference = 28.5 deg.

Electron Density and error (Zenith)

Pulse length = 9.6×10^{-4}



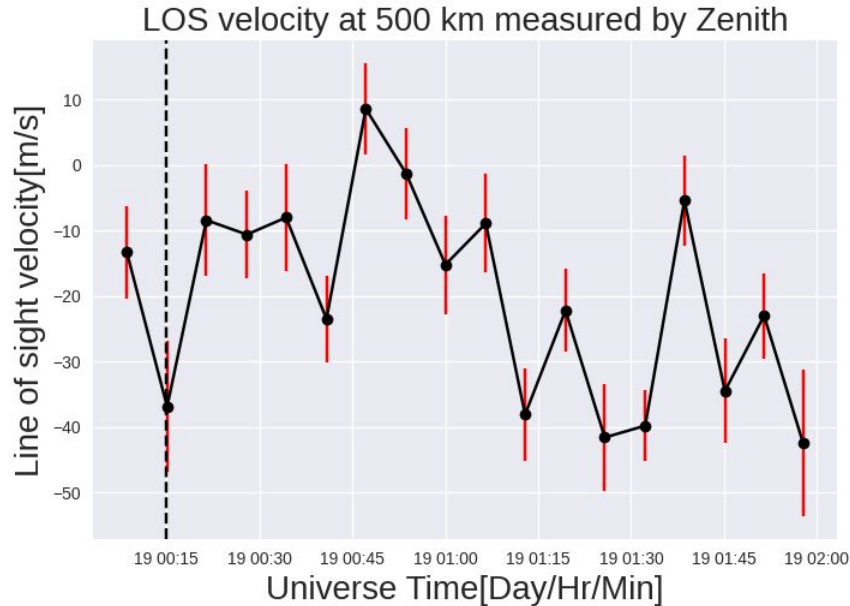
LOS ion velocity and error (Zenith)



