## Homework \#7 - April 9, 2009

Due: April 15, 2009 at recitation
No late homework accepted

1. [20 points] Each network shown below has a non-zero initial state at $t=0$, as indicated. Find the network $v(t)$ and $i(t)$ respectively for $t \geq 0$. Note that the impulse inputs are delayed. Hint: you may find it intuitively easier to use superposition, and Thevenin and Norton equivalents.

2. [20 points] The network shown below contains a $2-\mathrm{mA}$ current source, a resistor and an inductor all in parallel. The network has been assembled for a long time. At $\mathrm{t}=0$ the current source turns off, after which the common voltage $v(t)$ is measured as shown below. From the measured voltage, determine the resistance of the resistor and the inductance of the inductor.


3. [20 points] The network shown below contains a capacitor and an inductor. The network states are observed to oscillate with a frequency of $10^{7} \mathrm{rad} / \mathrm{s}$. Further, the peak value of $\mathrm{v}_{\mathrm{C}}$ is observed to be 100 mV , and the peak value of $\mathrm{i}_{\mathrm{L}}$ is observed to be 20 mA .
(A) What are the values of C and L ?
(B) How much energy is stored in the network?
(C) Suppose a resistor is placed in parallel with the inductor and capacitor. What resistance would it have if the energy stored in the network is then observed to decay by the factor of $1 / \mathrm{e}$ in $20 \mu \mathrm{~s}$ ?

4. [40 points] This problem makes use of the ELVIS iLab to study the large-signal and smallsignal response of a common-source MOSFET-resistor inverter/amplifier that is loaded with a large capacitor at its output. The circuit is shown below. It is the same circuit studied in Problem 5.1, with the addition of an output capacitor. In this problem, you will measure the large-signal and small-signal step responses of the inverter/amplifier and compare the time constants, which characterize those responses to predictions based on the models developed in class.

As discussed often in class, the MOSFET-resistor circuit shown above behaves both as an inverter and as an amplifier, depending on how it is used. When this circuit is loaded with a capacitor, it exhibits interesting dynamics. To study those dynamics you will first measure the large-signal step response of the circuit as an inverter, and extract the relevant time constants. You will then measure the small-signal step response of the circuit acting as an amplifier, and again extract the relevant time constants. Finally, using the models developed in class, you will estimate the values of the time constants, and compare those estimates with the experimentally-measured time constants.


The measurements are carried out in Parts (A) and (B) below. To carry out the measurements, log in to iLab and launch the ELVIS Lab Client. When you do, the circuit shown above will appear on the canvas.
(A) Experimentally characterize the large-signal switching behavior of the capacitor-loaded inverter. To do so, first select the signal generator (FGEN), and set its parameters to WaveForm $=$ SQUARE, Frequency $=10 \mathrm{~Hz}$, Amplitude $=1 \mathrm{~V}$, and Offset $=0 \mathrm{~V}$. Second, select the output measurement unit (SCOPE) and choose a suitable sampling rate that will allow you to see at least one full cycle of the output waveform with adequate resolution. Note that the system will allow you to take a maximum of 201 data samples at the output. Third, run the experiment. Finally, select $\mathrm{v}_{\mathrm{IN}}$ for the Y 1 axis and $\mathrm{v}_{\text {OUT }}$ for the Y2 axis, and use linear axes for both. When the figure resembles what you expect, capture a screen shot.

From the measured data, extract the pull-up (rising output) and pull-down (falling output) time constants. For this, you may find it useful to zoom in on the respective edges of vout to clearly observe the exponential portion of the transition, and use the graphical technique discussed in class to estimate the time constant. This might require additional measurements. Turn in any marked-up screen shots that you produce.
(B) Consider now the small-signal behavior of the circuit acting as an amplifier. Reduce the Amplitude to 120 mV . Select an offset that gives you an output bias point close to 0 V . You may need to try different values of the input offset to achieve the desired bias. An output bias within $\pm 300 \mathrm{mV}$ of 0 V is acceptable. Now, measure the square-wave response of the circuit. Capture a screen shot and extract the time constants of the response to a rising step input and a falling step input. Turn in any marked-up screen shots that you produce.
(C) Based on the analysis discussed in class, derive large-signal models for the pull-up (rising output) and pull-down (falling output) time constants of the MOSFET-resistor inverter driving a capacitor. Note that: (1) a typical value of $\mathrm{R}_{\mathrm{ON}}$ is $10 \Omega$ for the 2 N 7000 MOSFET; (2) the resistance of the pull-up resistor is $500 \Omega$; and (3) the capacitance of the load capacitor is $10 \mu \mathrm{~F}$. Quantitatively estimate the time constants that you expect for this inverter and compare the estimated time constants to those obtained experimentally. Comment on any discrepancies.
(D) Based on the analysis discussed in class, derive models for the time constant associated with the small-signal response of the MOSFET-resistor amplifier driving a capacitor. For this, you should derive a small-signal equivalent circuit model for the amplifier and then derive the time constant for the step response. In doing so, assume that the 2N7000 MOSFET is characterized by the typical values of $\mathrm{K}=0.14 \mathrm{~A} / \mathrm{V}^{2}$ and $\mathrm{V}_{\mathrm{T}}=1.9 \mathrm{~V}$. Quantitatively estimate the time constant that you expect for the step response of the amplifier and compare the estimated time constant to those determined experimentally. Comment on any discrepancies.