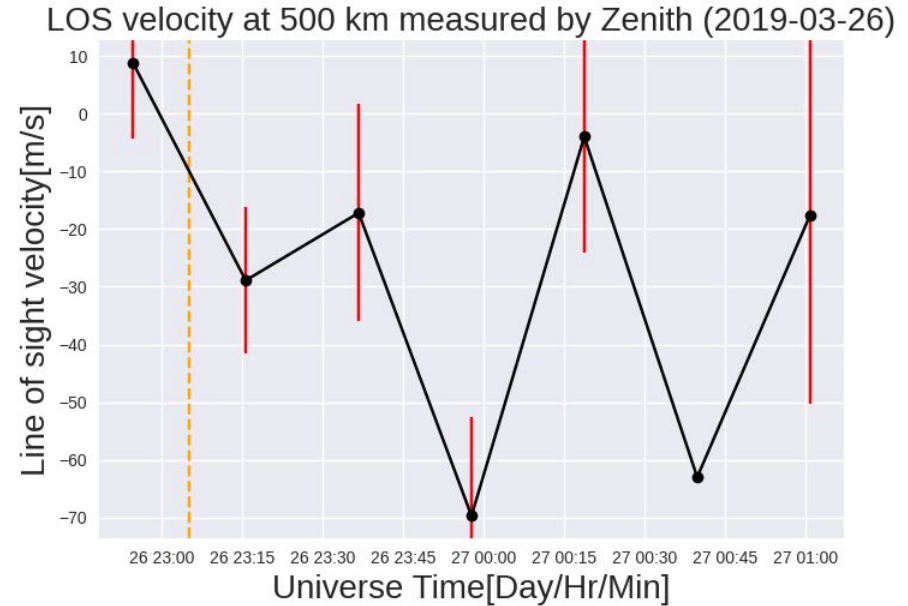
LOS ion velocity at 500 km



July-21-2022



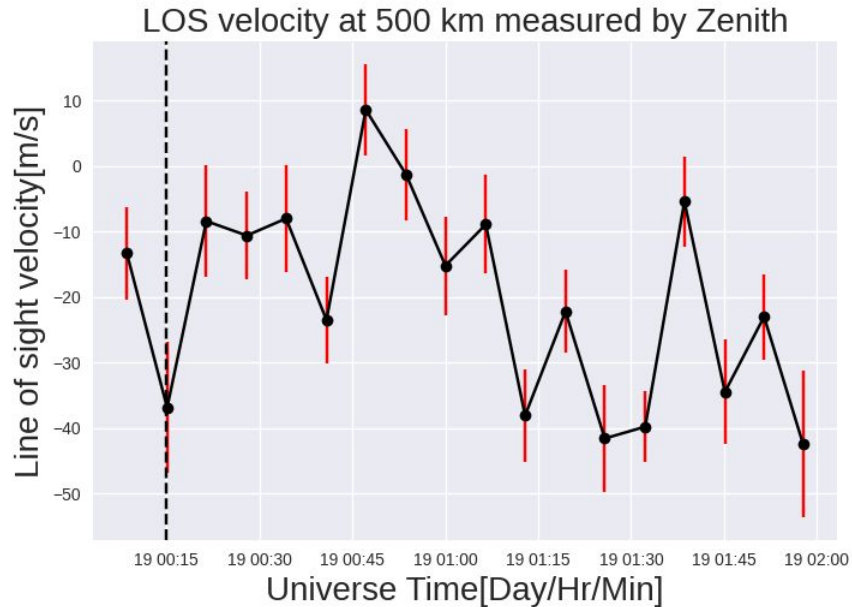
March-26-2019



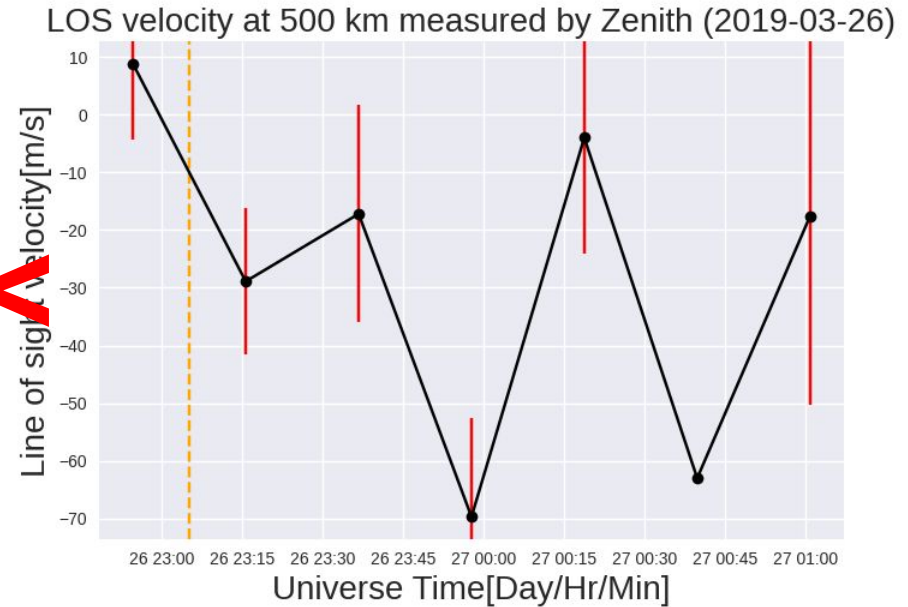
Error bars at 500 km



July-21-2022



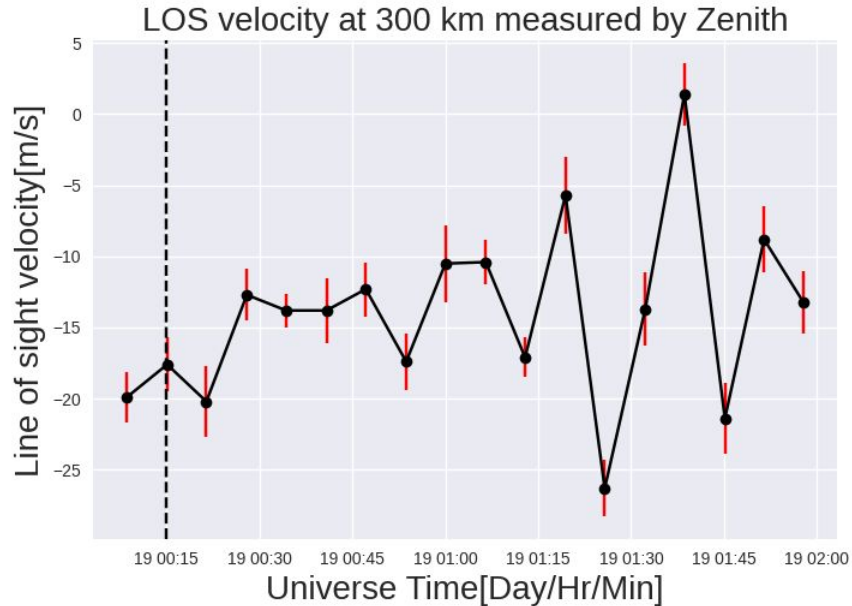
March-26-2019



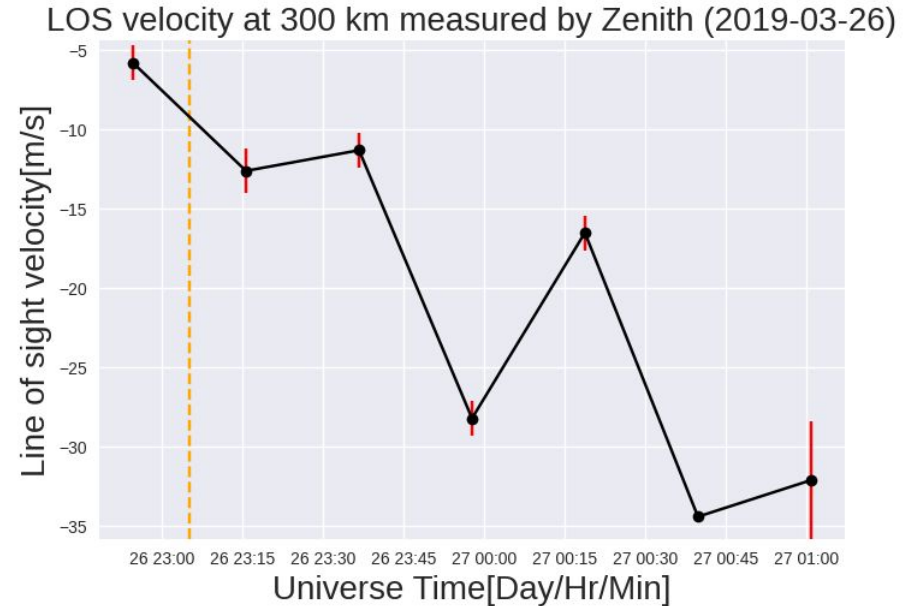
LOS ion velocity at 300 km



July-21-2022



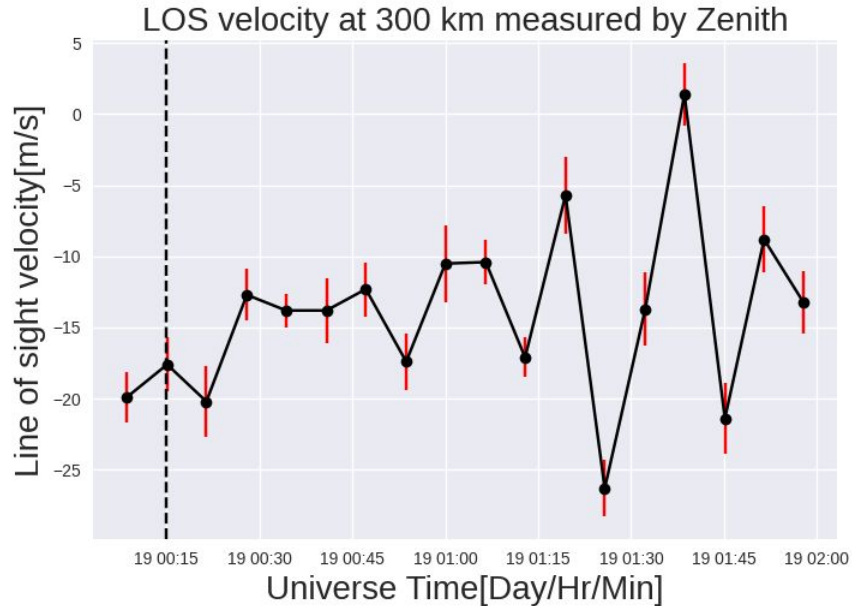
March-26-2019



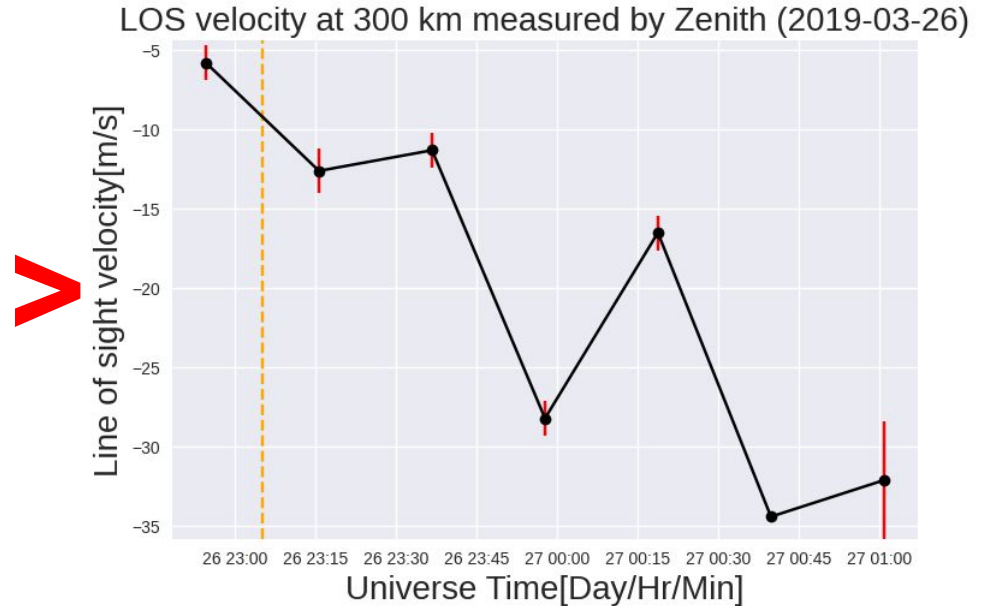
Error bars at 300 km

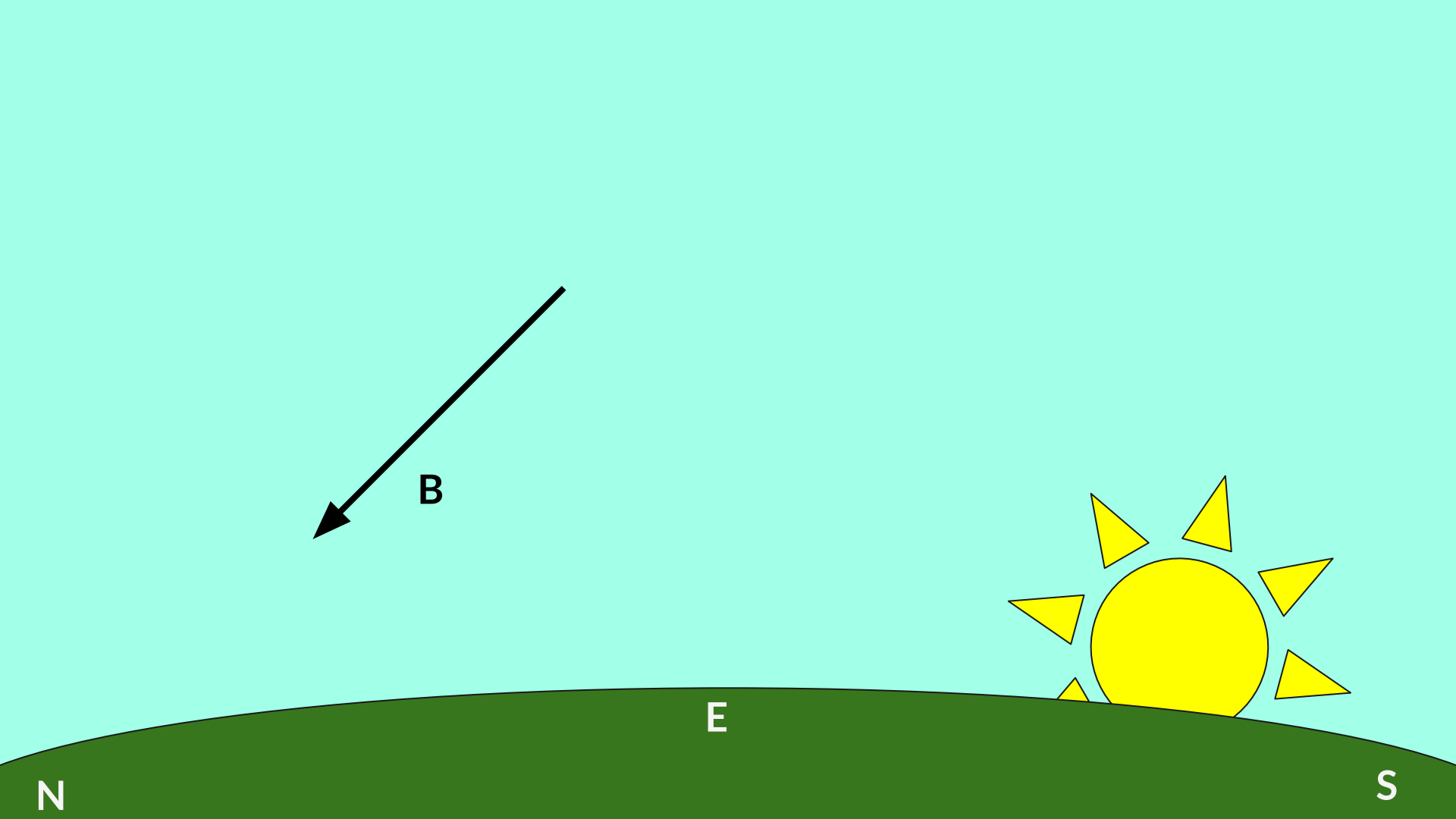


July-21-2022



March-26-2019



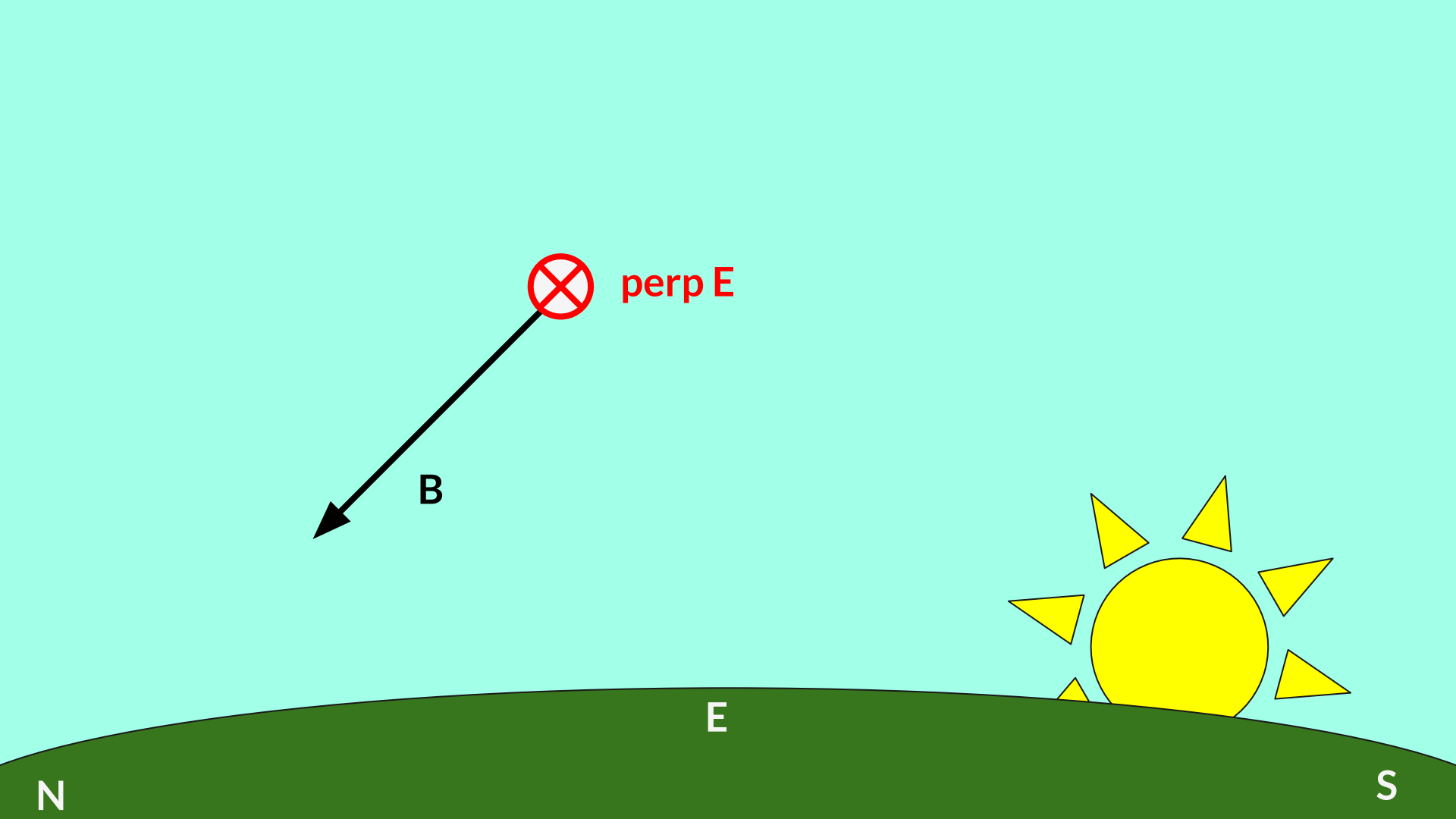


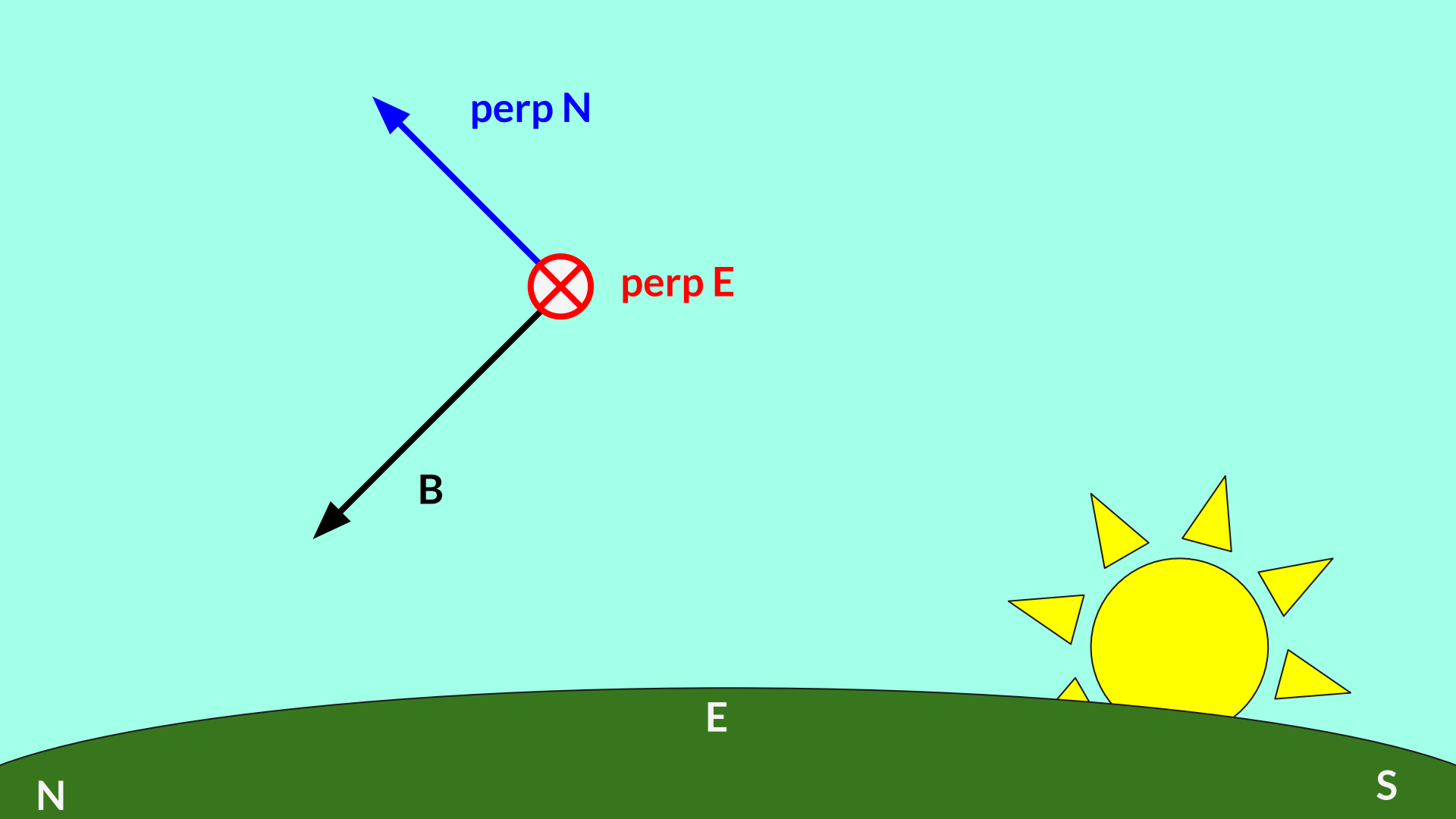
N

E

S

B

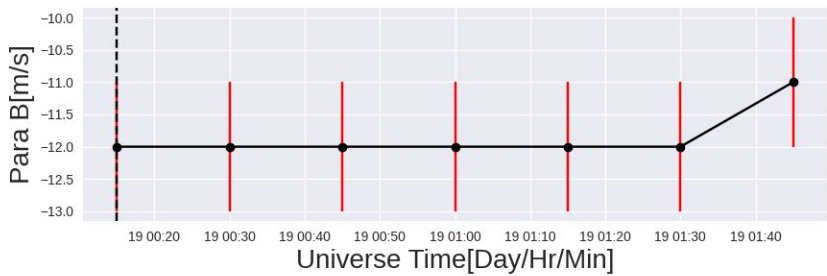
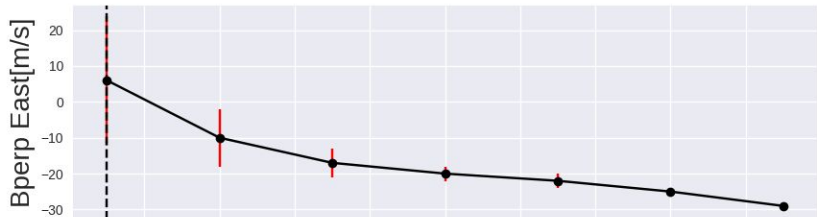
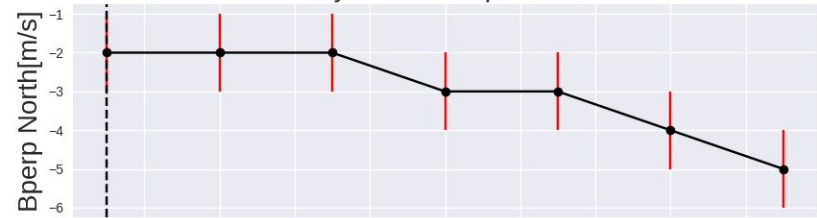




Error bars for velocity components (300 km)

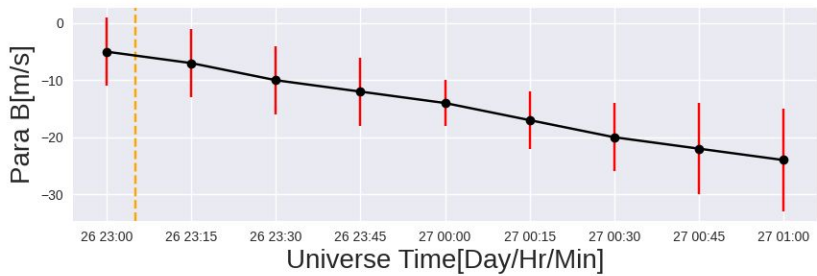
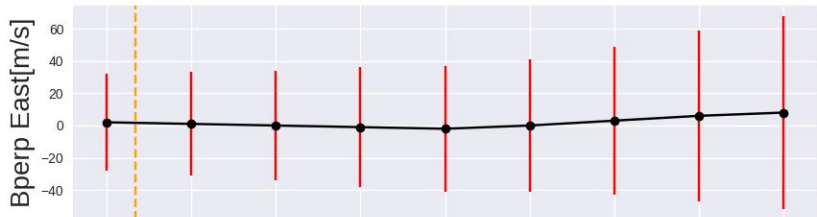
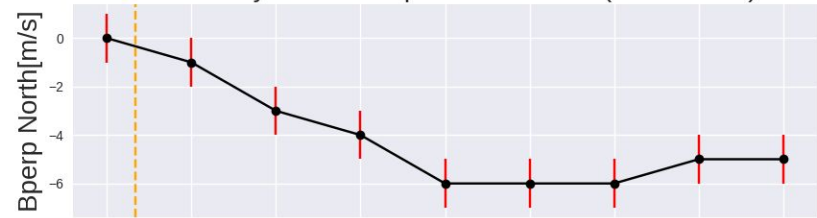
Azimuth difference = 45°

Ion velocity vector computed at 300 km



Azimuth difference = 28.5°

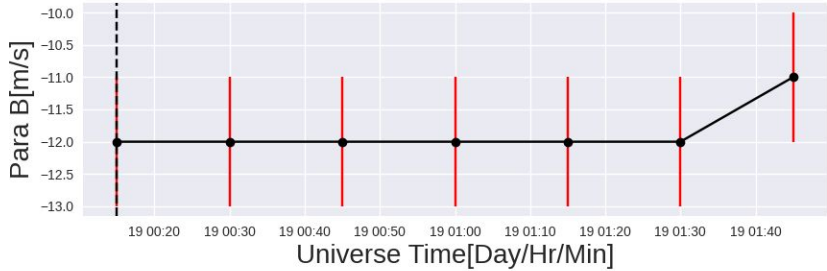
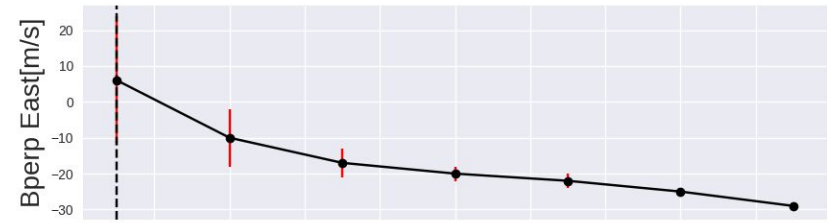
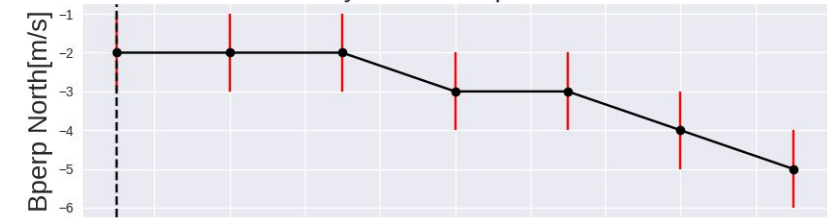
Ion velocity vector computed at 300 km (2019-03-26)



Error bars for velocity components (300 km)

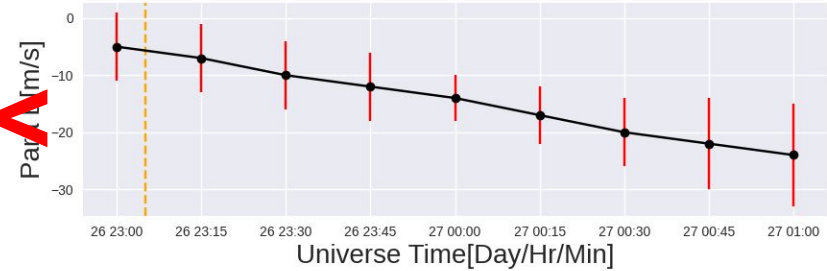
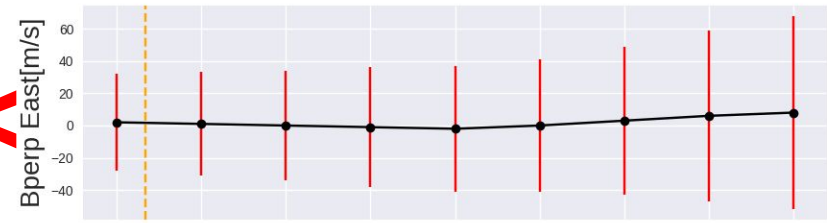
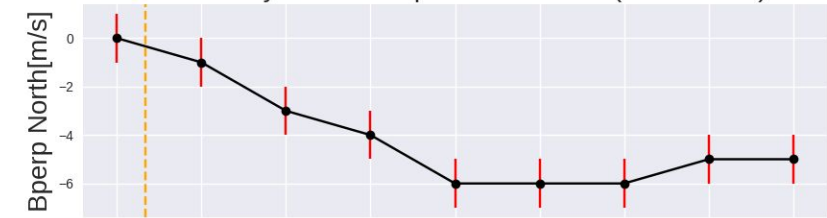
Azimuth difference = 45°

Ion velocity vector computed at 300 km

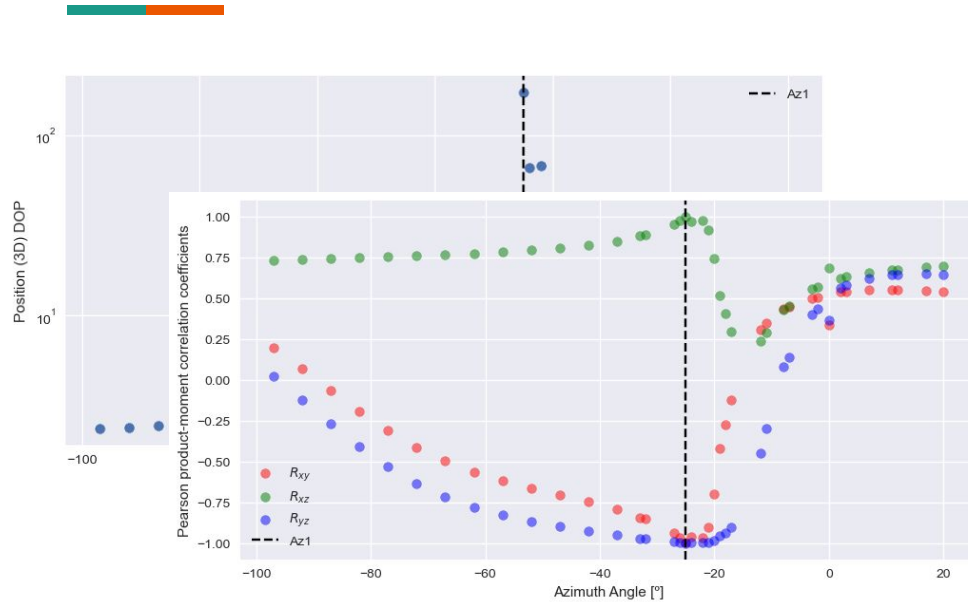


Azimuth difference = 28.5°

Ion velocity vector computed at 300 km (2019-03-26)



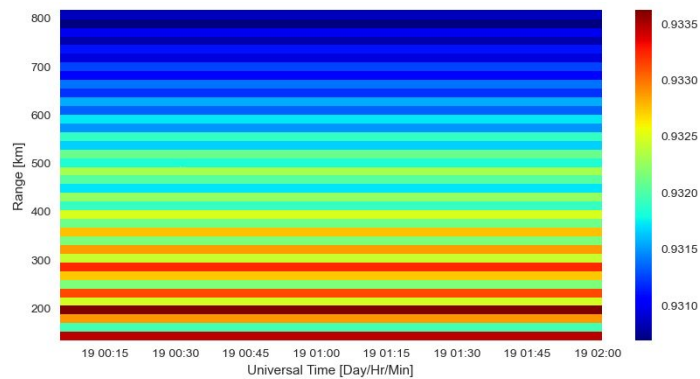
Time to look at geometry, matrices, and error propagation



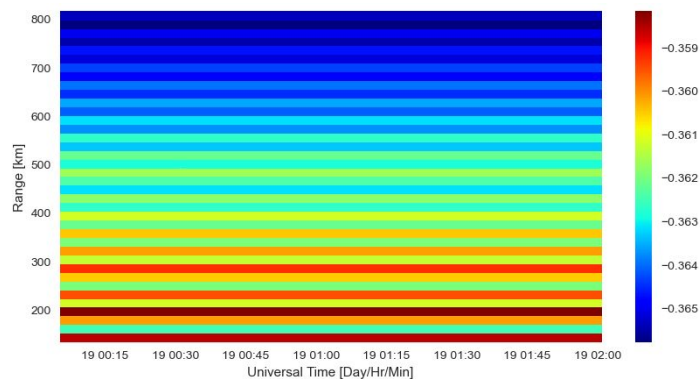
Zenith Single-Pulse

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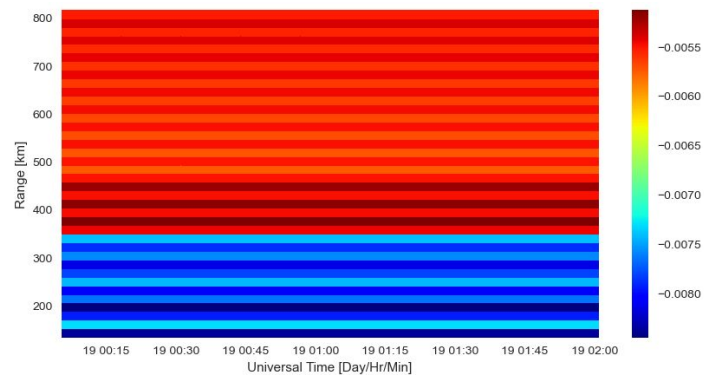
CZR



CXR



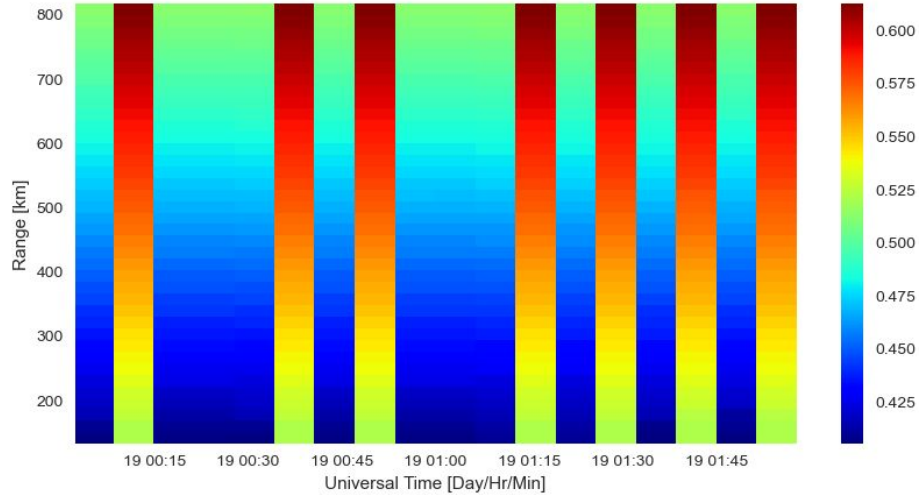
CYR



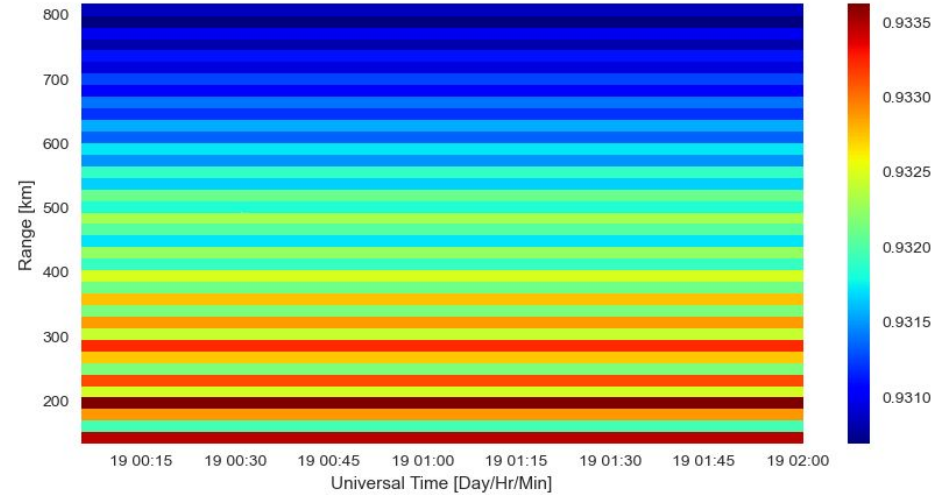
What about MISA single-pulse? Let's compare



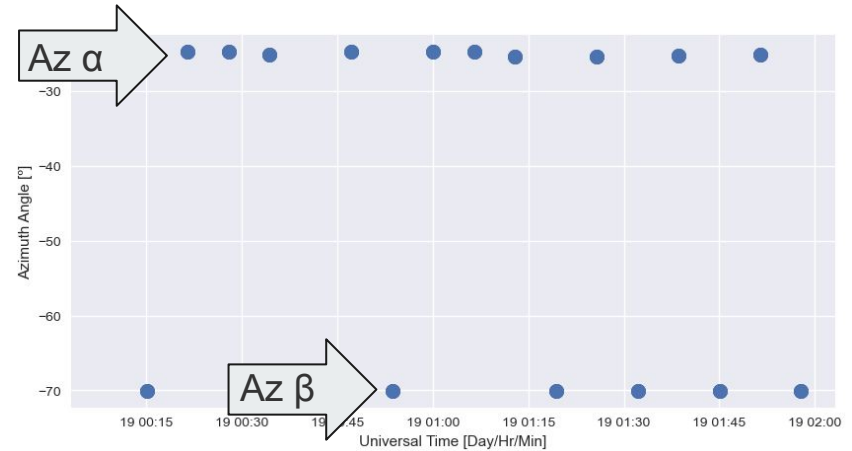
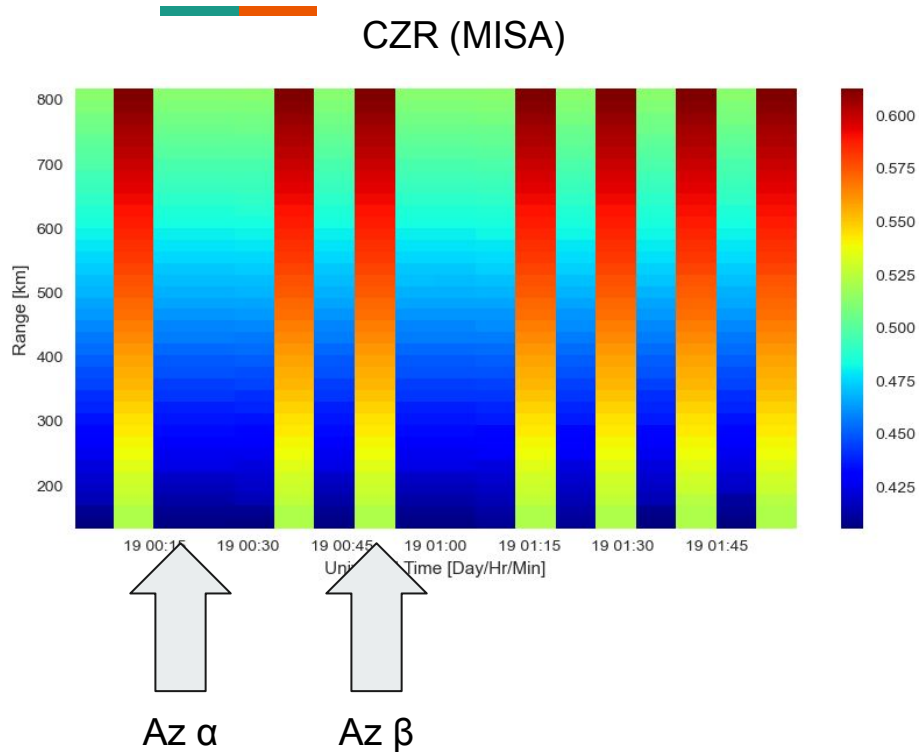
CZR (MISA)



CZR (Zenith)



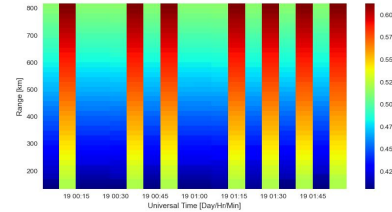
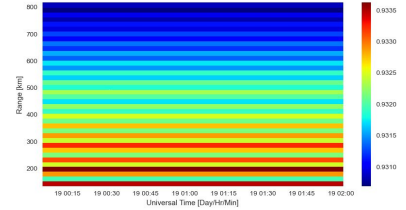
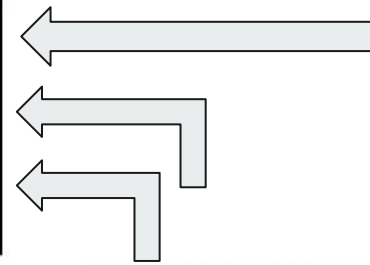
What about MISA single-pulse? Let's compare



The matrix we construct and why

Each coefficient is the “x/y/z-cosine of the radar line-of-sight with respect to apex coords.”

$$M = \begin{bmatrix} \text{cZr}^Z & \text{cyr}^Z & \text{cxr}^Z \\ \text{cZr}^{M1} & \text{cyr}^{M1} & \text{cxr}^{M1} \\ \text{cZr}^{M2} & \text{cyr}^{M2} & \text{cxr}^{M2} \end{bmatrix}$$



The matrix we construct and why

$$M = \begin{bmatrix} \text{cZr}^Z & \text{cyr}^Z & \text{cxr}^Z \\ \text{cZr}^{M1} & \text{cyr}^{M1} & \text{cxr}^{M1} \\ \text{cZr}^{M2} & \text{cyr}^{M2} & \text{cxr}^{M2} \end{bmatrix}$$

$$Q = AA^T, \text{ where } A = M^{-1} \text{ and } Q = \begin{bmatrix} \sigma_x^2 & \sigma_{xy} & \sigma_{xz} \\ \sigma_{xy} & \sigma_y^2 & \sigma_{yz} \\ \sigma_{xz} & \sigma_{yz} & \sigma_z^2 \end{bmatrix}$$

Some useful parameters we can now obtain

$$PDOP = \sqrt{\sigma_x^2 + \sigma_y^2 + \sigma_z^2} = \text{Trace}(Q)$$

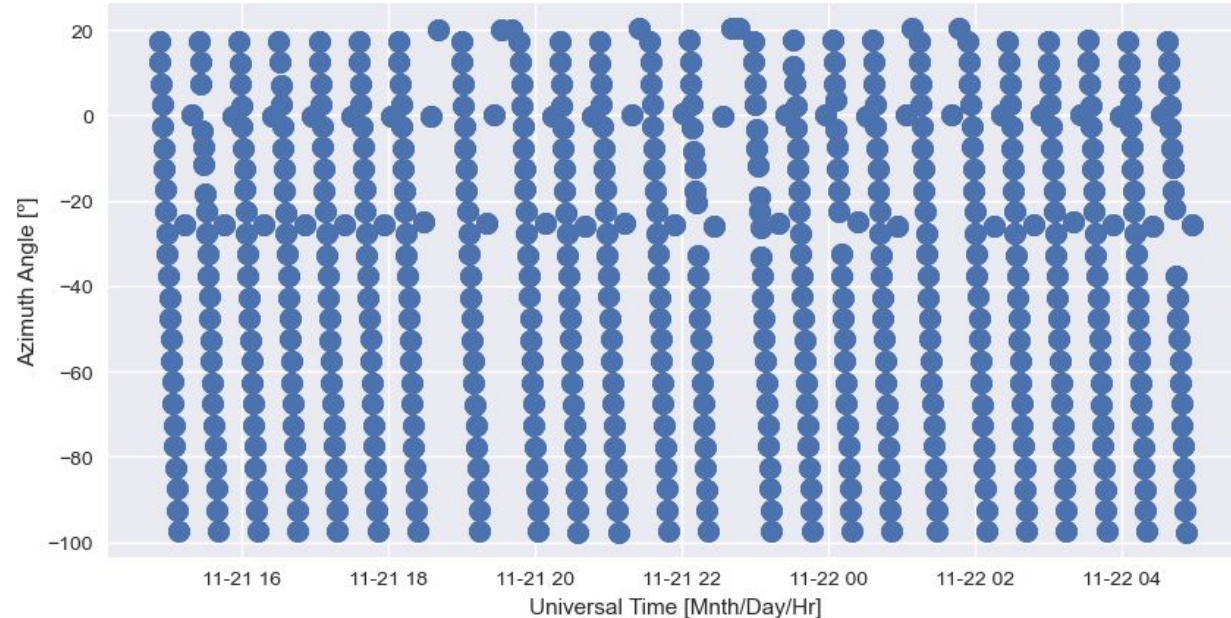
$$R_{ij} = \frac{\sigma_{ij}}{\sqrt{\sigma_i^2 \sigma_j^2}}$$

Wide Coverage Azimuth Scan Experiment (2019-11-21)

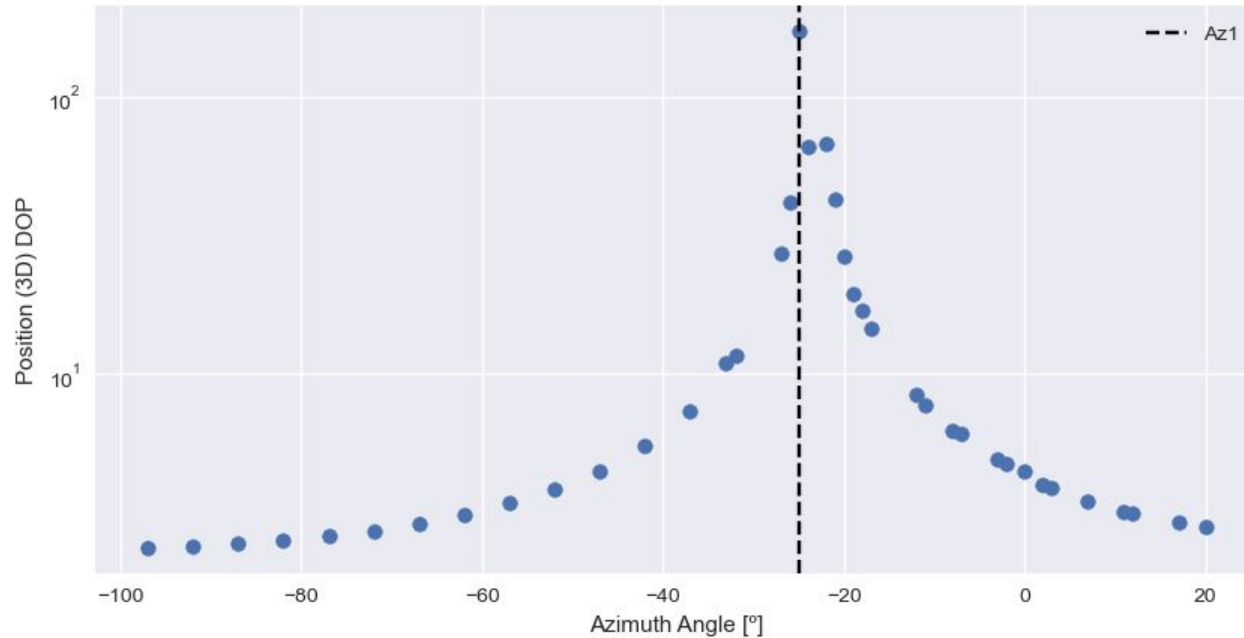
Disclosure:

6° of elevation,
not 45°

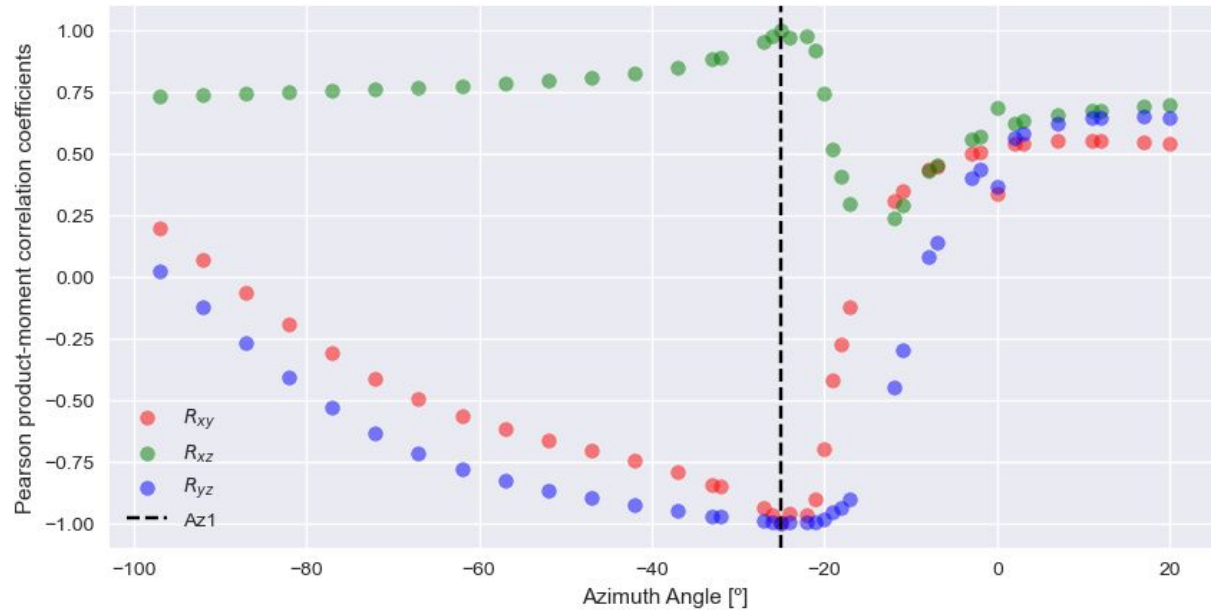
$$\begin{bmatrix} \text{cZr}^Z & \text{cyr}^Z & \text{cxr}^Z \\ \text{cZr}^{M1} & \text{cyr}^{M1} & \text{cxr}^{M1} \\ \text{cZr}^{M2} & \text{cyr}^{M2} & \text{cxr}^{M2} \end{bmatrix}$$



Positional (3D) Dilution of Performance



Pearson Correlation Coefficient



Conclusion



Enhanced electron densities at altitude range approximately 250-550[km]

Rapid changes and increased downward ion velocities after sunset.

Smaller MISA azimuth difference = bigger error bars in magnetic coordinates

The PDOP and Pearson correlation coefficient are powerful diagnostic quantities

An interactive lecture supplement for next year's summer school?